



Letter

The study of weak decays induced by $\frac{1}{2}^+ \rightarrow \frac{3}{2}^-$ transition in light-cone sum rules

T.M. Aliev^{a, *}, S. Bilmis^{a, b,}, M. Savci^{a,}

^a Department of Physics, Middle East Technical University, Ankara, 06800, Turkey

^b TUBITAK ULAKBIM, Ankara, 06510, Turkey



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ABSTRACT

In this study, we analyzed the weak decays induced by $J^P = \frac{1}{2}^+ \rightarrow \frac{3}{2}^-$ transitions within the light-cone sum rules. Specifically, semileptonic decays of the bottom baryons into the P-wave baryons $\Lambda_b \rightarrow \Lambda_c(2625)\ell\nu$ and $\Xi_b \rightarrow \Xi_c(2815)\ell\nu$, as well as nonleptonic $\Lambda_b \rightarrow \Lambda_c(2625)\pi(\rho)$ and $\Xi_b \rightarrow \Xi_c(2815)\pi(\rho)$ decays are investigated. The form factors for the considered transitions are obtained within the sum rules method. With the calculated form factors, the decay widths of the processes are determined. Up to now, only the decay width for $\Lambda_b^0 \rightarrow \Lambda_c^+\mu^- \nu_\mu$ has been measured among the considered decays, and we observe that our finding is quite compatible with the measurement. We also compare our results with the predictions of other approaches.

1. Introduction

The study of weak decays of bottom baryons is a promising area in heavy flavor physics. Bottom baryons, due to their higher mass, exhibit numerous decay modes, making them an excellent testing ground for Quantum Chromodynamics (QCD) and exploring the possibility of new physics beyond the Standard Model (SM). The analysis of $b \rightarrow c$ transitions holds phenomenological importance for the precise determination of the Cabibbo-Kobayashi-Maskawa (CKM) matrix element V_{cb} , as well as for testing the lepton universality [1–7] and searching for new physics beyond the Standard Model. For these reasons, the semileptonic and nonleptonic decays of the bottom baryons to ground state charmed baryons have been comprehensively discussed in the literature within various theoretical frameworks such as lattice QCD [8,9], QCD sum rules [10–12], light cone QCD sum rules [13–15], and various phenomenological models [16–28].

However, the semileptonic decays of the bottom baryons into the P-wave baryons have received less attention. Nonetheless, few studies are exploring the decays of the heavy bottom baryons to the excited P-wave baryons using different approaches like the constituent quark model [16], covariant confined model [25], lattice QCD [29], and light front-quark model [27,30].

In this study, we focus on weak decays involving two heavy baryons, specifically analyzing two semileptonic decays, $\Lambda_b \rightarrow \Lambda_c(2625)\ell\nu$ and $\Xi_b \rightarrow \Xi_c(2815)\ell\nu$, as well as nonleptonic decays, $\Lambda_b \rightarrow \Lambda_c(2625)M$ and $\Xi_b \rightarrow \Xi_c(2815)M$, where M represents the π or ρ meson. It is important to note that experimental data is only available for the $\Lambda_b \rightarrow \Lambda_c(2625)\ell\nu$ decay. The objectives of this work are twofold. First, we aim to compare the theoretical results for the $\Lambda_b \rightarrow \Lambda_c(2625)\ell\nu$ decay with the available experimental data. Second, we aim to provide theoretical predictions for the branching ratios of the semileptonic $\Xi_b \rightarrow \Xi_c(2815)\ell\nu$ decay and the nonleptonic $\Lambda_b \rightarrow \Lambda_c(2625)M$ and $\Xi_b \rightarrow \Xi_c(2815)M$ decays, which have not yet been measured but have the potential of being discovered with the upgraded LHCb. One of the main challenges in the theoretical studies of these decays is as follows: The interpolating current for $J = \frac{3}{2}$ baryon not only interacts with positive and negative parity $J = \frac{3}{2}$ baryons but also with $J^P = \frac{1}{2}^-$ baryon. This interaction leads to the unwanted contributions. To remove this pollution, the combinations of the sum rules corresponding to different Lorentz structures are constructed.

The work is organized as follows: In Sec 2, the sum rules for the relevant form factors are derived. In Sec. 3, the numerical analysis is performed to determine the form factors, and with the obtained results, the decay widths of the considered transitions are estimated. The last section contains our conclusion.

* Corresponding author.

E-mail addresses: taliev@metu.edu.tr (T.M. Aliev), sbilmis@metu.edu.tr (S. Bilmis), savci@metu.edu.tr (M. Savci).

2. The light-cone sum rules of $H_b \rightarrow H_c$ transition form factors

For the sake of simplicity, we will denote $\Xi_b(\Lambda_b)$ and $\Xi_c(\Lambda_c)$ baryons as H_b and H_c , respectively, for further discussions. The transition form factors for $H_b(\frac{1}{2}^+) \rightarrow H_c(\frac{3}{2}^+)$ induced by the $V - A$ current $\bar{c}\gamma_\mu(1 - \gamma_5)b$ are defined as [24],

$$\begin{aligned} & \langle H_c(p', s) | \bar{c}\gamma_\mu(1 - \gamma_5)b | H_b(p, s) \rangle \\ &= \bar{u}_\alpha(p', s) \left\{ \left[\frac{p_\alpha}{m_1} \left(\gamma_\mu F_1^+ + \frac{p_\mu}{m_1} F_2^+ + \frac{p'_\mu}{m_+} F_3^+ \right) + g_{\mu\alpha} F_4^+ \right] \gamma_5 \right. \\ & \left. - \left[\frac{p_\alpha}{m_1} \left(\gamma_\mu G_1^+ + \frac{p_\mu}{m_1} G_2^+ + \frac{p'_\mu}{m_+} G_3^+ \right) + g_{\mu\alpha} G_4^+ \right] \right\} u(p, s), \end{aligned} \quad (1)$$

where $u_\alpha(p')$ and $u(p)$ are the Rarita-Schwinger and Dirac spinors, m_1 and m_+ are the masses of the initial and final baryons, respectively, and F_i^+ and G_i^+ are the form factors. The matrix element for $H_b(\frac{1}{2}^+) \rightarrow H_c(\frac{3}{2}^-)$ transition can be obtained from Eq. (1) by making the following replacements: $F_i^+ \rightarrow F_i^-$, $G_i^+ \rightarrow G_i^-$, $\gamma_5 \rightarrow 1$, $1 \rightarrow \gamma_5$, and $m_+ \rightarrow m_-$, where m_- is the mass of the $H_c(\frac{3}{2}^-)$ baryon.

To calculate the form factors responsible for the $H_b(\frac{1}{2}^+) \rightarrow H_c(\frac{3}{2}^-)$ transitions, we start with the following vacuum to H_b baryon correlation function.

$$\Pi_{\mu\nu}(p, q) = i \int d^4x e^{i p' x} \langle 0 | T \{ \eta_\mu(x) j_\nu(0) \} | H_b(p) \rangle. \quad (2)$$

Here η_μ is the interpolating current of the final heavy H_c baryon and $j_\nu(0) = \bar{c}\gamma_\nu(1 - \gamma_5)b$ is the current describing the $b \rightarrow c$ transition.

The interpolating current for the heavy H_c baryons is chosen in the following form [31]

$$\eta_\mu = e^{abc} \left[\partial_\alpha \partial_\beta \left(q_1^{aT} C \gamma_5 q_2^b \right) \right] \Gamma_{\alpha\beta\mu} c^c, \quad (3)$$

where

$$\Gamma_{\alpha\beta\mu} = \left(g_{\mu\alpha} g_{\beta\rho} + g_{\alpha\rho} g_{\beta\mu} - \frac{1}{2} g_{\alpha\beta} g_{\mu\rho} \right) \gamma^\rho \gamma_5,$$

a , b , and c are the color indices, and C is the charge conjugation operator.

The reason for choosing the current in this form is as follows: In this form, the relative angular momentum of the diquark is $L_\rho = 0$, i.e., it is in S-wave. On the other hand, the angular momentum between the light diquark and heavy quark is equal to $L_\lambda = 2$, which is achieved by applying two consecutive derivatives.

It should be noted that the interpolating current $\eta_\mu(x)$ couples not only with $J^P = \frac{3}{2}^+$ state but also to the heavy baryon with negative parity $J^P = \frac{3}{2}^-$. Hence, the hadronic part of the correlation function is modified by the contribution of the negative parity resonance.

We proceed with our analysis by calculating the correlation function from the phenomenological (hadronic) side. At the hadronic level, the correlation function is obtained by sandwiching the currents between hadronic states,

$$\begin{aligned} \Pi_{\mu\nu} &= \frac{1}{m_+^2 - p'^2} \langle 0 | \eta_\mu | H_c^+ \rangle \langle H_c^+ | \bar{c}\gamma_\nu(1 - \gamma_5)b | H_b \rangle, \\ &+ \frac{1}{m_-^2 - p'^2} \langle 0 | \eta_\mu | H_c^- \rangle \langle H_c^- | \bar{c}\gamma_\nu(1 - \gamma_5)b | H_b(p) \rangle + \dots \end{aligned} \quad (4)$$

where dots represent the contributions of excited states and continuum, $H_c^{+(-)}$ is positive (negative) parity heavy baryon. The matrix elements $\langle 0 | \eta_\mu | H_c^+ \rangle$ and $\langle 0 | \eta_\mu | H_c^- \rangle$ are defined as

$$\begin{aligned} \langle 0 | \eta_\mu | H_c^+ \rangle &= \lambda_+ u_\mu(p'), \\ \langle 0 | \eta_\mu | H_c^- \rangle &= \lambda_- \gamma_5 u_\mu(p'). \end{aligned} \quad (5)$$

Using Eqs. (4) and (5) and performing summation over spins of Rarita-Schwinger spinors using

$$\begin{aligned} & \sum u_\mu(p', s) \bar{u}_\beta(p') \\ &= -(p' + m) \left[g_{\mu\beta} - \frac{1}{3} \gamma_\mu \gamma_\beta - \frac{2}{3} \frac{p'_\mu p'_\beta}{m^2} + \frac{1}{3} \frac{p'_\mu \gamma_\beta - p'_\beta \gamma_\mu}{m} \right], \end{aligned} \quad (6)$$

one can calculate the hadronic part of the correlation function.

We would like to make the following preliminary remarks before proceeding with further calculations.

- a) The interpolating current of the spin $\frac{3}{2}$ baryon has nonzero overlap not only with $J = \frac{3}{2}$ state, but also with $J^P = \frac{1}{2}$ baryon. Indeed,

$$\langle 0 | \eta_\mu | \frac{1}{2}(p') \rangle \sim (\gamma_\mu - \frac{4p'_\mu}{m}) u(p', s).$$

It follows from this expression that the Lorentz structures γ_μ or p'_μ contain contributions of spin- $\frac{1}{2}$ baryons. Based on Eq. (6), we can infer that the structure $g_{\mu\beta}$ solely contains spin-3/2 baryon contributions, excluding any spin-1/2 baryon contributions.

- b) From Eqs. (5) and (6), we observe that the hadronic part of the correlation function contains many Lorentz structures. However, not all these structures are independent.

To obtain the independent structures, a specific order of Dirac matrices are needed to be specified. In the present work, we choose $\gamma_\mu \not{q} \gamma_\nu$.

Taking these remarks into account, we get the following results for the correlation function from the hadronic side.

$$\begin{aligned} \Pi_{\mu\nu} &= \frac{\lambda_+}{m_+^2 - p'^2} (p' + m_+) \left\{ \frac{p_\mu}{m_1} \left(\gamma_\nu F_1^+ + \frac{p_\nu}{m_1} F_2^+ + \frac{p'_\nu}{m_+} F_3^+ \right) + g_{\mu\nu} F_4^+ \right\} \gamma_5 \\ & - \left[\frac{p_\mu}{m_1} \left(\gamma_\nu G_1^+ + \frac{p_\nu}{m_1} G_2^+ + \frac{p'_\nu}{m_+} G_3^+ \right) + g_{\mu\nu} G_4^+ \right] \gamma_5 u(p) \\ & + \frac{\lambda_- \gamma_5}{m_-^2 - p'^2} (p' + m_-) \left\{ \left[\frac{p_\mu}{m_1} \left(\gamma_\nu F_1^- + \frac{p_\nu}{m_1} F_2^- + \frac{p'_\nu}{m_-} F_3^- \right) + g_{\mu\nu} F_4^- \right] \right. \\ & \left. - \left[\frac{p_\mu}{m_1} \left(\gamma_\nu G_1^- + \frac{p_\nu}{m_1} G_2^- + \frac{p'_\nu}{m_-} G_3^- \right) + g_{\mu\nu} G_4^- \right] \right\} \gamma_5 u(p). \end{aligned} \quad (7)$$

Applying the Dirac equation and replacing the four-momentum of H_b baryon with $p_\mu \rightarrow mv_\mu$ in Eq. (7), where v_μ is its velocity, the above equation takes the following form,

$$\begin{aligned} \Pi_{\mu\nu} &= \frac{\lambda_+}{m_+^2 - p'^2} \left\{ v_\mu \left[F_1^+ \left(2m_1 v_\nu + (m_1 + m_+) \gamma_\nu - \not{q} \gamma_\nu \right) \gamma_5 \right. \right. \\ & \left. \left. + F_2^+ v_\nu \left[(m_+ - m_1) - \not{q} \right] \gamma_5 \right. \right. \\ & \left. \left. + F_3^+ \frac{(m_1 v_\nu - q_\nu)}{m_+} \left[-\not{q} + (m_+ - m_1) \right] \gamma_5 \right. \right. \\ & \left. \left. + F_4 g_{\mu\nu} (-m_1 + m_+ - \not{q}) \gamma_5 \right. \right. \\ & \left. \left. - v_\mu \left[G_1^+ \left(2m_1 v_\nu + (m_+ - m_1) \gamma_\nu - \not{q} \gamma_\nu \right) + G_2^+ v_\nu \left((m_1 + m_+) - \not{q} \right) \right. \right. \right. \\ & \left. \left. + G_3^+ \frac{m_1 v_\nu - q_\nu}{m_+} \left((m_+ + m_1) - \not{q} \right) - G_4^+ g_{\mu\nu} (m_+ + m_1 - \not{q}) \right] \right\} u(p) \\ & + \left(\lambda_+ \rightarrow \lambda_-, m_+ \rightarrow -m_-, \right. \\ & \left. F_1^+ \rightarrow F_1^-, F_2^+ \rightarrow -F_2^-, F_3^+ \rightarrow -F_3^-, F_4^+ \rightarrow -F_4^-, \right. \\ & \left. G_1^+ \rightarrow G_1^-, G_2^+ \rightarrow G_2^-, G_3^+ \rightarrow G_3^-, G_4^+ \rightarrow G_4^- \right). \end{aligned} \quad (8)$$

In the present study, we analyze the semileptonic decays of positive parity spin-1/2 H_b baryon to spin-3/2 baryon with negative parity H_c^- . Since this transition is described by the form factors $F_i^-(q^2)$ and $G_i^-(q^2)$, the contribution of the form factors $F_i^+(q^2)$ and $G_i^+(q^2)$ should be eliminated. For this goal, the combinations of the sum rules obtained from

the different Lorentz structures should be considered. The method of eliminating the unwanted pollution by considering the linear combinations of sum rules obtained from different Lorentz structures was proposed in [32].

Having obtained the correlation function from the hadronic side, let us turn our attention to the calculation of it given in Eq. (2) in terms of quarks and gluons using the operator product expansion. After applying Wick theorem for the correlation function, we get

$$\Pi_{\mu\nu} = i \int d^4x e^{ip'x} e^{abc} (C\gamma_5)_{\phi\eta} (\Gamma_{\alpha\beta\mu})_{\rho\gamma} [\gamma_\nu(1-\gamma_5)]_{h\xi} S_{\gamma h}(x) \times \partial_\alpha \partial_\beta \left(\langle 0 | q_{1\phi}^a(x) q_{2\eta}^b(x) b_\xi^c(0) | H_b(p) \rangle \right), \quad (9)$$

where $S(x)$ is the c -quark propagator. The matrix element, $\epsilon^{abc} \langle 0 | q_{1\phi}^a(x) q_{2\eta}^b(0) b_\xi^c(0) | H_b(p) \rangle$ must be determined to calculate the theoretical part of the correlation function from the QCD side. This matrix element is expressed in terms of the H_b baryon distribution amplitudes (DAs) whose explicit forms are given in [33–35]. When the polarization vector is parallel to the light cone plane, the matrix element mentioned above is parametrized in terms of the four DAs,

$$\epsilon^{abc} \langle 0 | s_\alpha^a(t_1) q_\beta^b(t_2) b_\sigma^c(0) | H_b(v) \rangle = \sum_{i=1}^4 \Lambda_i (\Gamma_i)_{\beta\alpha} u(v)_\sigma \quad (10)$$

where

$$\begin{aligned} \Lambda_1 &= \frac{1}{8} v_+ f^{(1)} \psi_2, & \Gamma_1 &= \gamma_5 C^{-1}, \\ \Lambda_2 &= \frac{1}{8} f^{(2)} \psi_3^\sigma, & \Gamma_2 &= i \sigma_{\rho\beta} n_\rho \bar{n}_\beta \gamma_5 C^{-1}, \\ \Lambda_3 &= \frac{1}{4} f^{(2)} \psi_3^{(s)}, & \Gamma_3 &= \gamma_5 C^{-1} \\ \Lambda_4 &= -\frac{1}{8v_+} f^{(1)} \psi_4, & \Gamma_4 &= \gamma_5 C^{-1} \end{aligned} \quad (11)$$

and

$$n_\mu = \frac{x_\mu}{vx}, \quad \bar{n}_\mu = 2v_\mu - n_\mu,$$

$f^{(1)}$ and $f^{(2)}$ are the decay constants and ψ_i are the DAs of H_b baryon with definite twist.

The light cone distribution amplitudes are scale-dependent functions. To obtain their scale dependency, it is convenient to go to momentum representation with the help of the Fourier transformation

$$\begin{aligned} \psi(t_1, t_2) &= \int_0^\infty d\omega_1 \int d\omega_2 e^{-i\omega_1 t_1 - i\omega_2 t_2} \psi(\omega_1, \omega_2) \\ &= \int_0^\infty d\omega d\omega \int_0^1 du e^{-i\omega(t_1 u + t_2 \bar{u})} \psi(\omega, u) \end{aligned} \quad (12)$$

In the first expression, ω_1 and ω_2 are the energies of the light quarks. In the second expression, instead of ω_1 and ω_2 , new variables ω and u , where $\omega = \omega_1 + \omega_2$ is the total energy carried by light quarks, and dimensionless variable u corresponds to the relative energy carried by light quark q_1 , have been introduced. Moreover, using the definition $t_1 = vx_i$, where t_i is the distance between i^{th} light quark and the origin along the light-cone vector n direction, for the distribution amplitudes, we get,

$$\psi(t_1, t_2) = \int_0^\infty d\omega \omega \int_0^1 du e^{-i\omega v[\bar{u}x_1 + \bar{u}x_2]} \psi(\omega, u), \quad (13)$$

when $t_1 = t_2$, we obtain,

$$\psi(t, t) = \int_0^\infty d\omega \omega \int_0^1 du e^{-i\omega vx} \psi(\omega, u) \quad (14)$$

This equation will be used in further calculations.

The DAs of H_b baryon, which we will use in further analysis, are obtained in [33] as follows:

$$\begin{aligned} \psi_2(\omega, u) &= \omega^2 u \bar{u} \sum_{n=0}^2 \frac{a_n C_n^{3/2}(2u-1)}{\epsilon_n^4 |C_n^{3/2}|^2} e^{-\omega/\epsilon_n}, \\ \psi_3(\omega, u) &= \frac{\omega}{2} \sum_{n=0}^2 \frac{a_n C_n^{1/2}(2u-1)}{\epsilon_n^3 |C_n^{1/2}|^2} e^{-\omega/\epsilon_n}, \\ \psi_4(\omega, u) &= \sum_{n=0}^2 \frac{a_n C_n^{1/2}(2u-1)}{\epsilon_n^2 |C_n^{1/2}|^2} e^{-\omega/\epsilon_n}, \end{aligned} \quad (15)$$

where the sub-index of ψ indicates the twist of the distribution amplitudes, C_n^λ is the Gegenbauer polynomials, and $|C_n^\lambda| = \int_0^1 du |C_n^\lambda(2u-1)|^2$. The parameters appearing in DAs of Ξ_b and Λ_b are presented in Table 1 for completeness.

Using Eqs. (9),(10) and (14), we get

$$\begin{aligned} \Pi_{\mu\nu} &= i \int d^4x \int du \left(\partial_\alpha \partial_\beta \int d\omega \omega e^{-i\omega vx} \right) \\ &\times \left\{ \sum \Lambda_i \text{Tr}(C\gamma_5 \Gamma_i) \Gamma_{\alpha\beta\mu} S(x) \gamma_\nu (1-\gamma_5) \right\} u(v), \end{aligned}$$

where $S(x)$ is the c -quark propagator given as,

$$S(x) = \int d^4k e^{-ikx} \frac{i(\not{k} + m_c)}{k^2 - m_c^2}.$$

Performing integrations over x and k , the expression of the correlation function from the QCD side is obtained as follows:

$$\begin{aligned} \Pi_{\mu\nu} &= \int du \int d\omega \omega^3 \frac{2f^{(2)}\psi_{3s}}{\bar{\sigma}(p^2 - s)} \left\{ 2\not{q}(1-\gamma_5)v_\mu v_\nu - \not{q}\gamma_\nu(1+\gamma_5)v_\mu \right. \\ &\left. + m_c \gamma_\nu(1+\gamma_5)v_\mu - 2m_c(1-\gamma_5)v_\mu v_\nu - \gamma_\nu(1-\gamma_5)v_\mu \frac{(q^2 + \omega m_1 - s)}{m_1} \right\}, \end{aligned} \quad (16)$$

where,

$$s(\sigma) = \frac{m_c^2 + \sigma(m_1^2 - q^2) - \sigma^2 m_1^2}{\bar{\sigma}}, \quad (17)$$

in which $\bar{\sigma} = 1 - \sigma$ and $\sigma = \frac{\omega}{m_1}$.

Equating the coefficients of the structures from theoretical and hadronic parts of the correlation function and combining the sum rules obtained for different Lorentz structures, and performing the Borel transformation over the variable $-p^2$, we get the following sum rules for the form factors F_i^- and G_i^- ,

$$\begin{aligned} F_1^- &= -\frac{e^{m_c^2/M^2}}{\lambda_-(m_- + m_+)} \left[\Pi_2^B + (m_1 + m_+) \Pi_3^B \right], \\ F_2^- &= \frac{e^{m_c^2/M^2}}{\lambda_-(m_- + m_+)} \left[\Pi_1^B + 2m_1 \Pi_3^B - (m_1 - m_+) \Pi_4^B \right], \\ G_1^- &= \frac{e^{m_c^2/M^2}}{\lambda_-(m_- + m_+)} \left[\Pi_6^B - (m_1 - m_+) \Pi_7^B \right], \\ G_2^- &= -\frac{e^{m_c^2/M^2}}{\lambda_-(m_- + m_+)} \left[\Pi_5^B + 2m_1 \Pi_7^B + (m_1 + m_+) \Pi_8^B \right], \end{aligned}$$

where Π_i are the invariant functions in the Lorentz structures that are listed in Table 2 and Π_i^B denotes the Borel transformed invariant function.

The form factors F_3^-, F_4^-, G_3^- and G_4^- are equal to zero since the corresponding Lorentz structures are absent in the theoretical part. Hence, only the form factors F_1^-, F_2^-, G_1^- and G_2^- are needed in further analysis. Note also that this result agrees with the HQET prediction in low recoil region [24]. To study the heavy hadron decay form factors at large recoil limit the soft-collinear effective can be applied [36,37].

Table 1Parameters appearing in the DAs of the form factors. In our calculations we used $A = \frac{1}{2}$.

	twist	a_0	a_1	a_2	$\epsilon_0(\text{GeV})$	$\epsilon_1(\text{GeV})$	$\epsilon_2(\text{GeV})$
Λ_b	2	1	—	$\frac{6.4(1-A)}{1.44-A}$	$\frac{2-1.4A}{0.21+0.56A}$	—	$\frac{0.32(1-A)}{0.83-A}$
	3s	1	—	$\frac{0.03(1-3A)}{-0.4-A}$	$\frac{1.6+A}{-0.87+0.65A}$	—	$\frac{0.09-0.35A}{1.41-A}$
	3a	—	1	—	—	$\frac{0.08+0.35A}{0.2+A}$	—
	4	1	—	$\frac{-0.12+0.07A}{1.34-A}$	$\frac{-0.87+0.65A}{-2+A}$	—	$\frac{-9.3+5.5A}{-30+A}$
Ξ_b	2	1	$\frac{0.71-0.25A}{1.68-A}$	$\frac{7.2-6.6A}{0.03(1-4A)}$	$\frac{2.4-1.4A}{0.35+0.56A}$	$\frac{-1.67+0.57A}{65+27A}$	$\frac{0.39-0.36A}{0.98-A}$
	3s	1	$\frac{0.1+0.04A}{0.6+A}$	$\frac{1.68-A}{0.03(1-4A)}$	$\frac{7.7-A}{1.9+A}$	$\frac{-5+A}{65+27A}$	$\frac{0.06(1-5A)}{1.54-A}$
	3a	$\frac{0.16(2-A)}{-0.3-A}$	1	$\frac{-0.17A}{0.17A}$	0.11	$\frac{160}{0.1+0.39A}$	0.33
	4	1	$\frac{0.14-0.03A}{1.16-A}$	$\frac{0.3+A}{-0.13+0.1A}$	$\frac{1.01-0.63A}{2.3-A}$	$\frac{3.92-0.82A}{2.9+A}$	$\frac{1.54-1.2A}{5.1-A}$

Table 2Invariant functions Π_i and their corresponding structures.

Π_i	Structures
$\Pi_2(\Pi_{10})$	$\gamma_5 v_\mu v_\nu (v_\mu v_\nu)$
$\Pi_3(\Pi_{11})$	$\gamma_\nu \gamma_5 v_\mu (\gamma_\nu v_\mu)$
$\Pi_4(\Pi_{12})$	$\not{q} \gamma_\nu \gamma_5 v_\mu (\not{q} \gamma_\nu v_\mu)$
$\Pi_6(\Pi_{14})$	$\not{q} \gamma_5 v_\mu v_\nu (\not{q} v_\mu v_\nu)$

The Borel transformation and continuum subtraction procedure is performed in the theoretical part with the help of the formula,

$$\int_0^\infty d\sigma \frac{\rho(\sigma)}{[(p^2 - s(\sigma))^n]} \rightarrow \int_0^{\sigma_0} d\sigma \left\{ (-1)^n \frac{e^{-s(\sigma)} I(\sigma)}{(n-1)!(M^2)^{n-1}} \right\} - \left[\frac{(-1)^{n-1}}{(n-1)!} e^{-s(\sigma)/M^2} \sum_{j=1}^{n-1} \frac{1}{(M)^{2n-j-1}} \frac{1}{s^j} \left(\frac{d}{d\sigma} \frac{1}{s^j} \right)^{j-1} I_n \Big|_{\sigma=\sigma_0} \right], \quad (18)$$

where

$$I_n = \frac{\rho(\sigma)}{\bar{\sigma}},$$

and σ_0 is the solution of the equation $s = s_{th}$,

$$\sigma_0 = \frac{(s_{th} + m_1^2 - q^2) + \sqrt{(s_{th} + m_1^2 - q^2)^2 - 4m_1^2(s_{th} - m_c^2)}}{2m_1^2},$$

in which s_{th} is the continuum threshold.

At the end of this section, we calculate the semileptonic decay widths $H_b \rightarrow H_c l \nu (l = e, \mu, \tau)$. To determine the decay width, we used the helicity amplitudes formalism.

In this formalism, the helicity amplitudes H_{λ_2, λ_w} are expressed in terms of vector and axial form factors, where $\lambda_2 = \pm 1/2, \pm 3/2$ and $\lambda_w = \pm 1, 0$ are the helicity components of the final baryon and vector meson.

The helicity amplitudes are determined as follows [38]:

$$H_{\lambda_2, \lambda_w} = \epsilon^{+\mu}(\lambda_w) \langle H_c(p', \lambda_2) | \bar{c} \gamma_\mu (1 - \gamma_5) b | H_b(p_1, \lambda_1) \rangle, \quad (19)$$

$$\begin{aligned} H_{1/2, t}^{V(A)} &= \pm \sqrt{\frac{2}{3}} \frac{Q_\pm}{q^2} \frac{Q_\pm}{2m_1 m_-} \left\{ F_4^-(G_4^-) m_1 \pm F_1^-(G_1^-) M_\pm \right. \\ &\quad \left. + \left[\frac{m_1}{m_-} F_3^-(G_3^-) + F_2^-(G_2^-) \right] \frac{m_1^2 - m_-^2 - q^2}{2m_1} + F_2^-(G_2^-) \frac{q^2}{m_1} \right\}, \\ H_{1/2, 0}^{V(A)} &= \pm \sqrt{\frac{2}{3}} \frac{Q_\pm}{q^2} \left\{ F_4^-(G_4^-) \frac{m_1^2 - m_-^2 - q^2}{2m_-} \pm F_1^-(G_1^-) \frac{Q_\pm(M_\pm)}{2m_1 m_-} \right. \\ &\quad \left. + \left[\frac{m_1}{m_-} F_3^-(G_3^-) + F_2^-(G_2^-) \right] \frac{|\vec{p}'|^2}{2m_-} \right\}, \\ H_{1/2, 1}^{V(A)} &= \sqrt{\frac{Q_\pm}{3}} \left[F_4^-(G_4^-) - F_1^-(G_1^-) \frac{Q_\pm}{m_1 m_-} \right], \\ H_{3/2, 1}^{V(A)} &= \sqrt{Q_\pm} \left[F_4^-(G_4^-) \right], \end{aligned}$$

$$\begin{aligned} H_{-\lambda_2, -\lambda_w}^V &= H_{\lambda_2, \lambda_w}^V, \\ H_{-\lambda_2, -\lambda_w}^A &= -H_{\lambda_2, \lambda_w}^A, \end{aligned} \quad (20)$$

where

$$M_\pm = m_1 \pm m_-,$$

$$Q_\pm = M_\pm^2 - q^2,$$

$$|\vec{p}'| = \frac{\lambda^{1/2}(m_1^2, m_-^2, q^2)}{2m_1},$$

$$\lambda(a, b, c) = a^2 + b^2 + c^2 - 2ab - 2ac - 2bc. \quad (21)$$

Note that, the above formula for the helicity amplitudes is derived for the general $\frac{1}{2}^+ \rightarrow \frac{3}{2}^-$ transitions. In our case, $F_3^-, F_4^-, G_3^-,$ and G_4^- are equal to zero.

Using the helicity amplitudes, we get the differential decay widths for the corresponding transitions

$$\frac{d\Gamma}{dq^2} = \frac{G^2 |V_{cb}|^2 \sqrt{Q_+ Q_-} q^2 (1 - \hat{m}_\ell^2)}{384\pi^3 m_1^3} \left[\left(1 + \frac{\hat{m}_\ell^2}{2}\right) \mathcal{H}_1 + \frac{3}{2} \hat{m}_\ell^2 \mathcal{H}_2 \right], \quad (22)$$

where

$$\mathcal{H}_1 = \sum_{\lambda_2 = \pm 1/2, \pm 3/2} \sum_{\lambda_w = \pm 1, 0} |H_{\lambda_2, \lambda_w}|^2,$$

$$\mathcal{H}_2 = \sum_{\lambda_2 = \pm 1/2} |H_{\lambda_2, t}|^2,$$

$$H_{\lambda_2, \lambda_w} = H_{\lambda_2, \lambda_w}^V - H_{\lambda_2, \lambda_w}^A,$$

$$\hat{m}_\ell^2 = \frac{m_\ell^2}{q^2}.$$

In the following section, we perform a numerical analysis of the obtained sum rules for the form factors as well as corresponding decay widths.

3. Numerical analysis

This section is devoted to the numerical analysis of the sum rules obtained in the previous section. To perform the numerical analysis, the values of input parameters, which are collected in Table 3, are needed.

It should be noted that in the numerical analysis, we neglect $\mathcal{O}(\alpha_s)$ corrections. Hence, to be consistent, we used the values of $f^{(1)}$ and $f^{(2)}$ for Λ_b baryon obtained without $\mathcal{O}(\alpha_s)$ corrections [40]. When the SU(3) symmetry violation is taken into account, we obtain $f^{(1)} = f^{(2)} = 0.026 \pm 0.001$ for the Ξ_b baryon.

In this study, we also calculated the residues $\lambda_{\Lambda_c^-}$ and $\lambda_{\Xi_c^-}$ of the negative parity spin $\frac{3}{2}^-$ baryons, respectively, whose values are presented in Table 3.

In addition to these input parameters, the sum rules involve two more additional parameters; the Borel mass, M^2 , and the continuum threshold s_{th} . The working region of s_{th} is determined by imposing the condition that the two-point sum rules predict the mass of the baryon

Table 3

Numerical values of the input parameters appearing in the sum rules of the form factors, and branching ratio calculations. For the mass of charm quark, we used the value in \overline{MS} scheme.

$m_c(\mu = m_c) = 1.27 \pm 0.02 \text{ GeV}$ [39]	$m_{\Xi_b} = 5797 \pm 0.6 \text{ MeV}$ [39]
$m_{\Lambda_b} = 5619 \pm 0.17 \text{ MeV}$ [39]	$m_{\Xi_c} = 2815 \pm 0.25 \text{ MeV}$ [39]
$m_{\Lambda_c} = 2625 \pm 0.19 \text{ MeV}$ [39]	$m_{\Xi_c} = 2645 \pm 0.2 \text{ MeV}$ [39]
$m_{\Lambda_c} = 2860 \pm 0.28 \text{ MeV}$ [39]	$f_1^{\Lambda_c} = 0.022 \pm 0.001 \text{ GeV}^3$ [40]
$f_1^{\Lambda_c} = 0.022 \pm 0.001 \text{ GeV}^3$ [40]	$f_1^{\Xi_c} = 0.026 \pm 0.001 \text{ GeV}^3$ [40]
$f_2^{\Lambda_c} = 0.022 \pm 0.001 \text{ GeV}^3$ [40]	$f_2^{\Xi_c} = 0.026 \pm 0.001 \text{ GeV}^3$ [40]
$\lambda_{\Lambda_c} = 0.050 \pm 0.005 \text{ GeV}^5$ (This work)	$\lambda_{\Xi_c} = 0.060 \pm 0.005 \text{ GeV}^5$ (This work)
$\tau_{\Lambda_b} = (1.471 \pm 0.009) \times 10^{-12} \text{ s}$ [39]	$\tau_{\Xi_b} = (1.57 \pm 0.04) \times 10^{-12} \text{ s}$ [39]
$V_{cb} = (40.8 \pm 1.4) \times 10^{-3}$ [39]	$V_{ud} = 0.973 \pm 0.004$ [39]

within an accuracy range of 5 – 10% compared to the experimental value. With this condition, we obtain the following working region for s_{th} , $10 \text{ GeV}^2 \leq s_{th} \leq 12 \text{ GeV}^2$.

The working region of M^2 is determined with the help of two requirements:

- Higher-order twist contributions should be suppressed compared to the leading twist one.
- The contributions from the continuum and higher states should constitute 40% of the total result. Our numerical analysis shows that both conditions are satisfied in the region $2.5 \text{ GeV}^2 \leq M^2 \leq 4 \text{ GeV}^2$.

After presenting the values of all input parameters and determining the working regions of M^2 and s_{th} , we can proceed with calculations of the form factors associated with the $\Xi_b \rightarrow \Lambda_c(2625)$ and $\Xi_b \rightarrow \Xi_c(2815)$ transitions.

To calculate the semileptonic decay widths $\Xi_b \rightarrow \Lambda_c(2625)\ell\nu$ and $\Xi_b \rightarrow \Xi_c(2815)\ell\nu$, we need to know the q^2 dependency of all the form factors. It is important to note that the LCSR predictions are reliable only in the region $q^2 \lesssim 6 \text{ GeV}^2$. To extend the results to the whole physical region $m_e^2 \leq q^2 \leq (m_1 - m_-)^2$, we will apply z-series parametrization for the form factors (see [41]).

$$F_i(q^2) = \frac{1}{1 - \frac{q^2}{m_{pole}^2}} \left\{ f_i(0) + \alpha[z(q^2) - z(0)] + \beta[z(q^2) - z(0)]^2 \right\}, \quad (23)$$

where

$$z(t) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}},$$

with

$$t_{\pm} = (m_1 \pm m_-)^2,$$

$$t_0 = t_+ \left(1 - \sqrt{1 - \frac{t_-}{t_+}} \right).$$

The mass of the resonances for $b \rightarrow c$ transitions are:

$$m_{pole} = \begin{cases} 6.275 \text{ GeV} & f_1, \\ 6.33 \text{ GeV} & f_2, \\ 6.706 \text{ GeV} & g_1, \\ 6.741 \text{ GeV} & g_2. \end{cases}$$

The fitting parameters, $f_i(0)$, α and β are presented in Table 4.

The errors in the form factors due to the variation of M^2 and s_{th} in their working regions, as well as the uncertainties in the input parameters, are taken into account for the obtained results. All the uncertainties are taken into account quadratically.

Using the lifetime of the H_b and the results of the form factors, one can easily calculate the corresponding branching ratios of the semileptonic $H_b \rightarrow H_c \ell \nu$ decays presented in Table 5.

Table 4

Fit parameters for the form factors of the $\Lambda_b \rightarrow \Lambda_c(2815)\ell\nu_{\ell}$ transition at $M^2 = 3 \text{ GeV}^2$, $s_0 = 10 \text{ GeV}^2$, and $\Xi_b \rightarrow \Xi_c(2625)\ell\nu_{\ell}$ transition at $M^2 = 3 \text{ GeV}^2$, $s_0 = 11 \text{ GeV}^2$.

	$\Lambda_b \rightarrow \Lambda_c$	α	β	$\Xi_b \rightarrow \Xi_c$	α	β
$f_1(0)$	-1.00 ± 0.15	4.29	16.80	-1.04 ± 0.14	5.67	7.25
F_1^-	0.37 ± 0.06	-4.38	19.30	0.38 ± 0.06	-5.04	26.37
F_2^-	-0.63 ± 0.10	0.50	32.30	-0.66 ± 0.11	1.25	29.24
G_1^-	0.37 ± 0.06	-4.70	23.41	0.38 ± 0.06	-5.38	30.87

Finally, the obtained results for the form factors enable us to evaluate the decay widths of the color-allowed two body nonleptonic decays $H_b \rightarrow H_c M$, where M corresponds to pseudoscalar π^- , or vector meson ρ^- . To calculate the decay widths of these nonleptonic decays, we need the values of the form factors at the point $q^2 = m_M^2$, where m_M is the mass of vector or pseudoscalar mesons.

The straightforward calculation leads to the following result for the nonleptonic decay width

$$\Gamma(H_b \rightarrow H_c M) = \frac{G_F^2 f_M^2 |\vec{p}'|}{32\pi m_1^2} |V_{cb} V_{uq}|^2 a_1^2 \mathcal{H}_2^2 m_M^2, \quad (24)$$

where f_M is the leptonic decay constant of the corresponding meson, N_c is the color factor, $c_1 = -0.25$, $c_2 = 1.1$ [22], and $a_1 = c_1 + \frac{c_2}{N_c}$ [42].

The results for the branching ratios of the nonleptonic $H_b \rightarrow H_c M$ decay widths are also presented in 5. For comparison, we also demonstrate the results from other approaches. We would like to note that the decay width is obtained within the naive factorization approximation and the non-factorizable contributions as well as the scale dependency are neglected. The calculations of the non-factorizable contributions have been discussed widely in the framework of different approaches. (See for example [43–47] and references therein.)

The experimental result on branching ratios is available only for the $\Lambda_b \rightarrow \Lambda_c(2625)\ell\nu_{\ell}$ decay. Our prediction of the branching ratio for this decay is quite compatible with this data.

From Table 5, we deduce that our results for the branching ratios of the semileptonic decay modes $\Lambda_b \rightarrow \Lambda_c(2625)\ell\nu_{\ell}$ and $\Xi_b \rightarrow \Xi_c(2815)\ell\nu_{\ell}$ are in good agreement with the results of the light-front approach [30]. However, they are considerably different from the results predicted within the confined covariant quark model (CCQM) [25], heavy quark spin symmetry (HQSS) [48], and constituent quark model (CQM) [16].

On the other hand, our predictions on the branching ratios of the nonleptonic decays $\Lambda_b(\Xi_b) \rightarrow \Lambda_c(\Xi_c)\pi$ are in good agreement with the findings of LFQM [22,30]. However, our predictions on the widths of the $\Lambda_b(\Xi_b) \rightarrow \Lambda_c(\Xi_c)\rho$ are approximately 2.5 times larger than those predicted by the LFQM.

Naively, one expects that the ratio,

$$R = \frac{Br[\Lambda_b(\Xi_b) \rightarrow \Lambda_c(\Xi_c)\rho]}{Br[\Lambda_b(\Xi_b) \rightarrow \Lambda_c(\Xi_c)\pi]},$$

should approximately be equal to 3 due to the three polarization states of the ρ meson. In our case, this ratio is equal to ~ 2.5 . The difference can be attributed to the mass difference of the ρ and π mesons.

Our analysis shows that the branching ratios of the semileptonic decays are slightly larger than 1%, which could be accessible in experiments planned to be conducted at LHCb in the near future. Measurement of the studied decays can provide useful information about the inner structures of $\Lambda_c(2625)$ and $\Xi_c(2815)$ baryons.

4. Summary

In the present work, we first calculate the form factors for $1/2^+ \rightarrow 3/2^-$, i.e., $\Lambda_b \rightarrow \Lambda_c(2625)$ and $\Xi_b \rightarrow \Xi_c(2815)$ transitions within the light-cone sum rules method by using the DAs of the Λ_b and Ξ_b baryons. Having obtained the form factors, we estimate the branching ratios of

Table 5

The branching ratios of the $\Lambda_b \rightarrow \Lambda_c(2625)\ell^+ \nu_\ell$, $\Xi_b \rightarrow \Xi_c(2815)\ell^+ \nu_\ell$, $\Lambda_b \rightarrow \Lambda_c(2625)\rho(\pi)$, and $\Xi_b \rightarrow \Xi_c(2815)\rho(\pi)$ decays. Here all numerical values are presented in percent (%).

Decay	This Study	Experiment [39]	LFQM [30]	CCQM [25]	HQSS [48]	CQM [16]	LFQM [22]
$\Lambda_b^0 \rightarrow \Lambda_c^+ e^- \nu_e$	1.44 ± 0.56	–	1.653 ± 0.114	0.17 ± 0.03	–	(0.88 – 1.40)	–
$\Lambda_b^0 \rightarrow \Lambda_c^+ \mu^- \nu_\mu$	1.42 ± 0.56	$1.3^{+0.6}_{-0.5}$	1.641 ± 0.113	0.17 ± 0.03	$3.5^{+1.3}_{-1.2}$	(0.88 – 1.40)	–
$\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \nu_\tau$	0.11 ± 0.04	–	0.1688 ± 0.0116	0.018 ± 0.004	$0.38^{+0.09}_{-0.08}$	(0.18 – 0.22)	–
$\Xi_b^{(0-)} \rightarrow \Xi_c^{(0-)} e^- \nu_e$	1.55 ± 0.62	–	$1.698 \pm 0.122(1.803 \pm 0.132)$	–	–	–	–
$\Xi_b^{(0-)} \rightarrow \Xi_c^{(0-)} \mu^- \nu_\mu$	1.50 ± 0.60	–	$1.685 \pm 0.121(1.789 \pm 0.131)$	–	–	–	–
$\Xi_b^{(0-)} \rightarrow \Xi_c^{(0-)} \tau^- \nu_\tau$	0.12 ± 0.048	–	$0.1758 \pm 0.0126(0.1868 \pm 0.0137)$	–	–	–	–
$\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-$	0.40 ± 0.16	–	0.310 ± 0.015	–	–	–	$(2.40^{+4.09}_{-1.82}) \times 10^{-1}$
$\Lambda_b^0 \rightarrow \Lambda_c^+ \rho^-$	1.1 ± 0.4	–	0.450 ± 0.023	–	–	–	$(4.38^{+6.78}_{-3.17}) \times 10^{-1}$
$\Xi_b^{(0-)} \rightarrow \Xi_c^{(0-)} \pi^-$	0.43 ± 0.16	–	0.310 ± 0.017	–	–	–	$(3.32^{+6.08}_{-2.85}) \times 10^{-1}$
$\Xi_b^{(0-)} \rightarrow \Xi_c^{(0-)} \rho^-$	1.1 ± 0.4	–	0.430 ± 0.025	–	–	–	$(6.10^{+9.95}_{-4.84}) \times 10^{-1}$

semileptonic $\Xi_b \rightarrow \Xi_c(2815)\ell^+ \nu_\ell$, $\Lambda_b \rightarrow \Lambda_c(2625)\ell^+ \nu_\ell$ as well as nonleptonic $\Xi_b \rightarrow \Xi_c(2815)\rho(\pi)$ and $\Lambda_b \rightarrow \Lambda_c(2625)\rho(\pi)$.

Within the sum rules accuracy, our result on the branching ratio for the semileptonic $\Lambda_b \rightarrow \Lambda_c(2625)$ decay is in good agreement with the existing experimental data. We also compared our findings with the predictions of other approaches.

Relatively large branching ratios, which follow from our calculations, indicate that, hopefully, considered semileptonic decays would be measured in future experiments to be carried out at LHCb.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

No data was used for the research described in the article.

References

- [1] LHCb Collaboration, Test of lepton universality in $b \rightarrow s\ell^+\ell^-$ decays, arXiv:2212.09152.
- [2] LHCb Collaboration, Measurement of lepton universality parameters in $B^+ \rightarrow K^+\ell^+\ell^-$ and $B^0 \rightarrow K^0\ell^+\ell^-$ decays, arXiv:2212.09153.
- [3] Belle-II Collaboration, L. Aggarwal, et al., A test of light-lepton universality in the rates of inclusive semileptonic B -meson decays at Belle II, arXiv:2301.08266.
- [4] D. Guadagnoli, P. Koppenburg, Lepton-flavor violation and lepton-flavor-universality violation in b and c decays, in: 2022 Snowmass Summer Study, vol. 7, 2022, arXiv:2207.01851.
- [5] Y.-M. Wang, Y.-B. Wei, Y.-L. Shen, C.-D. Lü, Perturbative corrections to $B \rightarrow D$ form factors in QCD, J. High Energy Phys. 06 (2017) 062, arXiv:1701.06810.
- [6] J. Gao, T. Huber, Y. Ji, C. Wang, Y.-M. Wang, Y.-B. Wei, $B \rightarrow D\ell^+\nu_\ell$ form factors beyond leading power and extraction of $|V_{cb}|$ and $R(D)$, J. High Energy Phys. 05 (2022) 024, arXiv:2112.12674.
- [7] B.-Y. Cui, Y.-K. Huang, Y.-M. Wang, X.-C. Zhao, Shedding new light on $R(D_{(s)}^{(*)})$ and $|V_{cb}|$ from semileptonic $\bar{B}_{(s)} \rightarrow D_{(s)}^{(*)}\ell^+\nu_\ell$ decays, arXiv:2301.12391.
- [8] S.A. Gottlieb, S. Tamhankar, A Lattice study of Λ_b semileptonic decay, Nucl. Phys. B, Proc. Suppl. 119 (2003) 644–646, arXiv:hep-lat/0301022.
- [9] W. Detmold, C. Lehner, S. Meinel, $\Lambda_b \rightarrow p\ell^+\nu_\ell$ and $\Lambda_b \rightarrow \Lambda_c\ell^+\nu_\ell$ form factors from lattice QCD with relativistic heavy quarks, Phys. Rev. D 92 (3) (2015) 034503, arXiv:1503.01421.
- [10] M.-Q. Huang, H.-Y. Jin, J.G. Körner, C. Liu, Note on the slope parameter of the baryonic $\Lambda_b \rightarrow \Lambda_c$ Isgur-Wise function, Phys. Lett. B 629 (2005) 27–32, arXiv:hep-ph/0502004.
- [11] Z.-X. Zhao, R.-H. Li, Y.-L. Shen, Y.-J. Shi, Y.-S. Yang, The semi-leptonic form factors of $\Lambda_b \rightarrow \Lambda_c$ and $\Xi_b \rightarrow \Xi_c$ in QCD sum rules, Eur. Phys. J. C 80 (12) (2020) 1181, arXiv:2010.07150.
- [12] K. Azizi, J.Y. Süngü, Semileptonic $\Lambda_b \rightarrow \Lambda_c\ell^+\nu_\ell$ transition in full QCD, Phys. Rev. D 97 (7) (2018) 074007, arXiv:1803.02085.
- [13] H.-H. Duan, Y.-L. Liu, M.-Q. Huang, Light-cone sum rule analysis of semileptonic decays $\Lambda_b^0 \rightarrow \Lambda_c^+\ell^-\nu_\ell$, Eur. Phys. J. C 82 (10) (2022) 951, arXiv:2204.00409.
- [14] Y. Miao, H. Deng, K.-S. Huang, J. Gao, Y.-L. Shen, $\Lambda_b \rightarrow \Lambda_c$ form factors from QCD light-cone sum rules, Chin. Phys. C 46 (11) (2022) 113107, arXiv:2206.12189.
- [15] Z.-G. Wang, Analysis of the Isgur-Wise function of the $\Lambda_b \rightarrow \Lambda_c$ transition with light-cone QCD sum rules, arXiv:0906.4206.
- [16] M. Pervin, W. Roberts, S. Capstick, Semileptonic decays of heavy Λ baryons in a quark model, Phys. Rev. C 72 (2005) 035201, arXiv:nucl-th/0503030.
- [17] D. Ebert, R.N. Faustov, V.O. Galkin, Semileptonic decays of heavy baryons in the relativistic quark model, Phys. Rev. D 73 (2006) 094002, arXiv:hep-ph/0604017.
- [18] H.-W. Ke, X.-Q. Li, Z.-T. Wei, Diquarks and $\Lambda_b \rightarrow \Lambda_c$ weak decays, Phys. Rev. D 77 (2008) 014020, arXiv:0710.1927.
- [19] R.N. Faustov, V.O. Galkin, Semileptonic decays of Λ_b baryons in the relativistic quark model, Phys. Rev. D 94 (7) (2016) 073008, arXiv:1609.00199.
- [20] T. Gutsche, M.A. Ivanov, J.G. Körner, V.E. Lyubovitskij, P. Santorelli, N. Habył, Semileptonic decay $\Lambda_b \rightarrow \Lambda_c + \tau^- + \bar{\nu}_\tau$ in the covariant confined quark model, Phys. Rev. D 91 (7) (2015) 074001, arXiv:1502.04864, Erratum: Phys. Rev. D 91 (2015) 119907.
- [21] S. Rahmani, H. Hassanabadi, J. Křifž, Nonleptonic and semileptonic $\Lambda_b \rightarrow \Lambda_c$ transitions in a potential quark model, Eur. Phys. J. C 80 (7) (2020) 636.
- [22] C.-K. Chua, Color-allowed bottom baryon to charmed baryon nonleptonic decays, Phys. Rev. D 99 (1) (2019) 014023, arXiv:1811.09265.
- [23] H.-W. Ke, N. Hao, X.-Q. Li, Revisiting $\Lambda_b \rightarrow \Lambda_c$ and $\Sigma_b \rightarrow \Sigma_c$ weak decays in the light-front quark model, Eur. Phys. J. C 79 (6) (2019) 540, arXiv:1904.05705.
- [24] C.-K. Chua, Color-allowed bottom baryon to s -wave and p -wave charmed baryon nonleptonic decays, Phys. Rev. D 100 (3) (2019) 034025, arXiv:1905.00153.
- [25] T. Gutsche, M.A. Ivanov, J.G. Körner, V.E. Lyubovitskij, P. Santorelli, C.-T. Tran, Analyzing lepton flavor universality in the decays $\Lambda_b \rightarrow \Lambda_c^{(0)}(\frac{1}{2}^+, \frac{3}{2}^-) + \ell^+ \bar{\nu}_\ell$, Phys. Rev. D 98 (5) (2018) 053003, arXiv:1807.11300.
- [26] C.-Q. Geng, C.-W. Liu, T.-H. Tsai, Nonleptonic two-body weak decays of Λ_b in modified MIT bag model, Phys. Rev. D 102 (3) (2020) 034033, arXiv:2007.09897.
- [27] Y.-S. Li, X. Liu, F.-S. Yu, Revisiting semileptonic decays of Λ_{bc} supported by baryon spectroscopy, Phys. Rev. D 104 (1) (2021) 013005, arXiv:2104.04962.
- [28] P. Guo, H.-W. Ke, X.-Q. Li, C.-D. Lü, Y.-M. Wang, Diquarks and the semileptonic decay of Λ_b in the hybrid scheme, Phys. Rev. D 75 (Mar 2007) 054017, <https://link.aps.org/doi/10.1103/PhysRevD.75.054017>.
- [29] S. Meinel, G. Rendon, $\Lambda_b \rightarrow \Lambda_c^*(2595, 2625)\ell^+\nu_\ell$ form factors from lattice QCD, Phys. Rev. D 103 (9) (2021) 094516, arXiv:2103.08775.
- [30] Y.-S. Li, X. Liu, Investigating the transition form factors of $\Lambda_b \rightarrow \Lambda_c(2625)$ and $\Xi_b \rightarrow \Xi_c(2815)$ and the corresponding weak decays with support from baryon spectroscopy, Phys. Rev. D 107 (3) (2023) 033005, arXiv:2212.00300.
- [31] Z.-G. Wang, The $\Lambda_c(2860)$, $\Lambda_c(2880)$, $\Xi_c(3055)$ and $\Xi_c(3080)$ as D-wave baryon states in QCD, Nucl. Phys. B 926 (2018) 467–490, arXiv:1705.07745.
- [32] A. Khodjamirian, C. Klein, T. Mannel, Y.M. Wang, Form factors and strong couplings of heavy baryons from QCD light-cone sum rules, J. High Energy Phys. 09 (2011) 106, arXiv:1108.2971.
- [33] A. Ali, C. Hambrock, A.Y. Parkhomenko, W. Wang, Light-cone distribution amplitudes of the ground state bottom baryons in HQET, Eur. Phys. J. C 73 (2) (2013) 2302, arXiv:1212.3280.
- [34] G. Bell, T. Feldmann, Y.-M. Wang, M.W.Y. Yip, Light-cone distribution amplitudes for heavy-quark hadrons, J. High Energy Phys. 11 (2013) 191, arXiv:1308.6114.
- [35] P. Ball, V.M. Braun, E. Gardi, Distribution amplitudes of the Λ_b baryon in QCD, Phys. Lett. B 665 (2008) 197–204, arXiv:0804.2424.
- [36] T. Mannel, Y.-M. Wang, Heavy-to-light baryonic form factors at large recoil, J. High Energy Phys. 12 (2011) 067, arXiv:1111.1849.
- [37] Y.-M. Wang, Y.-L. Shen, Perturbative corrections to $\Lambda_b \rightarrow \Lambda$ form factors from QCD light-cone sum rules, J. High Energy Phys. 02 (2016) 179, arXiv:1511.09036.
- [38] T. Gutsche, M.A. Ivanov, J.G. Körner, V.E. Lyubovitskij, V.V. Lyubushkin, P. Santorelli, Theoretical description of the decays $\Lambda_b \rightarrow \Lambda^{(0)}(\frac{1}{2}^+, \frac{3}{2}^-) + J/\psi$, Phys. Rev. D 96 (1) (2017) 013003, arXiv:1705.07299.
- [39] Particle Data Group Collaboration, R.L. Workman, et al., Review of Particle Physics, PTEP 2022 (2022) 083C01.
- [40] S. Groote, J.G. Körner, O.I. Yakovlev, QCD sum rules for heavy baryons at next-to-leading order in α_s , Phys. Rev. D 55 (1997) 3016–3026, arXiv:hep-ph/9609469.
- [41] C. Bourrely, I. Caprini, L. Lellouch, Model-independent description of $B \rightarrow \pi\ell^+\nu_\ell$ decays and a determination of $|V_{cb}|$, Phys. Rev. D 79 (2009) 013008, arXiv:0807.2722, Erratum: Phys. Rev. D 82 (2010) 099902.

- [42] Y.K. Hsiao, S.-Y. Tsai, E. Rodrigues, Direct CP violation in internal W-emission dominated baryonic B decays, *Eur. Phys. J. C* 80 (6) (2020) 565, arXiv:1909.08780.
- [43] A. Ali, G. Kramer, Y. Li, C.-D. Lu, Y.-L. Shen, W. Wang, Y.-M. Wang, Charmless non-leptonic B_c decays to PP , PV and VV final states in the pQCD approach, *Phys. Rev. D* 76 (2007) 074018, arXiv:hep-ph/0703162.
- [44] A. Ali, G. Kramer, C.-D. Lu, Experimental tests of factorization in charmless nonleptonic two-body B decays, *Phys. Rev. D* 58 (1998) 094009, arXiv:hep-ph/9804363.
- [45] Z. Rui, C.-Q. Zhang, J.-M. Li, M.-K. Jia, Investigating the color-suppressed decays $\Lambda_b \rightarrow \Lambda \psi$ in the perturbative QCD approach, *Phys. Rev. D* 106 (5) (2022) 053005, arXiv:2206.04501.
- [46] H.-Y. Cheng, Nonleptonic weak decays of bottom baryons, *Phys. Rev. D* 56 (1997) 2799–2811, arXiv:hep-ph/9612223, Erratum: *Phys. Rev. D* 99 (2019) 079901.
- [47] M.A. Ivanov, J.G. Korner, V.E. Lyubovitskij, A.G. Rusetsky, Exclusive nonleptonic bottom to charm baryon decays including nonfactorizable contributions, *Mod. Phys. Lett. A* 13 (1998) 181–192, arXiv:hep-ph/9709325.
- [48] J. Nieves, R. Pavao, S. Sakai, Λ_b decays into $\Lambda_c^+ \ell \bar{\nu}_\ell$ and $\Lambda_c^* \pi^-$ [$\Lambda_c^* = \Lambda_c(2595)$ and $\Lambda_c(2625)$] and heavy quark spin symmetry, *Eur. Phys. J. C* 79 (5) (2019) 417, arXiv:1903.11911.