

THE ADSORPTION AND DISSOCIATION OF AsH<sub>3</sub> and B<sub>2</sub>H<sub>6</sub> MOLECULES  
ON STEPPED Ge(100) SURFACE

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**THE ADSORPTION AND DISSOCIATION OF AsH<sub>3</sub> and B<sub>2</sub>H<sub>6</sub> MOLECULES  
ON STEPPED Ge(100) SURFACE**

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## ABSTRACT

### THE ADSORPTION AND DISSOCIATION OF AsH<sub>3</sub> AND B<sub>2</sub>H<sub>6</sub> MOLECULES ON STEPPED Ge(100) SURFACE

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In this work, the doping processes of the S<sub>A</sub> type stepped Ge (100) surface by arsine (AsH<sub>3</sub>) and diborane (B<sub>2</sub>H<sub>6</sub>) gas flow have been simulated separately by the possible adsorption and dissociation models. The most stable adsorption and dissociation models of AsH<sub>3</sub> and B<sub>2</sub>H<sub>6</sub> on stepped Ge(100) surface have been determined by the local minimum total energy and/or binding energy calculations based on Hartree-Fock Theory. The present calculations have shown that, the step region (both up and down terraces) of the stepped Ge (100) surface has the most attractive sites for the initial adsorption stages of the gas molecules. It has been found that the thermodynamically preferred structures in the dissociation paths of arsine and diborane are the same; AsH<sub>3</sub>, BH<sub>3</sub> (fragment of diborane), AsH<sub>2</sub> and BH<sub>2</sub> products prefer to be bounded to a single surface Ge atom, but AsH and BH prefer to be bridged between two adjacent surface Ge atoms. It has been also found that, at the first step of the adsorptions, AsH<sub>3</sub> can only dissociate to AsH<sub>2</sub>, but BH<sub>3</sub> can dissociate to both BH<sub>2</sub> and BH. This remarkable result has showed that dissociation of BH<sub>3</sub> on Ge(100) surface can be easier than AsH<sub>3</sub>'s. According to the optimization calculations, the dissociation path has started with the adsorption of AsH<sub>3</sub> (or BH<sub>3</sub>) on the electron deficient side (buckled down) of the Ge dimer bond and ended with the occupation of the empty Ge sites in the surface layers by As (or B) atom substitutionally. In the present work, the beginning of the n – (or p-) type doping of the stepped Ge(100) surface has been illustrated by the As (or B) electronic states obtained in the optical energy gap of Ge very close to HOMO (or LUMO) energy edge.

**Keywords:** Arsine ( $\text{AsH}_3$ ), Diborane ( $\text{B}_2\text{H}_6$ ), Stepped Ge(100), Adsorption, Dissociation, Hartree-Fock (HF).

## ÖZ

### AsH<sub>3</sub> VE B<sub>2</sub>H<sub>6</sub> MOLEKÜLLERİNİN BASAMAKLI Ge(100) YÜZEYİNE YAPIŞMASI VE AYRIŞMASI

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Bu çalışmada, S<sub>A</sub> tipi basamaklı Ge(100) yüzeyinin Arsine (AsH<sub>3</sub>) ve Diborane (B<sub>2</sub>H<sub>6</sub>) gaz akışıyla ayrı ayrı katkılanması, olası yapışma ve çözünme modelleriyle simule edilmiştir. AsH<sub>3</sub> ve B<sub>2</sub>H<sub>6</sub>'nın basamaklı Ge(100) yüzeyi üzerinde en kararlı yapışma ve çözünme modelleri Hartree-Fock kuramına dayalı lokal en düşük toplam enerji ve/veya bağlanma enerjisi hesaplamalarıyla belirlenmiştir. Yapılan hesaplamalar basamaklı Ge(100) yüzeyinin basamak bölgesinin (üst ve alt teraslar) gaz moleküllerinin başlangıç yapışma aşaması için en çekici bölge olduğunu göstermiştir. Arsine ve diborane'nin çözünme yolları üzerinde termodinamik olarak tercih ettikleri yapıların benzer olduğu bulunmuştur; AsH<sub>3</sub>, BH<sub>3</sub> (Diborane parçası), AsH<sub>2</sub> ve BH<sub>2</sub> çözünme ürünleri sadece bir Ge yüzey atomuna bağlanmayı tercih ederlerken, AsH ve BH komşu iki Ge yüzey atomu arasında köprü olmayı tercih etmişlerdir. Bu çalışmada ayrıca, yapışma aşamasının ilk adımında AsH<sub>3</sub>'ün sadece AsH<sub>2</sub>'ye fakat BH<sub>3</sub>'nün hem BH<sub>2</sub> hem de BH'a ayrıştığı bulunmuştur. Bu kayda değer sonuç BH<sub>3</sub>'ün Ge(100) yüzeyinde AsH<sub>3</sub>'den daha kolay çözünebileceğini göstermiştir. Optimizasyon hesaplamalarına göre, çözünme yolu AsH<sub>3</sub>'ün (veya BH<sub>3</sub>) Ge dimer bağının elektron eksik tarafına (aşağıya bükülmüş) yapışmasıyla başlamış ve yüzey tabakaları içinde Ge atomu tarafından terkedilmiş yerlerin As (veya B) atomları tarafından doldurulmasıyla sonlanmıştır. Sunulan çalışmada, basamaklı Ge(100) yüzeyinin n- (veya p-) tipi katkılanmasının başlaması Ge'un optik enerji boşluğunda HOMO (veya LUMO) enerji ucuna yakın As (veya B) elektronik durumlarının elde edilmesiyle açıklanmıştır.

**Anahtar Kelimeler:** Arsine (AsH<sub>3</sub>), Diborane (B<sub>2</sub>H<sub>6</sub>), Basamaklı Ge(100), Yapışma, Çözünme (Ayrışma), Hartree-Fock (HF).

*to my father...*

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# CHAPTER 1

## INTRODUCTION

Nowadays, Germanium (Ge) material is coming into prominence again in device technology. The recent works [1-3] have showed that its high low-field hole mobility is interesting for high-mobility nano-devices applications, while its band gap (suitable for light absorption at communication wavelengths) is attractive in modern optoelectronics for fabrication of high-quality photo-detectors [4-6]. The use of the Germanium materials (n- and p- type Ge) for the electronic devices manufacturing was started at the beginning of the electronic age. In the 1950 and 1960s, a huge amount of data on the preparation of Ge with certain carrier type and concentration during the crystal growth and device manufacturing were reported by various research groups [7-10]. In these works, the superior low-field carrier mobility and small band gap energy were reported to be main features for Ge. Although the Ge material with high hole and electron mobility has considered to be important in device applications, the building electronic devices on germanium was left years ago because of its unstable oxides (germanium oxides), poor dielectric properties and temperature dependent electrical properties due to low energy band gap. Therefore, in the last three decades, instead of Ge, Silicon (Si) gained recognition as a dominant substrate for electronic devices especially, with its good quality oxide layer. Consequently, Si completely dominated the microelectronic industry although the first transistor was fabricated on Ge. But, according to a recent work [11], the continuous scaling into nanometer region of the Complementary Metal Oxide Semiconductor (CMOS) technology (for n- and p- type MOS transistors) brings silicon to its limits. Hence, in the next few years, it will no longer be possible to follow Moore's law (describes a long-term trend in the history of computing hardware, in which the number of transistors per square inch on an integrated circuit

has doubled approximately every two years) with silicon devices. For this reason, the investigations on new materials and innovative device design have been restarted. Along these lines there is a renewed interest in Ge as a possible candidate to replace silicon in a future integrated devices technology because its appealing properties like higher carrier mobility [12]. The Ge electronic devices could be faster than Si ones. On the other hand, the heterostructures consisting of alternate Ge and Si layers grown on Si were recognized to be a new class of materials in the last decade for modulated band gap engineering [13-14]. For exploring Ge's renewed application in semiconductor devices, the previously reported fundamentals of Ge such as the preparation conditions with a certain carrier type and concentration, the carrier mobility and its dependence on the carrier concentration, knowledge on the sticking and segregation coefficients of various dopants, have all been tried to be reevaluated in the recent works [15-20] from a current point of view.

Arsenic (As) and Boron (B) are usually used n- and p- type dopants for Ge, respectively. In the doping process, B atoms have been provided with diborane ( $B_2H_6$ ) gas flow during or after the growth of Ge materials by gas- phase molecular beam epitaxy (GP-MBE) [21-22], solid-phase molecular beam epitaxy (SP-MBE) [23] or chemical vapor deposition (CVD) techniques [2, 6, 20, 24-25]. The thermally or photochemically activated  $B_2H_6$  gas molecules or their fragments first adsorb on Ge surface, then decompose to further corresponding precursors and finally reduce to B atoms by desorption of H atoms from the surface [2, 6, 20-21, 23-25]. In recent works [2, 6, 20, 25] the application of heat treatment in low pressure CVD technique has intended the doping reaction and migration of B atoms in Ge sample. In Ref. [24], plasma-enhanced CVD with the surface irradiated by a 193 nm, 50 Hz pulsating laser was performed to synthesize boron films from  $B_2H_6 + He$  gas flow at a pressure of 200Pa. In this process, plasma was employed to generate precursor radicals ( $BH_3$ ,  $BH_2$ ,  $BH$ ) for the growth while the irradiation was intended for photochemical enhancement of the surface processes such as again migration and growth reactions. In another work [21], the p-type doping was provided with Boron concentration of  $8 \times 10^{21}/cm^3$  by  $B_2H_6$  gas molecules in the temperature range of 325-600°C during the epitaxial growth of Ge(100) layers from  $Ge_2H_6$  gas flow. In the same work [21], the

exhibited temperature programmed desorption (TPD) spectra associated with dideuteride, monodeuteride and deuterium desorption from Ge surface indicated the decomposition of  $B_2H_6$  on Ge(100) surface. The growth of p-type Ge(100) surface was also reported in Ref. [22] by GP-MBE technique with B concentration of  $4 \times 10^{19}/\text{cm}^3$  in the temperature range of 300-400°C. Therefore p-type (by B atoms) doping of Ge materials have been initiated by the adsorption of  $BH_3$  precursors on the surface and ended by the deposition of B atoms depending on the rate of desorption of H atoms from the surface. In the literature, Tertiarybutylarsine (TBAs) and Arsine ( $AsH_3$ ) gas were frequently used n-type dopant source for Ge [26-28] and SiGe materials [29] in metal-organic vapor phase epitaxy (MOVPE) and CVD techniques. However, the Ge materials have been generally doped by As atoms in ion implantation method at room temperature [19] or under the heat treatment [17, 30]. In Ref. [26], the concentration of As atoms in Ge sample was limited to approximately  $1 \times 10^{19}/\text{cm}^3$  in the temperature range of 500-700°C. According to the structural works on As doped Ge surfaces [27-28], TBAs or  $AsH_3$  gas flow forms facets on Ge surfaces having different miscut directions by etching. Particularly, the faceting on Ge (955) and Ge(11 3 3) surfaces were identified by scanning tunneling microscopy (STM) images when the samples were annealed under  $AsH_3$  partial pressure of 1.2 torr at 560°C for 20 min exposure time [27]. The etching and faceting were determined to be removed on Ge surfaces by reducing the temperature, TBAs (or  $AsH_3$ ) partial pressure and total TBAs (or  $AsH_3$ ) exposure time [27]. The different faceting structures due to different annealing temperatures were also identified on As-terminated vicinal Ge(100) surface by STM, X-ray photoemission spectroscopy (XPS) and low energy electron diffraction (LEED) measurements [28].

In the literature, the morphology of Ge surfaces has been also investigated to determine the different surface structures effective on the adsorption of dopant precursors. Especially, equilibrium surfaces of vicinal Ge (100) have been studied in detailed experimentally [31-38]. In the literature, the structure of Ge(100) surface is reported to be very similar to Si(100). The surface atoms on both Si(100) and Ge(100) dimerize resulting in (2x1) reconstruction [31-46]. The dimerization of the surface atoms first proposed by Schlier et al [47] for Si(100) and Ge(100) surfaces

was first imaged on Si(100) surface in real space by STM [39-40]. The dimerization of the surface atoms is derived by the reduction of surface energy due to the reduction in the number of dangling bonds from two to one for each surface atom. In STM images of Si(100) [39-40] both buckled (asymmetric) and non-buckled (symmetric) dimers were determined. While the symmetric dimer bonds are in the plane of the surface, asymmetric dimer bonds make an angle with the surface. In time averaged STM images of Ge(100) and Si(100) [33-34, 43-44] all the dimer bonds were determined to be buckled (asymmetric) with a length of  $\sim 2.45 \text{ \AA}$  [36]. According to analysis given in these works [33-34, 43-44] the buckled dimers had flip flop motion and the symmetric appearing dimers are imaged as a result of a time average of the two configurations (up and down) of buckled dimers. The tilt angle of the parallel dimer bonds on Ge(100) surface are associated with the displacement of electron density from buckled down to buckled up Ge atom. The tilt angle of the asymmetric dimers out of the surface plane is  $\sim 14^\circ$  [36]. The surface dimers of Si(100) and Ge(100) were also proposed to be buckled by Chadi [48]. In this work [48], the total energy calculations of the dimerized surface without imposing any symmetry constraints have indicated that the surface dimers spontaneously buckle, and the symmetric dimers are unstable.

The analysis of STM images have also illustrated that there are surface defects on Ge (100) and Si(100) as well as the asymmetric dimers, such as steps, missing dimer defects, or kink atoms [31-38, 43-44, 49-50]. In Ref. [36], Zandvliet has shown that STM images of vicinal Ge(100) can provide quantitative estimates for energetic parameters, such as the step free energy, the kink creation energy, the step-step interaction energies, and the energy of the facet. Because of the high coordination around the step edge the sites of the atomic steps are dominant to initiate the adsorption, chemical reaction, and catalysis. In light of the high resolution scanning tunneling microscopy (STM) [31-32, 36, 49-50], LEED [35-38], ultraviolet photoemission spectroscopy (UPS) [35, 37], and XPS [35-37] measurements, the main structure of vicinal Ge(100) surfaces are terraces (step up and down) formed by asymmetrically dimerized Ge surface atoms either in (1x2) or (2x1) domains. Two types of stepped structures,  $S_A$  and  $S_B$ , have been observed on vicinal Ge(100) surfaces for the small miscut angles towards the [110] direction [31-32, 35-36, 37-

38]. However, for the large miscut angles, the stepped structure was determined to be  $D_B$  (or  $D_A$ ) type [35-38] with a double atomic height at the step edge. These most probable types of steps were first modeled and labeled by Chadi [51] for vicinal Si(100) surfaces. According to the definition of  $D_B$  (or  $D_A$ ) type steps [51] dimer bonds on both upper and lower terraces are parallel (or perpendicular) to the step edge. In the case of the  $S_A$  (or  $S_B$ ) type step edges, the dimer rows of the upper and lower terraces are parallel (or perpendicular) and perpendicular (or parallel) respectively, to step edge direction. Since the kink formation energy was reported to be significantly lower in  $S_B$  steps than in  $S_A$ ,  $S_B$  steps contain many more thermally excited kinks than in  $S_A$  [52]. In Ref. [31], the STM images of vicinal Ge(100) surface were explained by both rebonded and nonbonded  $S_B$  step edges. But the STM images of the same system were explained by only bonded  $S_B$  step edges in Ref. [32]. The  $D_B$  (or  $D_A$ ) type steps were first observed on STM images of vicinal Ge(100) and Si(100) surfaces by Wierenga et al [49]. The coexistence of  $S_B$  (or  $S_A$ ) and  $D_B$  (or  $D_A$ ) type steps on Ge(100) and Si(100) surfaces were reported in Ref. [50] for a range of miscut angle. The formation of steps has been reinvestigated by spot profile analysis of LEED (SPA-LEED), UPS, and XPS measurements in Ref. [35] for vicinal Ge(100) samples having miscut angles of  $2.7^\circ$  and  $5.4^\circ$ . Tegenkamp et al [35] have reported that the vicinal Ge(100) surface with miscut angle of  $2.7^\circ$  have mainly terraces which are separated by steps of single atomic height ( $S_A$  or  $S_B$ ). The average upper and lower terrace sizes and the monatomic step height of the sample were determined to be 29.9, 14.9 and  $1.40 \text{ \AA}$ , respectively, by diffraction analysis [35, 38]. According to the qualitative results of SPA-LEED, the terraces which are separated by double atomic height ( $D_A$  or  $D_B$ ) were determined to be also present on the same sample with a small fraction ( $\sim 1\%$ ). The fraction of double steps were found to be increased ( $\sim 50\%$ ) when the miscut angle of vicinal Ge(100) was taken to be  $5.4^\circ$  [35]. A recent work [37] has indicated that the double steps can be induced on vicinal Ge(100) surfaces by Si adsorption under an appropriate kinetic growth conditions. All these works [31-36, 38, 43-44] have indicated that the critical value of the miscut angle is  $\sim 6^\circ$  to have  $D_A$  or  $D_B$  types steps on Ge(100) surface. The corresponding critical value of the miscut angle is  $4^\circ$  for Si(100) surface.

Although a considerable experimental and a few theoretical efforts have been devoted to understand the kinematics of stepped Ge(100) surfaces, there isn't any experimental or theoretical work investigating the decomposition stages of AsH<sub>3</sub> and B<sub>2</sub>H<sub>6</sub> in the n- and p- type doping processes of stepped Ge(100). This work aims to compensate the lack of the literature by presenting a systematic theoretical study about the possible adsorption and dissociation models of AsH<sub>3</sub> and B<sub>2</sub>H<sub>6</sub> on stepped Ge(100) surfaces. In the present work, the most probable dissociation paths for AsH<sub>3</sub>, and B<sub>2</sub>H<sub>6</sub> on stepped Ge(100) surfaces have been determined by the local minimal energy calculations based on Hartree-Fock theory. The binding energy of the fragments (AsH<sub>3</sub>, AsH<sub>2</sub>, AsH, As, and BH<sub>3</sub>, BH<sub>2</sub>, BH, B) has been also calculated in the adsorption and decomposition models of arsine and diborane gas molecules by

$$E_{\text{binding}} = E_{\text{model}} - E_{\text{surface}} - E_{\text{fragment}} \quad (1.1)$$

Here,  $E_{\text{model}}$ ,  $E_{\text{surface}}$ , and  $E_{\text{fragment}}$  are the total energies of the adsorption (or dissociation) models, stepped Ge(100) surface with necessary dangling bonds, and the fragment molecules (or atoms), respectively. In the present work, the kink free vicinal Ge(100) surface with a small miscut angle has been simulated by a cluster having (2x1) and (1x2) dimerized domains separated by kink free S<sub>A</sub> type step.

This thesis is organized as follows: In chapter II, the calculation method used in this work is explained and formulated, in chapter III, the stepped Ge(100) surface is modeled by a cluster, in Chapters IV and V the dissociation paths of AsH<sub>3</sub> and B<sub>2</sub>H<sub>6</sub> on stepped Ge(100) surfaces are examined, and finally conclusion of the whole present works is outlined in chapter VI.

## CHAPTER 2

### HARTREE-FOCK THEORY

#### 2.1 Introduction

In the present work, the total energy of the cluster models involving the decomposition steps of  $\text{AsH}_3$  and  $\text{BH}_3$  molecules on stepped Ge(100) surface has been calculated by Hartree-Fock theory. Since the present cluster models consist of many interacting atoms (Ge, H, As (or B)) with many interacting electrons the present calculations deal with the solution of many body problem defined in Quantum mechanics.

The many-body problem is a general name for a vast category of physical problems pertaining to the properties of microscopic systems made of a large number of interacting particles. Microscopic here implies that quantum mechanics has to be used to provide an accurate description of the system. In such a quantum system, the repeated interactions between particles create quantum correlations, or entanglement. As a consequence, the wave function of the system is a complicated object holding a large amount of information, which usually makes exact and/or analytical calculations impractical. Thus, many-body theoretical physics most often relies on a set of approximations specific to the problem at hand, and ranks among the most computationally intensive fields of science. Since the present cluster models have limited the number of atoms, the present many body problem has been defined for a molecular system.

## 2.2 The Schrödinger Equation

In quantum mechanics, the Schrödinger equation describes the wavefunction of a particle:

$$\left\{-\frac{\hbar^2}{8\pi^2m}\nabla^2 + V\right\}\Psi(\vec{r}, t) = \frac{i\hbar}{2\pi} \frac{\partial\Psi(\vec{r}, t)}{\partial t} \quad (2.1)$$

In this equation,  $\Psi(\vec{r}, t)$  is the wave function,  $m$  is the mass of the particle,  $\hbar$  is Planck's constant, and  $V$  is the potential field in which the particle is moving. The energy of the particle can be obtained by solving the Eq. 2.1 for  $\Psi$ , subject to the appropriate boundary conditions. If  $V$  is not a function of time, the Schrödinger equation can be simplified by separation of variables mathematical technique. In this technique the wave function is written as the product of a spatial function and a time function:

$$\Psi(\vec{r}, t) = \psi(\vec{r})\tau(t) \quad (2.2)$$

The substitution of these new functions into Eq. 2.1 gives two equations, one of which depends only the position of the particle and the other of which is a function of time only. Since the potential field,  $V(\vec{r})$ , is considered to be time independent, the problem is entirely the solution of the time independent Schrödinger equation:

$$H\psi(\vec{r}) = E\psi(\vec{r}) \quad (2.3)$$

Where  $E$  is the energy of the particle, and  $H$  is the Hamiltonian operator, equal to:

$$H = \frac{-\hbar^2}{8\pi^2m}\nabla^2 + V(\vec{r}) \quad (2.4)$$

Eq. (2.3) is an eigen value equation, eigen values are the energies corresponding to the different stationary states of the particle.

### 2.3 The molecular Hamiltonian

The Schrödinger equation for a collection of particles like a molecule is very similar with the Schrödinger equation written for a particle (Eq. (2.1)):

$$H_{\text{mol}}\Psi(\vec{r}, t) = E\Psi(\vec{r}, t) \quad (2.5)$$

In this case,  $\Psi(\vec{r}, t)$  would be a function of the coordinates of all the particles in the system as well as time. Therefore the spatial function, in time independent Schrödinger equation (Eq. 2.3), is a function of the positions of the electrons,  $\vec{r}$ , and the nuclei,  $\vec{R}$ , within the molecule. The position of a particular electron or nucleus is described below by  $\vec{r}_i$  or  $\vec{R}_A$ , respectively. The molecular Hamiltonian,  $H_{\text{mol}}$ , is made up of kinetic and potential energy:

$$H_{\text{mol}} = T + V \quad (2.6)$$

The kinetic energy operator (T) is a summation of  $\nabla^2$  over all the particles in the molecule:

$$T = -\frac{\hbar^2}{8\pi^2} \sum_k \frac{1}{m_k} \left( \frac{\partial^2}{\partial x_k^2} + \frac{\partial^2}{\partial y_k^2} + \frac{\partial^2}{\partial z_k^2} \right) \quad (2.7)$$

or

$$T = -\frac{\hbar^2}{8\pi^2} \sum_k \frac{1}{m_k} \nabla_k^2(x, y, z) \quad (2.8)$$

The potential energy component is the Coulomb repulsion between each pair of charged entities:

$$V = \frac{1}{4\pi\epsilon_0} \sum_j \sum_{k < j} \frac{e_j e_k}{\Delta \vec{r}_{jk}} \quad (2.9)$$

where  $\Delta \vec{r}_{jk}$  is the distance between the two particles, and  $e_j$  and  $e_k$  are the charges on particles  $j$  and  $k$ , respectively. For an electron, the charge is  $-e$ , for a nucleus the charge is  $Ze$ , where  $Z$  is the atomic number for that atom. Thus for a molecule with

N electrons and M nuclei, the  $H_{\text{mol}}$  is written explicitly in atomic unit of length

$$(a_0 = \frac{h^2}{4\pi^2 m_e e^2}):$$

$$H_{\text{mol}} = -\frac{1}{2} \sum_{i=1}^N \nabla_i^2 - \sum_{A=1}^M \frac{1}{2M_A} \nabla_A^2 - \sum_{i=1}^N \sum_{A=1}^M \frac{Z_A}{\Delta \vec{r}_{iA}} + \sum_{i=1}^N \sum_{j>i}^N \frac{1}{\Delta \vec{r}_{ij}} + \sum_{A=1}^M \sum_{B>A}^M \frac{Z_A Z_B}{\Delta \vec{R}_{AB}} \quad (2.10)$$

Here,  $M_A$  is the ratio of the mass of the nucleus A to the mass of an electron and  $Z_A$  is the atomic number of nucleus A. The Laplacian operators,  $\nabla_i^2$  and  $\nabla_A^2$  involve the differentiation with respect to the coordinates of the  $i^{\text{th}}$  electrons and  $A^{\text{th}}$  nucleus. The first and second terms in Eq. (2.10) are the total kinetic energies of the electrons and nuclei. The fourth and fifth terms of Eq. (2.10) define the total electron-electron and nuclei-nuclei repulsion interactions. The third term in the same equation defines the Coulomb attraction between the electrons and nuclei. The above Hamiltonian (Eq. (2.10)) gives the energies in Hartrees and the lengths in Bohrs.

An exact solution to the Schrödinger equation (Eq. (2.5)) is not possible for any molecular systems. However, a number of simplifying assumptions and procedures make an approximate solution possible for a large of molecules like in the present work. Since there are no known solutions for many-electron systems, the problem is solved numerically. One of the numerical solution methods to Schrödinger equation is provided by Hartree-Fock theory. The Hartree-fock theory is formulated below using the Refs. [53-56].

## 2.4. The Hartree-Fock Theory

The Hartree-Fock method is typically used to solve the time-independent Schrödinger equation for a multi-electron atom or molecule. In Hartree-Fock approximation, the equations are solved using a nonlinear method such as iteration, which gives rise to the name “self-consistent field method”. The Hartree-Fock method makes five major simplifications in order to deal with the solution of the Schrödinger equation (Eq. (2.5)):

- The Born-Oppenheimer approximation is inherently assumed. The full molecular wave function is actually a function of the coordinates of each of the nuclei, in addition to those of the electrons.
- The relativistic effects are completely neglected.
- Each energy eigen function is assumed to be describable by a single Slater determinant, an antisymmetrized product of one-electron wave functions (i.e., orbitals).
- The variational solution is assumed to be a linear combination of a finite number of basis functions which are chosen to be orthogonal.
- The mean field approximation is implied. Effects arising from deviations from this assumption, known as electron correlation, are completely neglected for the electrons of opposite spin, but are taken into account for electrons of parallel spin.

#### 2.4.1 Born-Oppenheimer Approximation

Born-Oppenheimer (BO) Approximation is the first of several approximations used to simplify the solution of the Schrödinger equation. It is based on the observation, that the electrons are much lighter particles than the nuclei. The electron-nucleus mass ratio  $M/m_e$  amounts to 1836 for a proton and to order of  $10^4$  for typical elements such as carbon or silicon. Due to their smaller mass electrons bound in the potential of the nuclei move more rapidly than the heavy nuclei themselves and on the average follow their motion. Therefore the electron distribution within a molecular system depends on only the positions of the nuclei and not on their velocities. In BO approximation the molecular wave function,  $\psi \equiv \psi(\mathbf{r}, \mathbf{R})$ , is written as a product of a nuclear and electronic wave function:

$$\psi(\vec{\mathbf{r}}, \vec{\mathbf{R}}) = \Phi_{\text{elec}}(\vec{\mathbf{r}}, \vec{\mathbf{R}})\Phi_{\text{nuc}}(\vec{\mathbf{R}}) \quad (2.11)$$

The molecular wave function for a particular electron position  $\mathbf{r}_i$  and nuclear position  $\mathbf{R}_A$  is

$$\psi(\vec{\mathbf{r}}_i, \vec{\mathbf{R}}_A) = \Phi_{\text{elec}}(\vec{\mathbf{r}}_i, \vec{\mathbf{R}}_A)\Phi_{\text{nuc}}(\vec{\mathbf{R}}_A) \quad (2.12)$$

The above definition of the molecular wave function in BO approximation separates the nuclear and electronic motions, and consequently allows the two parts of the problem to be solved independently. In the first part of the BO approximation the electronic Schrödinger equation is solved, yielding the wave function,  $\Phi_{\text{elec}}(\vec{r}, \vec{R})$ , depending on electrons only. During this solution the nuclei are fixed in a certain configuration, very often the equilibrium configuration. Since nuclei are much heavier and move more slowly than electrons, in the electronic Hamiltonian the kinetic energies of the nuclei are neglected and repulsion between the nuclei is considered to be constant:

$$H_{\text{elec}} = -\frac{1}{2} \sum_{i=1}^N \nabla_i^2 - \sum_{i=1}^N \sum_{A=1}^M \frac{Z_A}{\Delta \vec{r}_{iA}} + \sum_{i=1}^N \sum_{j>i}^N \frac{1}{\Delta \vec{r}_{ij}} + \sum_{A=1}^M \sum_{B>A}^M \frac{Z_A Z_B}{\Delta \vec{R}_{AB}} \quad (2.13)$$

This Hamiltonian is then used in the Schrödinger equation describing the motion of the electrons in the field of fixed nuclei:

$$H_{\text{elec}} \Phi_{\text{elec}}(\vec{r}, \vec{R}) = E_{\text{elec}}(\vec{R}) \Phi_{\text{elec}}(\vec{r}, \vec{R}) \quad (2.14)$$

The solution function,  $\Phi_{\text{elec}}(\vec{r}, \vec{R})$ , in Eq. (2.14) is antisymmetric and required to be normalized. The  $E_{\text{elec}}$  resulted from Eq. (2.14) is nuclear coordinate functional and describes the potential energy surface for the molecular system.

Accordingly, in the second part of the BO approximation,  $E_{\text{elec}}$  is also used as the effective potential for the nuclear Hamiltonian:

$$H_{\text{nuc}} = T_{\text{nuc}}(\vec{R}) + E_{\text{elec}}(\vec{R}) \quad (2.15)$$

or

$$H_{\text{nuc}} = -\sum_{A=1}^M \frac{1}{2M_A} \nabla_A^2 + E_{\text{elec}}(\vec{R}) \quad (2.16)$$

This Hamiltonian is used in the Schrodinger equation for nuclear motion:

$$H_{\text{nuc}} \Phi_{\text{nuc}}(\vec{R}) = E \Phi_{\text{nuc}}(\vec{R}) \quad (2.17)$$

describing the vibrational, rotational, and translational states of the nuclei.

In the present work, the total energy values of the considered cluster models are resulted from the eq. (2.14) for fixed optimized coordinates of Ge, H, and the corresponding dopant atoms.

### 2.4.2 Molecular Orbitals

According to the third assumption considered in Hartree-Fock theory the electronic wave function  $\Phi_{\text{elec}}(\vec{r})$  in Eq. (2.14), (for fixed nuclei configuration), is Hartree product of molecular orbitals:

$$\Phi_{\text{elec}}(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N) = \varphi_1(\vec{r}_1)\varphi_2(\vec{r}_2)\dots\varphi_N(\vec{r}_N) \quad (2.18)$$

However, such a function is not satisfactory for fermions, such as electrons, because the wave function is not antisymmetric. For the two- particle case, an antisymmetric wave function can be mathematically described as follows:

$$\Phi_{\text{elec}}(\vec{r}_1, \vec{r}_2) = -\varphi_2(\vec{r}_2)\varphi_1(\vec{r}_1) \quad \text{for} \quad \Phi_{\text{elec}}(\vec{r}_1, \vec{r}_2) = \varphi_1(\vec{r}_1)\varphi_2(\vec{r}_2) \quad (2.19)$$

Since the interchanging two of the  $\vec{r}_i$ 's does not change the sign of the Eq. (2.18), the wave function is not antisymmetric. Therefore the Hartree product does not satisfy the Pauli principle. This problem can be overcome by taking a linear combination of all Hartree products.

The antisymmetric wave function for the two-particle case can be written as the linear combination of both Hartree products:

$$\Phi_{\text{elec}}(\vec{r}_1, \vec{r}_2) = \frac{1}{\sqrt{2}} \{ \varphi_1(\vec{r}_1)\varphi_2(\vec{r}_2) - \varphi_1(\vec{r}_2)\varphi_2(\vec{r}_1) \} \quad (2.20)$$

or in the Slater determinant expression

$$\Phi_{\text{elec}}(\vec{r}_1, \vec{r}_2) = \frac{1}{\sqrt{2}} \begin{vmatrix} \varphi_1(\vec{r}_1) & \varphi_2(\vec{r}_1) \\ \varphi_1(\vec{r}_2) & \varphi_2(\vec{r}_2) \end{vmatrix} \quad (2.21)$$

where the coefficient,  $\frac{1}{\sqrt{2}}$ , is the normalization factor. This wave function is antisymmetric and no longer distinguishes between fermions. Moreover, it also goes to zero if any two wave functions or two fermions are the same. This is equivalent to satisfying the Pauli Exclusion Principle.

The Slater determinant for the two-particle case is:

$$\Phi_{\text{elec}}(\vec{r}_1, \vec{r}_2) = \frac{1}{\sqrt{2}} \begin{vmatrix} \varphi_1(\vec{r}_1)\alpha(1)\varphi_1(\vec{r}_1)\beta(1) & \varphi_2(\vec{r}_1)\alpha(1)\varphi_2(\vec{r}_1)\beta(1) \\ \varphi_1(\vec{r}_2)\alpha(2)\varphi_1(\vec{r}_2)\beta(2) & \varphi_2(\vec{r}_2)\alpha(2)\varphi_2(\vec{r}_2)\beta(2) \end{vmatrix} \quad (2.22)$$

when the electron spin is taken into account. Here, two spin functions are defined as follows:

$$\alpha(\uparrow) = 1 \quad \text{spin up}, \quad \alpha(\downarrow) = 0 \quad \text{spin down}$$

$$\beta(\uparrow) = 0 \quad \text{spin down}, \quad \beta(\downarrow) = 1 \quad \text{spin up} \quad (2.23)$$

Therefore  $\alpha(I)$  is the value of  $\alpha$  for electron 1. The product of the molecular orbital,  $\varphi(\vec{r}_i)$  and a spin function  $\alpha$  (or  $\beta$ ) is defined as a spin orbital, a function of both the electron's location and its spin.

### 2.4.3 Slater determinant for a molecular system

The expression of the antisymmetric wave function (Eq. 2.21) can be generalized to n number of electrons by writing it as a Slater determinant. For an n-electron system, a closed shell wave function can be built particularly by defining n/2 molecular orbitals:

$$\Phi_{\text{elec}} = \frac{1}{\sqrt{N!}} \begin{vmatrix} \varphi_1(\bar{r}_1)\alpha(1) & \varphi_1(\bar{r}_1)\beta(1) & \varphi_2(\bar{r}_1)\alpha(1) & \varphi_2(\bar{r}_1)\beta(1)\dots & \varphi_n(\bar{r}_1)\alpha(1) & \varphi_n(\bar{r}_1)\beta(1) \\ \varphi_1(\bar{r}_2)\alpha(2) & \varphi_1(\bar{r}_2)\beta(2) & \varphi_2(\bar{r}_2)\alpha(2) & \varphi_2(\bar{r}_2)\beta(2)\dots & \varphi_n(\bar{r}_2)\alpha(2) & \varphi_n(\bar{r}_2)\beta(2) \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \varphi_1(\bar{r}_i)\alpha(i) & \varphi_1(\bar{r}_i)\beta(i) & \varphi_2(\bar{r}_i)\alpha(i) & \varphi_2(\bar{r}_i)\beta(i)\dots & \varphi_n(\bar{r}_i)\alpha(i) & \varphi_n(\bar{r}_i)\beta(i) \\ \varphi_1(\bar{r}_j)\alpha(j) & \varphi_1(\bar{r}_j)\beta(j) & \varphi_2(\bar{r}_j)\alpha(j) & \varphi_2(\bar{r}_j)\beta(j)\dots & \varphi_n(\bar{r}_j)\alpha(j) & \varphi_n(\bar{r}_j)\beta(j) \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \varphi_1(\bar{r}_n)\alpha(n) & \varphi_1(\bar{r}_n)\beta(n) & \varphi_2(\bar{r}_n)\alpha(n) & \varphi_2(\bar{r}_n)\beta(n) & \varphi_n(\bar{r}_n)\alpha(n) & \varphi_n(\bar{r}_n)\beta(n) \end{vmatrix} \quad (2.24)$$

Here, the electrons are assigned to these orbitals in pairs of opposite spin.

#### 2.4.4 Basis sets

The fourth assumption given for Hartree-fock theory involves expressing the molecular orbitals as linear combinations of a pre-defined set of one electron functions known as basis functions. Here any set of appropriately defined functions may be used. An individual molecular orbital is defined as:

$$\varphi_i = \sum_{\mu=1}^N C_{\mu i} \chi_{\mu} \quad (2.25)$$

where the coefficients  $C_{\mu i}$  are known as the molecular orbital expansion coefficients. The normalized  $\chi_1 \chi_2 \dots \chi_N$  are the basis functions. Larger number of well chosen wave functions yields more accurate approximations to the molecular orbitals. In the present work Gaussian -type atomic functions ( $e^{-\alpha r^2}$ ) provided by Gauss03 package [57] are used as basis functions.

#### 2.4.5 The variational principle

The problem has now become how to solve Eq. 2.14 for the set of molecular orbital expansion coefficients,  $C_{\mu i}$ . Hartree-Fock theory takes advantage of the variational

principle, which says that “the expectation value of the known Hamiltonian for any normalized wave function must be greater than the actual ground state energy corresponds to the exact wave function of the system”. In the present molecular hamiltonian (Eq. (2.14)), the energy  $E_{\text{elec}}(\vec{R})$  corresponds to the exact wave function,  $\Phi_{\text{elec}}(\vec{r}, \vec{R})$ . According to the variational principle since the ground state antisymmetric normalized wave function of the electronic coordinates are defined to be the linear combinations of any set of appropriate basis functions (Eq. (2.25)), the solution of the Eq. 2.14, which we will denote it  $\Xi_{\text{elec}}(\mathbf{r}, \mathbf{R})$ , gives the expectation value of the energy greater than the energy for the exact wave function,  $\Phi_{\text{elec}}$  :

$$E_{\text{var}} = \frac{\langle \Xi(\vec{r}, \vec{R}) | H_{\text{mol}} | \Xi(\vec{r}, \vec{R}) \rangle}{\langle \Xi(\vec{r}, \vec{R}) | \Xi(\vec{r}, \vec{R}) \rangle} \quad (2.26)$$

and

$$E_{\text{var}} \langle \Xi_{\text{elec}}(\vec{r}, \vec{R}) \rangle > E_{\text{elec}} \langle \Phi_{\text{elec}}(\vec{r}, \vec{R}) \rangle \quad (2.27)$$

Thus the problem solving the Eq. 2.14 becomes one of finding the set of coefficients,  $C_{\mu i}$ , that minimize the energy of the resultant wave function  $\Xi_{\text{elec}}(\mathbf{r}, \mathbf{R})$ :

$$\frac{\partial E_{\text{var}}}{\partial \Xi_i(\vec{r}_i, \vec{R})} = 0 \quad \text{or} \quad \frac{\partial E_{\text{var}}}{\partial \phi_i(\vec{r}_i, \vec{R})} = 0 \quad (2.28)$$

with the fourth assumption of the Hartree –Fock theory ( $\iint \phi_i^* \phi_j d\vec{r}_i d\vec{r}_j = \delta_{ij}$ ).

#### 2.4.6 The Roothaan-Hall Equations

The equations (2.26) and (2.28) yield the Fock equation:

$$\hat{F}\phi_i = \varepsilon_i \phi_i \quad (2.29)$$

in which the Fock operator,  $\hat{F}$ , is an effective one electron Hamiltonian for an orbital  $\phi$ . Therefore Fock operator involves one electron integrals of kinetic and nuclear-electron attraction operators:

$$-\frac{1}{2}\nabla_i^2(\vec{r}_i) - \sum_{A=1}^M \frac{Z_A}{\Delta\vec{r}_{iA}} \quad (2.30)$$

and two electron integrals of  $\frac{1}{\vec{r}_{ij}} : \hat{J} - \hat{K}$ , for which

$$\hat{J}\phi_i = \left\{ \sum_{j=1}^N \int \phi_j(\vec{r}_j) \frac{1}{\vec{r}_{ij}} \phi_j(\vec{r}_j) d\vec{r}_j \right\} \phi_i(\vec{r}_i) \quad (2.31)$$

and

$$\hat{K}\phi_i = \left\{ \sum_{j=1}^N \iint \phi_j(\vec{r}_j) \frac{1}{\vec{r}_{ij}} \phi_i(\vec{r}_i) d\vec{r}_i d\vec{r}_j \right\} \phi_j(\vec{r}_j) \quad (2.32)$$

In Eq. (2.29)  $\varepsilon_i$  is the orbital energy. Therefore, finding a many electron wave function is reduced to finding a series of one electron orbitals in Eq. (2.29).

The basis set expansion of the wave function used in Eq. (2.29) leads to the following equations describing the molecular expansion coefficients,  $C_{vi}$  derived by Roothaan and by Hall [58-59]:

$$\sum_{v=1}^N (F_{\mu v} - \varepsilon_i S_{\mu v}) C_{vi} = \vec{0} \quad \mu = 1, 2, \dots, N \quad (2.33)$$

Or

$$FC_i = \varepsilon_i SC_i \quad (2.34)$$

Here, each element in Eq. (2.34) is a matrix.  $\varepsilon$  is a diagonal matrix of orbital energies. Each term of  $\varepsilon_i$  is the one-electron orbital energy of molecular orbital  $\chi_i$ .

The matrix C in Eq. (2.34) shows a column vector of molecular orbital coefficients. The matrix S indicates the overlap between the orbitals:

$$S_{\mu v} = \int \chi_{\mu}^*(\vec{r}_i) \chi_v(\vec{r}_i) d\vec{r}_i \quad (2.35)$$

In Eq. (2.34) F is called the Fock matrix, and it represents the average effects of the field of all the electrons on each orbital:

$$F_{\mu v} = \int \chi_{\mu}^*(\vec{r}_i) \hat{F} \chi_v(\vec{r}_i) d\vec{r}_i \quad (2.36)$$

or

$$\begin{aligned}
 F_{\mu\nu} = & \int \chi_{\mu}^*(\vec{r}_i) \left( -\frac{1}{2} \nabla_i^2(\vec{r}_i) - \sum_{A=1}^M \frac{Z_A}{\Delta \vec{r}_{iA}} \right) \chi_{\nu}(\vec{r}_i) d\vec{r}_i + \sum_{j=1}^N \iint \chi_{\mu}^*(\vec{r}_i) \chi_{\mu}(\vec{r}_i) \left( \frac{1}{r_{ij}} \right) \chi_{\nu}^*(\vec{r}_j) \chi_{\nu}(\vec{r}_j) d\vec{r}_i d\vec{r}_j \\
 & - \sum_{j=1}^N \iint \chi_{\mu}^*(\vec{r}_i) \chi_{\nu}(\vec{r}_j) \left( \frac{1}{r_{ij}} \right) \chi_{\nu}^*(\vec{r}_i) \chi_{\mu}(\vec{r}_j) d\vec{r}_i d\vec{r}_j
 \end{aligned} \tag{2.37}$$

In the above equation, the first term ( $H_{ii}$ ) involves one electron integrals of kinetic and nuclear-electron attraction operators, the second and third terms ( $J_{ij}$  and  $K_{ij}$ ) define the Coulomb and exchange integrals, respectively. The diagonalization of the Fock matrix gives the energies correspond to the molecular orbitals. The energy of the of the  $i^{\text{th}}$  electron can be written as:

$$\varepsilon_i = H_{ii} + \sum_{j=1}^N (J_{ij} - K_{ij}) \tag{2.38}$$

#### 2.4.7 Solving the Roothaan-Hall Equations

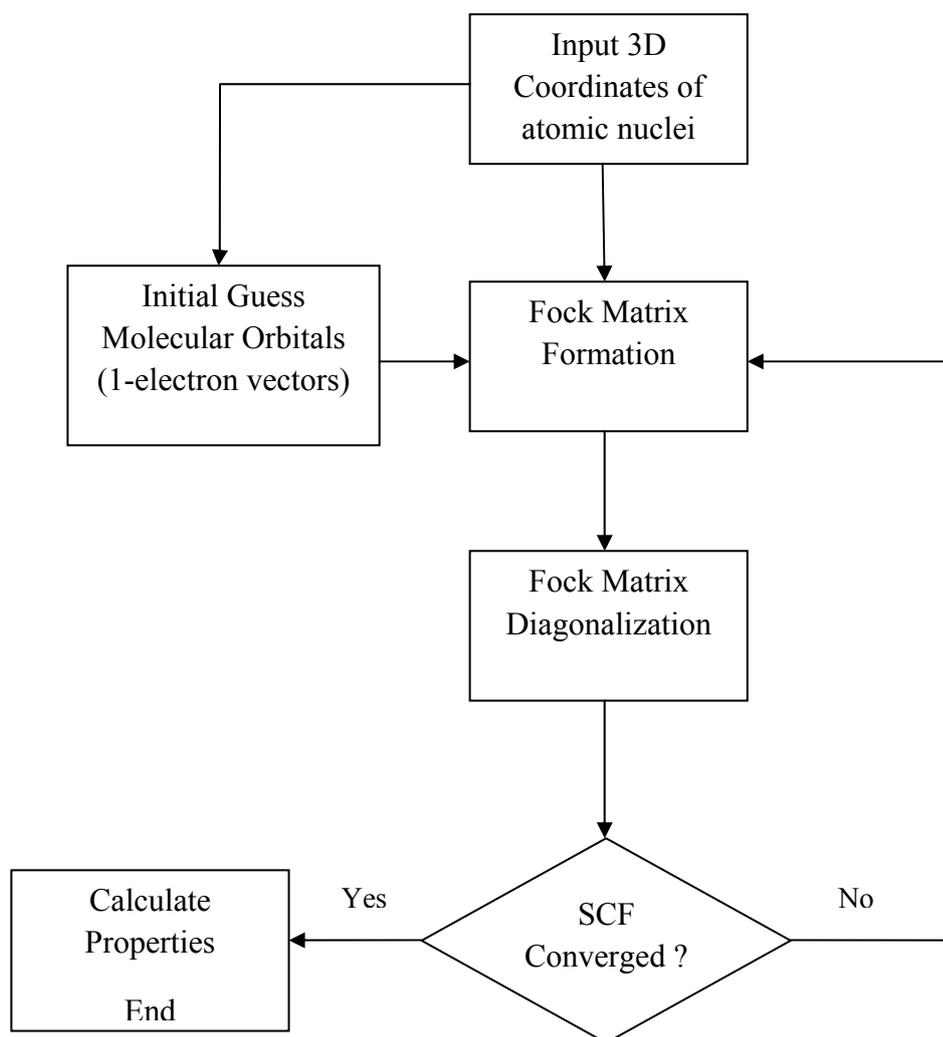
Since the the Roothaan-Hall Equations ((Eq. (2.33 or 2.34)) are not linear they must be solved iteratively. The procedure is called the Self-Consistent Field (SCF) method. At convergence, the energy is at a minimum, and the orbitals generate a field which produces the same orbitals. The solution produces a set of orbitals ( $\phi_i$ ), both occupied and unoccupied. The total number of orbitals is equal to the number of basis functions used. Under Hartree-Fock treatment, each electron sees all of the other electrons as an average distributions, there is no instantaneous electron-electron interaction included. The solution steps of the Roothaan-Hall Equations are outlined below:

1. choose a basis set ( $\chi_{\mu}$ )
2. calculate all the one ( $H_{\mu\nu}$ ) and two electron integrals ( $J_{\mu\nu}$  and  $K_{\mu\nu}$ )
3. obtain an initial guess for all the molecular orbital coefficients  $C_i$
4. use the current  $C_i$  construct a new Fock matrix ( $F$ )
5. solve  $FC_i = \varepsilon_i SC_i$  for a new set of  $C_i$

- if the new  $C_i$  are different from the old  $C_i$ , go back to step 4.

### 2.4.8 Hartree–Fock algorithm

In the self consistent field calculations of Hartree–Fock theory, the solution steps (1-6) are followed in iteration method. Iteration in computing is the repetition of a process within a computer program. The algorithmic flowchart illustrating the SCF iteration of Hartree –Fock method within Gauss03 [57] program is simply given in Fig 2.1.



**FIG. 2.1.** The algorithmic flowchart illustration of the SCF iteration of Hartree – Fock method within Gauss03 program.

At the last step of the algorithm, the ground state molecular orbital energies are obtained for the occupied and unoccupied molecular states. The energy of the highest occupied molecular orbital (HOMO) and the energy of the least unoccupied molecular orbital (LUMO) are important reference energy levels to find out the energy of the impurity states defined for a doped host molecule. Furthermore the calculated molecular orbital energies obtained at the last step of the Hartree-Fock algorithm can be used to calculate the total energy of the molecular structure:

$$E_{\text{tot}} = \sum_{i=1}^N \varepsilon_i + \sum_{A=1}^M \sum_{B>A}^M \frac{Z_A Z_B}{R_{AB}} \quad (2.39)$$

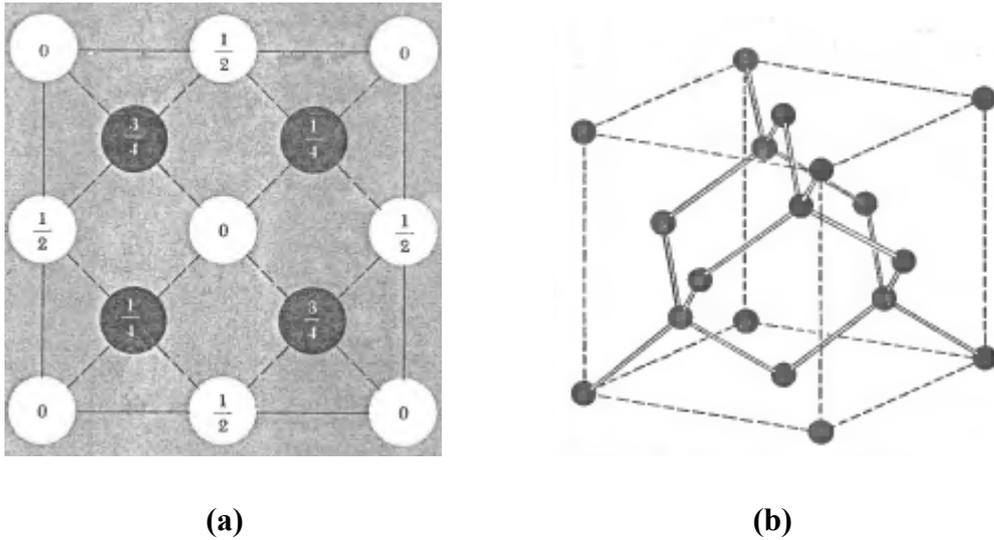
The repetition of the above self consistent iteration cycle for different positions of the atoms provides the lowest energy corresponding to the optimized geometry of the system. All the calculations outlined in this chapter are provided by Gauss03 package [57].

## CHAPTER 3

### STEPPED Ge(100) SURFACE

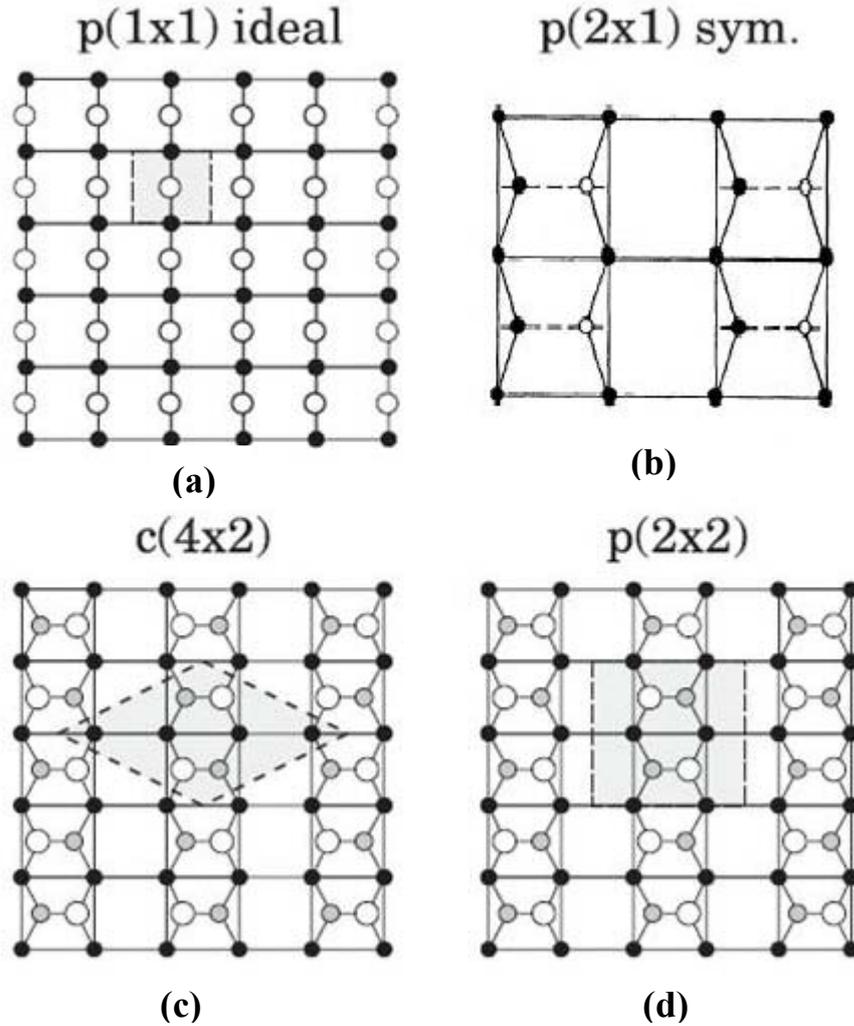
#### 3.1 Introduction

The bulk Ge crystallizes in diamond structure. The diamond structure consists of two interpenetrated fcc structures. The second fcc is displaced with respect to the first one along the main diagonal of the cubic structure by a distance of  $\frac{a\sqrt{3}}{4}$ . Here,  $a$  is the lattice constant with the value of  $5.658 \text{ \AA}$  [60] for Ge. The conventional unit cell of the Ge bulk structure is pictured in Fig. 3.1. There are two Ge atoms in the unit cell located at  $(0,0,0)$  and  $(a/4, a/4, a/4)$ . The electron configuration of Ge is  $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^2 4p^2$ . The four valence electrons on 4s and 4p orbitals are responsible to form four covalent bonds around each Ge atom. Therefore, each Ge atom is surrounded by four nearest neighbor atoms in  $\frac{a\sqrt{3}}{4}$  distance. The Ge bulk structure sliced along  $\langle 100 \rangle$  directions gives Ge(100) surfaces. The unreconstructed Ge(100) surface consists of unit cells with an area of  $\frac{a\sqrt{2}}{2} \times \frac{a\sqrt{2}}{2}$  in (1x1) dimension. There is one Ge atom in each unit cell with two uncompensated (dangling) bonds. While the two dangling bonds are extending outside of the surface, the other two bonds bond the surface Ge atoms to the next layer of the Ge(100) (1x1) surface. The top view of the Ge(100) (1x1) surface is pictured in Fig. 3.2(a) for two sublayers. In Fig. 3.2(a), the open and closed circles define the position of the first and second sublayer Ge atoms, respectively.



**FIG. 3.1.** The top (a) and side (b) view of the conventional unit cell of the Ge bulk structure [60].

The studies in the past have clearly showed that Ge(100) surface has both strong short range and energetically weaker moderate-range reconstructions as well as Si(100). At room temperature, the short range interaction forces the nearest neighbor atoms on Ge(100) (1x1) surface to form rows of dimers in a new Ge(100) (2x1) structure. As it is mentioned in the first chapter, the reconstruction reduces the surface energy by eliminating half of Ge's dangling bonds. The necessary energy in reconstruction was reported to be quite strong ( $\geq 1$  eV) [41]. The rows of dimers with (2x1) periodicity were observed clearly on Ge(100) surface by LEED [35, 37-38, 41] and STM [33-34, 39-40, 43-44] images. According to the results of these works [33-35, 37-41], one Ge atom is pushed up and the other is pushed down on the same dimer bond, so that the dimer is buckled or asymmetric. Therefore the dimers are tilted along  $\langle 110 \rangle$  direction and form dimer row structure on Ge(100) surface. The line up of dimer bonds is associated with the displacement of electron density from buckled down to buckled up atom. The structure of dimer rows on Ge(100) (2x1) surface were also proposed theoretically [48] and the asymmetric dimers being more stable than the symmetric ones was found by total energy calculations. In another theoretical work [61], the energetic stability of asymmetric dimers has been examined by Ising model. Because of the electron displacement from buckled down



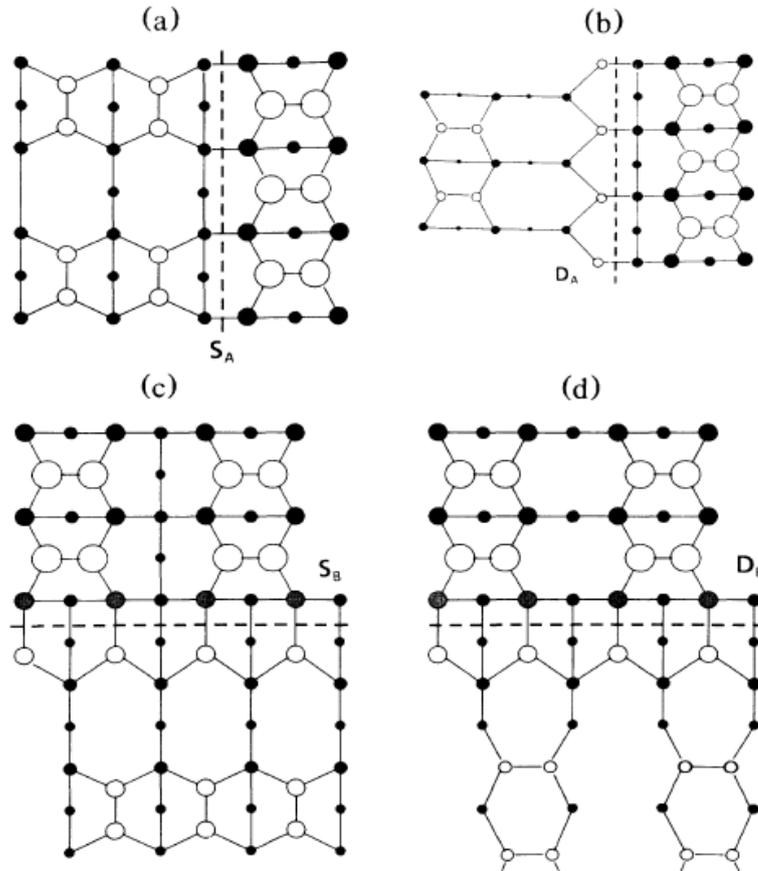
**FIG. 3.2.** Ge (100) surface with (a) unreconstructed (1x1) unit cell, b) p(2x1) dimer reconstruction, (c) c(4x2) dimer reconstruction, (d) p(2x2) dimer reconstruction.

to buckled up, the asymmetric dimers are treated as interacting spins in this model. Therefore all the spins defined for the structure of asymmetric dimers on Ge(100) (2x1) are totally aligned like in ferromagnetic case. The top view of the Ge(100) (2x1) surface is pictured in Fig. 3.2(b) with two sublayers. In Fig. 3.2(b), the open and closed circles define the position of the first and second sublayer Ge atoms, respectively. The asymmetric dimer bonds on Ge(100) surface make it possible to form other larger surface reconstructions such as p(2x2), c(4x2), p(4x1) [48]. They are energetically weaker moderate-range reconstructions. Among these reconstructions, c(4x2) and p(2x2) were found to be the lowest energy reconstructions with their nearly degenerate energies by ab-initio calculations [61, 62]. According to LEED [41, 63] and STM [34, 64, 65] images, (2x1) structure of

Ge(100) surface changes to  $c(4 \times 2)$  and  $p(2 \times 2)$  periodicities at temperatures lower than 250 K. In  $c(4 \times 2)$  reconstruction, the bonds along the same and different rows are arranged in the order of “zig-zag”. Therefore the dimers on the same and different rows are either buckled up or down at every two dimers. In  $p(2 \times 2)$  reconstructions, while the asymmetric dimers are in zig-zag type order from one row to other, they are all either in buckled up or down order along the same row. The stability of the asymmetric dimers for  $c(4 \times 2)$  and  $p(2 \times 2)$  reconstructions was studied within Ising model [36, 61] by treating the dimers as spins like in antiferromagnetic case. The top view of the  $c(4 \times 2)$  and  $p(2 \times 2)$  reconstructions on Ge(100) surface are pictured in Fig. 3.2(c) and (d). In these figures, the open and shaded circles show the positions of the buckled up and buckled down first layer Ge atoms on the same dimer bonds, respectively. The closed circles in the same figures define the positions of the second layer Ge atoms.

### 3.2 Stepped Ge(100) surface

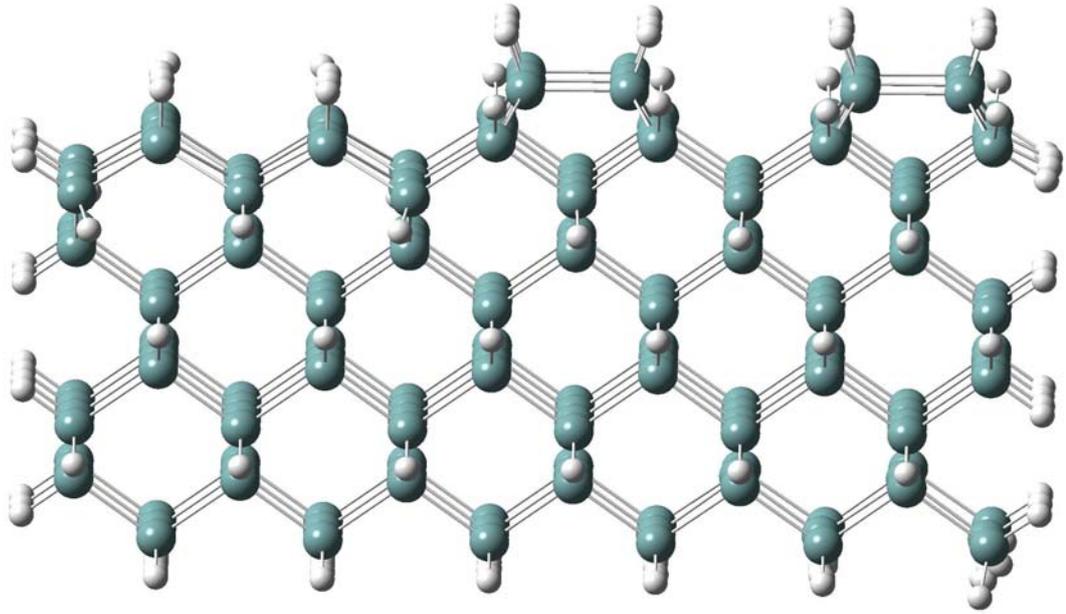
As it is introduced in chapter I, atomic steps, kinks or missing dimer type defects can be formed on the crystal surfaces during the growth process. Since the step edges are more attractive to initiate the adsorption, chemical reactions and catalysis, the investigations in the literature have been usually focused on defected crystal surfaces having single or double atomic steps. According to the outline introduced in chapter I, vicinal Ge(100) surface can have single ( $S_A$  or  $S_B$ ) or double ( $D_A$  or  $D_B$ ) atomic steps when the miscut angle is less or greater than  $\sim 6^\circ$ , respectively [31-36, 38, 43-44]. For both types of step structures, the step edge is the boundary between the upper and lower terraces. Since the rows of dimers on the upper and lower terraces are parallel and perpendicular to the step edge, the upper and lower terraces in  $S_A$  type vicinal surface are defined by  $(2 \times 1)$  and  $(1 \times 2)$  reconstructions. The reconstruction is in  $(1 \times 2)$  and  $(2 \times 1)$  periods on the upper and lower terraces, respectively, for  $S_B$  type steps. However, the reconstruction is same for both terraces, i.e.  $(2 \times 1)$  for  $D_A$  and  $(1 \times 2)$  for  $D_B$  type steps. The top view of the steps structures,  $S_A$ ,  $S_B$ ,  $D_A$ , and  $D_B$  are given in Fig. 3.3. In Fig. 3.3, the open big and small circles define the positions of the first layer dimerized Ge atoms on the upper and lower terraces of



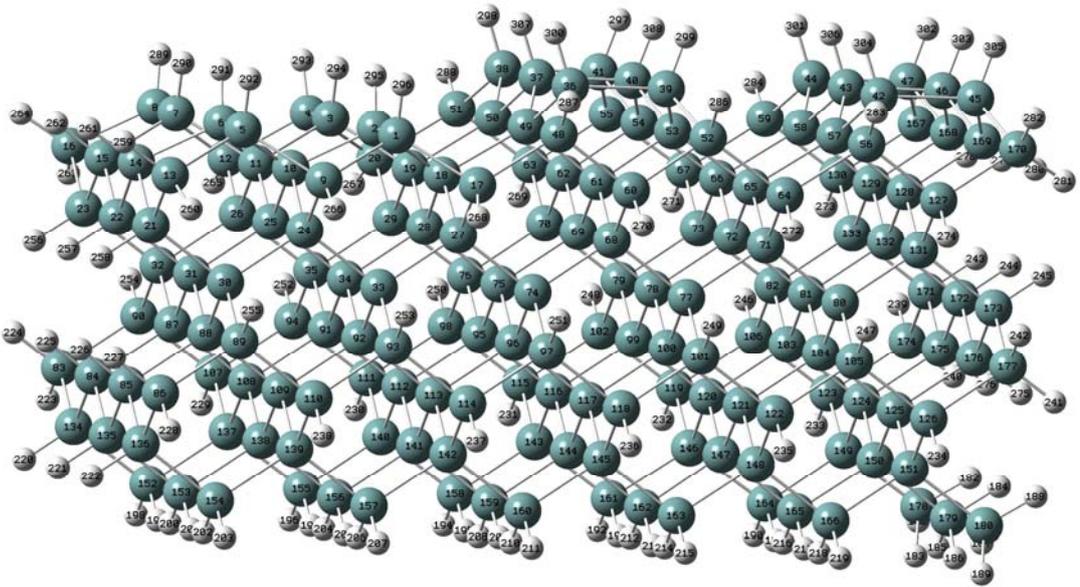
**FIG. 3.3.** Top views of (a)  $S_A$ , (b)  $D_A$ , (c)  $S_B$ , and (d)  $D_B$  steps.

the step models, respectively. In the same figure, the positions of the second and third layer Ge atoms on the upper and lower terraces of the step models are shown by the closed circles having different sizes. Since the aim of this project is to find out only the effect of step on the reaction mechanisms, the vicinal Ge(100) surface is considered to be kinks free. Therefore the present kinks free Ge(100) surface could have either  $S_A$  or  $S_B$  type steps. In the present work, the vicinal Ge(100) surface is determined to be  $S_A$  type instead of  $S_B$ . Because  $S_A$  type steps have relatively less attractive kinks than  $S_B$  [52]. The prototype of the kinks free vicinal Ge(100) surface with  $S_A$  type step is modeled by a cluster consists of nine and eight sublayers on the upper and lower terraces, respectively. The (2x1) and (1x2) periods on the upper and lower terraces are formed by three and two dimer rows, respectively in the cluster model. All the dimer bonds in the stepped Ge(100) cluster are asymmetric with a length of  $2.54\text{\AA}$  and a tilt angle of  $\sim 14^\circ$ . Because of the compensation of the

dangling bonds at the step edge, the dimer bonds are elongated with respect to the ones on the flat Ge(100)(2x1) surface. Since the present calculations are based on optimized structures, the initial length and tilt angle of the asymmetric dimer bonds on Ge(100) cluster do not need to be determined precisely. The length and tilt angle of the asymmetric dimer bonds on optimized stepped Ge(100) cluster are determined to be  $2.50\text{\AA}$  and  $\sim 4^\circ$ , respectively. The  $S_A$  type stepped Ge(100) cluster with hydrogenated dangling bonds is pictured in Fig. 3.4.



(a)



(b)

**FIG. 3.4.** The side view (a) and the perspective (b) of the  $S_A$  type stepped Ge(100) cluster with hydrogenated dangling bonds.

## CHAPTER 4

### RESULTS:1

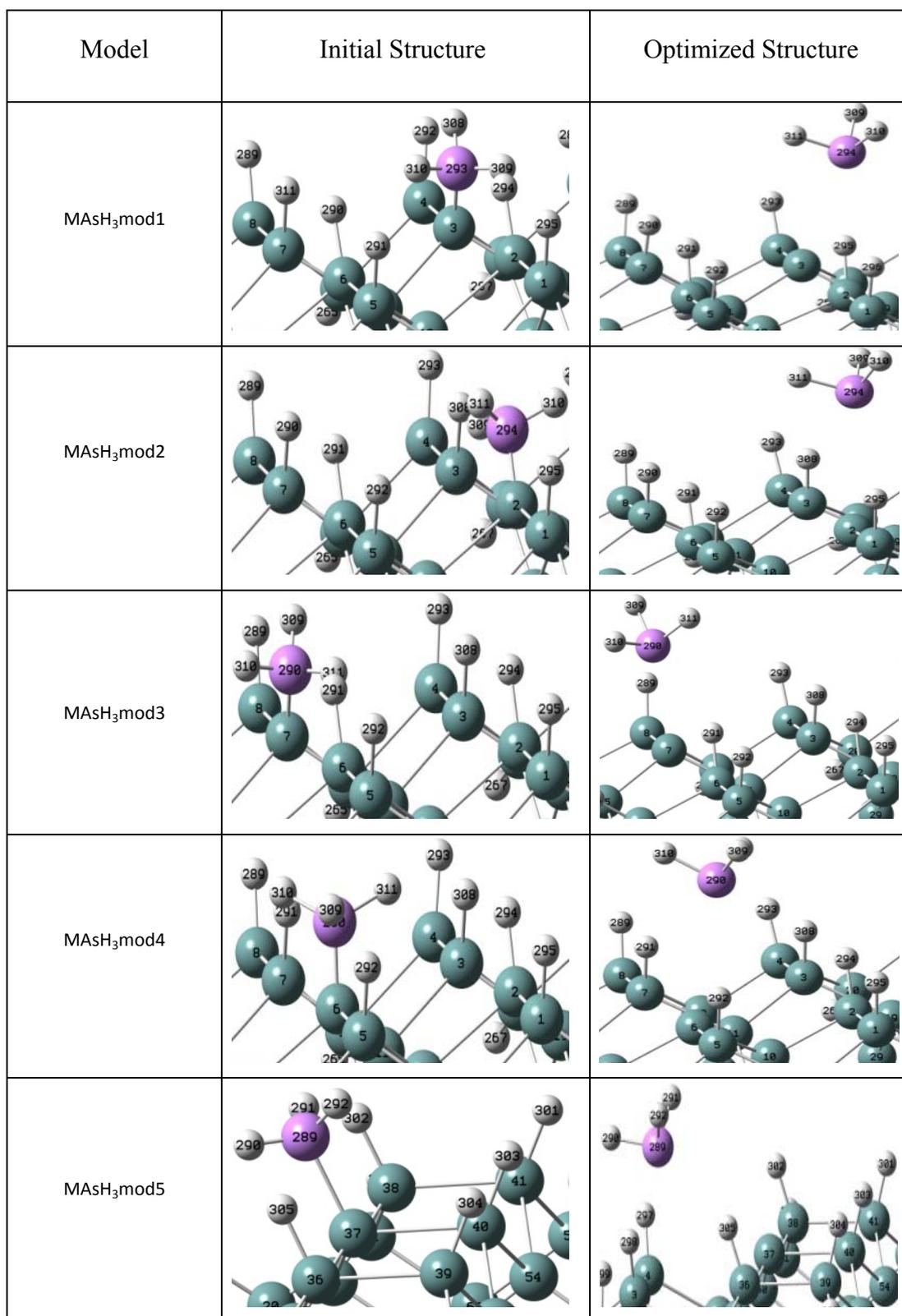
## STEPPED Ge(100) SURFACE EXPOSED TO ARSINE GAS

### 4.1. Introduction

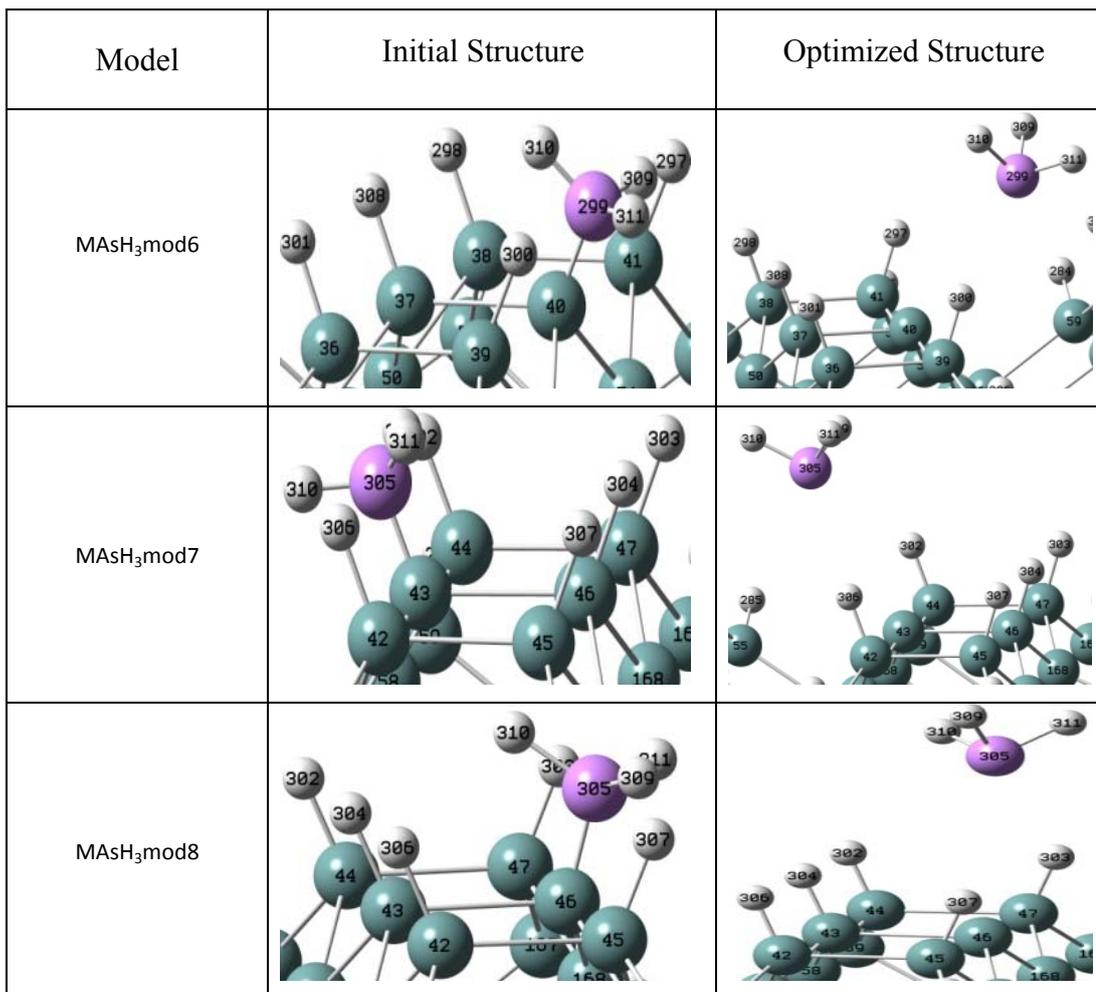
In the present work, the n-type doping process of the Ge sample exposed to arsine gas has been simulated by the possible adsorption and dissociation models of  $\text{AsH}_3$  on stepped Ge(100) surface. The total energy and the binding energy have been calculated for the models and  $\text{AsH}_3$ ,  $\text{AsH}_2$ ,  $\text{AsH}$ ,  $\text{As}$ , respectively, to find out the initial stages of the doping process of Ge(100) surface by Arsenic atoms.

### 4.2 Adsorption of $\text{AsH}_3$ on Stepped Ge(100) surface

In the present work, the adsorption of  $\text{AsH}_3$  molecule on  $S_A$  type stepped Ge(100) surface has been investigated by considering single and double open surface bonds on step-down and step-up terraces. In the first group adsorption models (MAsH<sub>3</sub>mod1-MAsH<sub>3</sub>mod8),  $\text{AsH}_3$  molecule is adsorbed to the step-down (MAsH<sub>3</sub>mod1-MAsH<sub>3</sub>mod4) and step-up (MAsH<sub>3</sub>mod5-MAsH<sub>3</sub>mod8) terraces via an open Ge bond taken at the step and close to the step regions. Since the stepped Ge(100) surface has asymmetric dimer bonds, the adsorption of  $\text{AsH}_3$  is considered for both buckled-up and buckled-down Ge atoms, separately. The other open bonds of the stepped Ge surface are saturated by H atoms. The adsorption input models of  $\text{AsH}_3$  on  $S_A$  type stepped Ge surface having single open bond are pictured in Fig. 4.1,



**FIG. 4.1.** The initial and optimized adsorption models of AsH<sub>3</sub> on stepped Ge(100) surface having single open bond.



**FIG. 4.1.** (Cont.)

by the labels of the surface Ge atoms given in Fig. 3.4. As an example, in MAsH<sub>3</sub>mod1 structure, AsH<sub>3</sub> molecule is adsorbed to buckled-down side of the dimer bond via third Ge atom when the other surface atoms are totally compensated by H atoms. In the present work, the input geometries of the adsorption models are optimized by minimizing their total energies. The optimized structures of MAsH<sub>3</sub>mod1 - MAsH<sub>3</sub>mod8 models are pictured in Fig. 4.1. The total energy of each optimized model is given in Table 4.1. The binding energy of AsH<sub>3</sub> in each optimized adsorption model has been also calculated by Eq. (1.1) and tabulated in Table 4.1. The total energy calculations have shown that, the most probable adsorption model is MAsH<sub>3</sub>mod2 in which AsH<sub>3</sub> is initially adsorbed to the buckled

**TABLE 4.1.** The structural parameters, the total energy, and the binding energy of AsH<sub>3</sub>, for the optimized adsorption models of AsH<sub>3</sub> on stepped Ge(100) surface having single open bond.

Model	Bond Length(A°)			Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-As	As-H	Dimer Ge-Ge			
MAsH <sub>3</sub> mod1	4.21	1.45	2.45	3.5	-371613.8565	-5.113
MAsH <sub>3</sub> mod2	4.20	1.45	2.50	0.5	-371613.8571	-5.129
MAsH <sub>3</sub> mod3	4.26	1.45	2.45	5.8	-371613.8556	-5.102
MAsH <sub>3</sub> mod4	4.29	1.45	2.49	0.5	-371613.8563	-5.112
MAsH <sub>3</sub> mod5	4.20	1.45	2.47	1	-371613.8563	-5.105
MAsH <sub>3</sub> mod6	4.28	1.45	2.47	1	-371613.8562	-5.102
MAsH <sub>3</sub> mod7	4.36	1.45	2.48	0.9	-371613.8560	-5.099
MAsH <sub>3</sub> mod8	4.33	1.45	2.48	0.2	-371613.8558	-5.104

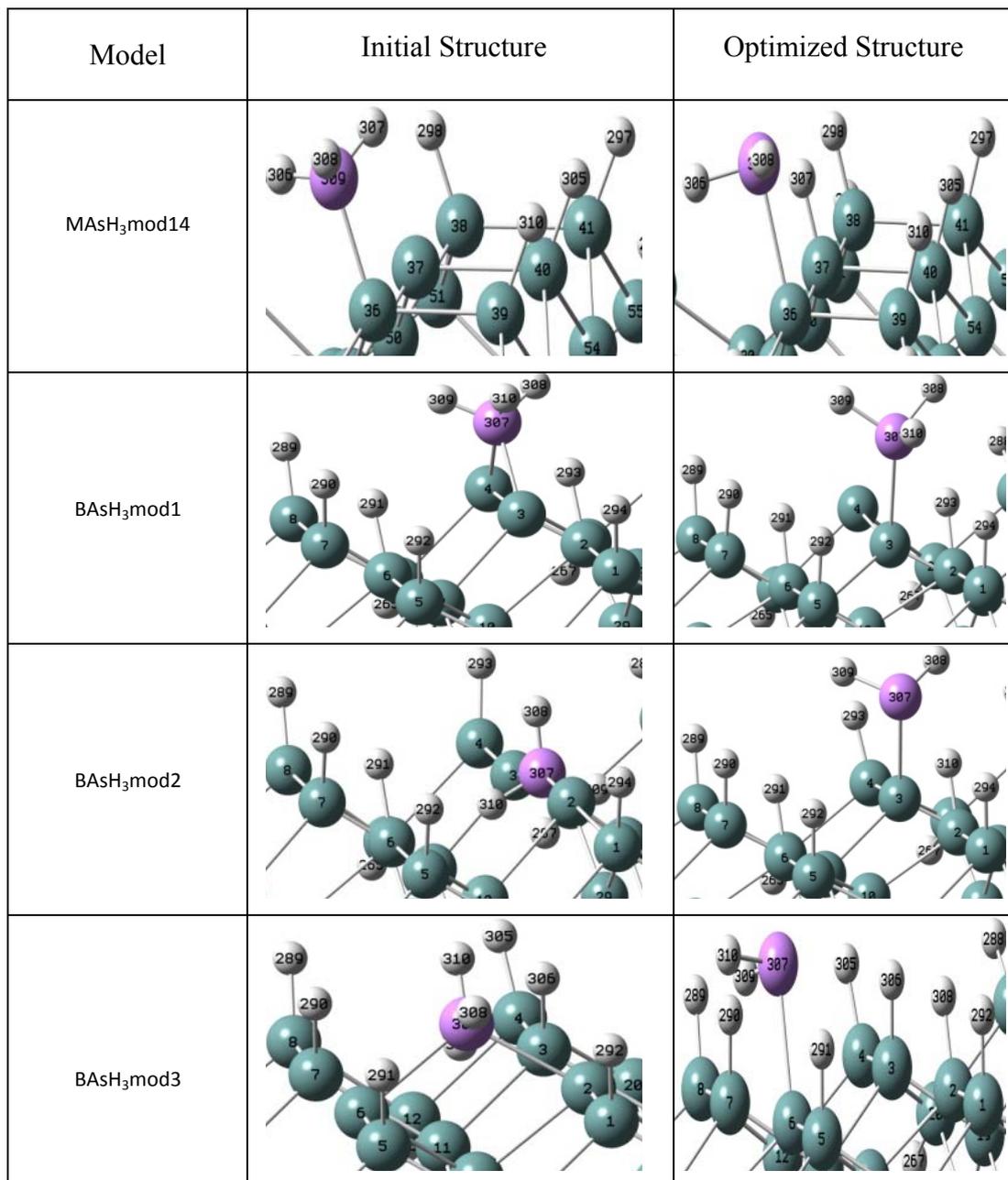
up Ge atom at the step region of the step-down terrace. Since the total energies of the stepped Ge(100) surfaces (having single open bond at different sites) have found to be approximately the same (-369402.7350 - (-369402.7355) a.u), the most probable adsorption model (MAsH<sub>3</sub>mod2) has been also confirmed by the binding energy of AsH<sub>3</sub>. The minimum binding energy of AsH<sub>3</sub> is calculated to be -5.129eV for MAsH<sub>3</sub>mod2 structure. Although the total energies of the models (Table 4.1) are very close to each other, there is a small energy difference of 0.038eV between the step down models (MAsH<sub>3</sub>mod1-MAsH<sub>3</sub>mod4) in which AsH<sub>3</sub> is initially adsorbed to the step and closed to the step regions. The energy difference is calculated to be 0.014eV for corresponding models (MAsH<sub>3</sub>mod5-MAsH<sub>3</sub>mod8) of the step-up terrace. On the other hand, the total energy of the most probable adsorption model (MAsH<sub>3</sub>mod2) is found to be ~0.022eV lower than the total energies of the step-up

models. In all adsorption models (MAsH<sub>3</sub>mod1-MAsH<sub>3</sub>mod8), AsH<sub>3</sub> molecule has been suspended on the open Ge bond after optimization. In most probable adsorption model (MAsH<sub>3</sub>mod2), AsH<sub>3</sub> molecule has suspended on the open bond of the second Ge atom with a Ge-As distance of 4.20 Å. The asymmetric dimer bond structure of the surface is found to be not changed by optimization.

The adsorption of AsH<sub>3</sub> on stepped Ge(100) surface with two open bonds has been defined by unbridged MAsH<sub>3</sub>mod9-MAsH<sub>3</sub>mod14 and bridged BAsH<sub>3</sub>mod1-BAsH<sub>3</sub>mod5 models. Since the total energies of the adsorption models at the step region are found to be lower than those of the others in the group of MAsH<sub>3</sub>mod1-MAsH<sub>3</sub>mod8 models, the two open bonds are considered at the step region for both terraces. The two open surface bonds are either on the same or adjacent dimer bonds. In MAsH<sub>3</sub>mod9-MAsH<sub>3</sub>mod14 models, AsH<sub>3</sub> molecule is initially adsorbed to one of the open bond when the other bond is open. The two open bonds considered on the step-down and step-up terraces have also allowed forming bridge adsorption models (BAsH<sub>3</sub>mod1-BAsH<sub>3</sub>mod5). In Fig. 4.2, the initial and optimized models correspond to two dangling bonds of the surface are pictured by the labels of Ge atoms given in Fig. 3.4. The total energies of the optimized bridged and optimized unbridged adsorption models have been listed in Table 4.2. The optimized unbridged adsorption models (MAsH<sub>3</sub>mod9-MAsH<sub>3</sub>mod14) have expressed two kinds of structures; when the model has two open bonds on the same dimer bond, AsH<sub>3</sub> remains on the initial adsorption bond leaving the other bond as open (MAsH<sub>3</sub>mod9, MAsH<sub>3</sub>mod10, MAsH<sub>3</sub>mod13), but when the two open bonds are on the adjacent dimers, AsH<sub>3</sub> dissociates into AsH<sub>2</sub> and H fragments (MAsH<sub>3</sub>mod11, MAsH<sub>3</sub>mod12, MAsH<sub>3</sub>mod14). Similarly, when the bridged adsorption models are considered on the same dimer bond (BAsH<sub>3</sub>mod1, BAsH<sub>3</sub>mod4), AsH<sub>3</sub> breaks the bridge and adsorbs to one of the open bond after optimization. But in the other bridged adsorption models (BAsH<sub>3</sub>mod2, BAsH<sub>3</sub>mod3, BAsH<sub>3</sub>mod5), initially AsH<sub>3</sub> makes a bridge between the adjacent dimers and decomposes to AsH<sub>2</sub> and H fragments spontaneously after optimization. Therefore when the stepped Ge terraces with more

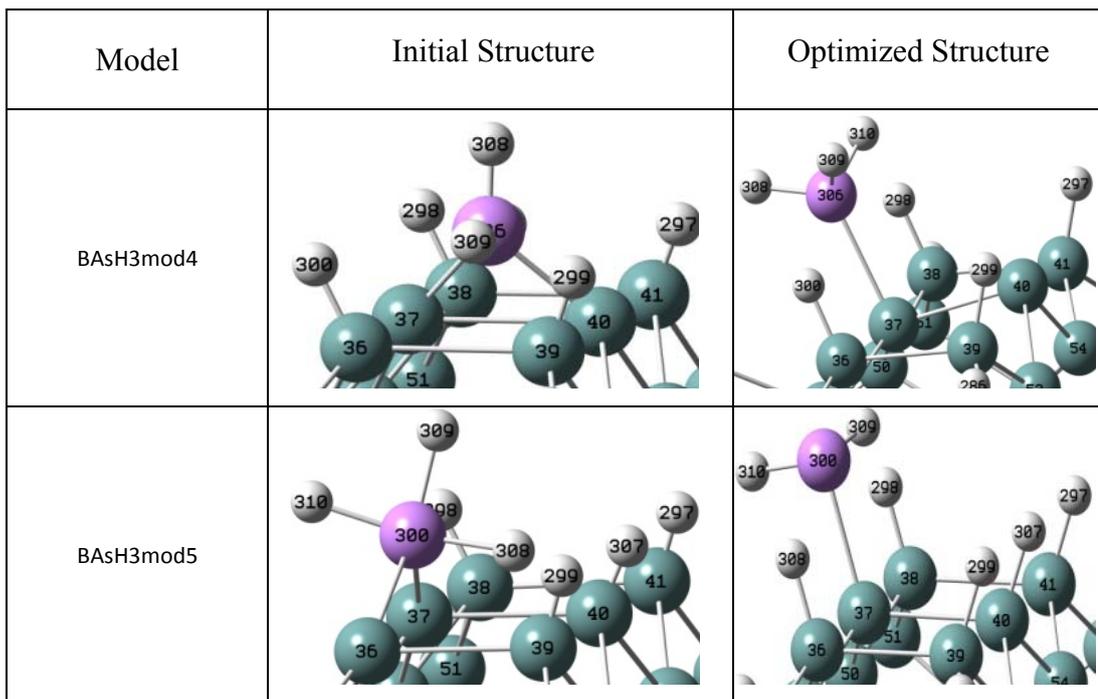
Model	Initial Structure	Optimized Structure
MAsh <sub>3</sub> mod9		
MAsh <sub>3</sub> mod10		
MAsh <sub>3</sub> mod11		
MAsh <sub>3</sub> mod12		
MAsh <sub>3</sub> mod13		

**FIG. 4.2.** The initial and optimized adsorption models of AsH<sub>3</sub> on stepped Ge(100) correspond to two dangling bonds of the surface.



**FIG. 4.2.** (Cont.)

than one dangling bonds on the same or different dimers adjacent to each other have been exposed to arsine gas, AsH<sub>3</sub> molecules will be adsorbed to the surface either directly or dissociatively. The most probable direct adsorption models of AsH<sub>3</sub> are obtained by optimization of BAsH<sub>3</sub>mod1 and BAsH<sub>3</sub>mod4 models on the step-down and step-up terraces respectively. The binding energy of AsH<sub>3</sub> are calculated (Eq. 1.1) to be -6.544 and -6.789eV in BAsH<sub>3</sub>mod1 and BAsH<sub>3</sub>mod4, respectively. Since



**FIG. 4.2.** (Cont.)

the adsorption of  $\text{AsH}_3$  to the surface is not provided actually in the most probable structure of  $\text{MAsH}_3\text{mod}2$  (Fig.4.1 and Table 4.1), the binding energy of  $\text{AsH}_3$  in this model is higher than those in optimized  $\text{BAsH}_3\text{mod}1$  and  $\text{BAsH}_3\text{mod}4$  structures (Fig. 4.2 and Table 4.2). In optimized  $\text{BAsH}_3\text{mod}1$  and  $\text{BAsH}_3\text{mod}4$  models,  $\text{AsH}_3$  has adsorbed to the buckled down bond of the dimer with a bond length of  $\sim 2.51\text{\AA}$  and increased the buckled angle (tilt angle) of the dimer after optimization. In these most probable models, the dimer bond is found to be elongated ( $2.50\text{-}2.56\text{\AA}$ ) by the adsorption of  $\text{AsH}_3$  molecule. According to the total energies given in Table 4.2, the most probable dissociation models of  $\text{AsH}_3$  in ( $\text{AsH}_2$ , H) form are obtained when  $\text{AsH}_3$  molecule makes a bridge between the rows of the dimers on both step-down ( $\text{BAsH}_3\text{mod}3$ ) and step-up ( $\text{BAsH}_3\text{mod}5$ ) terraces. Although the  $\text{AsH}_3$  molecule is also dissociated into  $\text{AsH}_2$  and H fragments in the optimized  $\text{MAsH}_3\text{mod}11$ ,  $\text{MAsH}_3\text{mod}12$ ,  $\text{MAsH}_3\text{mod}14$ , and  $\text{BAsH}_3\text{mod}2$  models, the total energies correspond to their local minima are all higher than the total energy of  $\text{BAsH}_3\text{mod}3$  model. The binding energies of  $\text{AsH}_2$  calculated by Eq. (1.1) are  $-6.073$  and  $-5.967\text{eV}$  (Table 4.2) for the most probable structures of  $\text{BAsH}_3\text{mod}3$  and  $\text{BAsH}_3\text{mod}5$ , respectively. Therefore the adsorption of  $\text{AsH}_2$  on step-down terrace is

**TABLE 4.2.** The structural parameters, the total energy, and the binding energy of AsH<sub>3</sub> (or AsH<sub>2</sub>), for the optimized adsorption models of AsH<sub>3</sub> on stepped Ge(100) correspond to two dangling bonds of the surface.

Model	Bond length(A <sup>o</sup> )			Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-As	As-H	Dimer Ge-Ge			
MAsH <sub>3</sub> mod9	2.52	1.45	2.53	16.2	-371613.2050	-6.391
MAsH <sub>3</sub> mod10	2.52	1.45	2.59	20.0	-371613.2048	-6.386
MAsH <sub>3</sub> mod11	2.38	1.45	2.51	0.2	-371613.3677	-5.970 for AsH <sub>2</sub>
MAsH <sub>3</sub> mod12	2.38	1.45	2.47	4.4	-371613.3669	-5.948 for AsH <sub>2</sub>
MAsH <sub>3</sub> mod13	2.50	1.45	2.58	19.7	-371613.2106	-6.666
MAsH <sub>3</sub> mod14	2.38	1.45	2.50	0.6	-371613.3674	-5.984 for AsH <sub>2</sub>
BAsH <sub>3</sub> mod1	2.51	1.45	2.50	15.8	-371613.2106	-6.544
BAsH <sub>3</sub> mod2	2.38	1.45	2.47	4.4	-371613.3681	-5.980 for AsH <sub>2</sub>
BAsH <sub>3</sub> mod3	2.38	1.45	2.42	9.8	-371613.3712	-6.073 for AsH <sub>2</sub>
BAsH <sub>3</sub> mod4	2.51	1.45	2.56	19.7	-371613.2151	-6.789
BAsH <sub>3</sub> mod5	2.38	1.45	2.48	0	-371613.3677	-5.967 for AsH <sub>2</sub>

stronger than the adsorption on step-up terrace. The bond length between AsH<sub>2</sub> and the surface Ge atom is found to be 2.38A<sup>o</sup> in both most probable structures, BAsH<sub>3</sub>mod3 and BAsH<sub>3</sub>mod5. The optimized geometries of BAsH<sub>3</sub>mod3 and BAsH<sub>3</sub>mod5 have illustrated that, H atoms appeared by the dissociation of AsH<sub>3</sub> will be adsorbed to one of the open surface bonds. Hence at this initial stage of the doping process, AsH<sub>3</sub>, AsH<sub>2</sub>, and H will be appeared totally on the stepped Ge(100) surface depending on the positions of the open bonds in front of AsH<sub>3</sub> molecules.

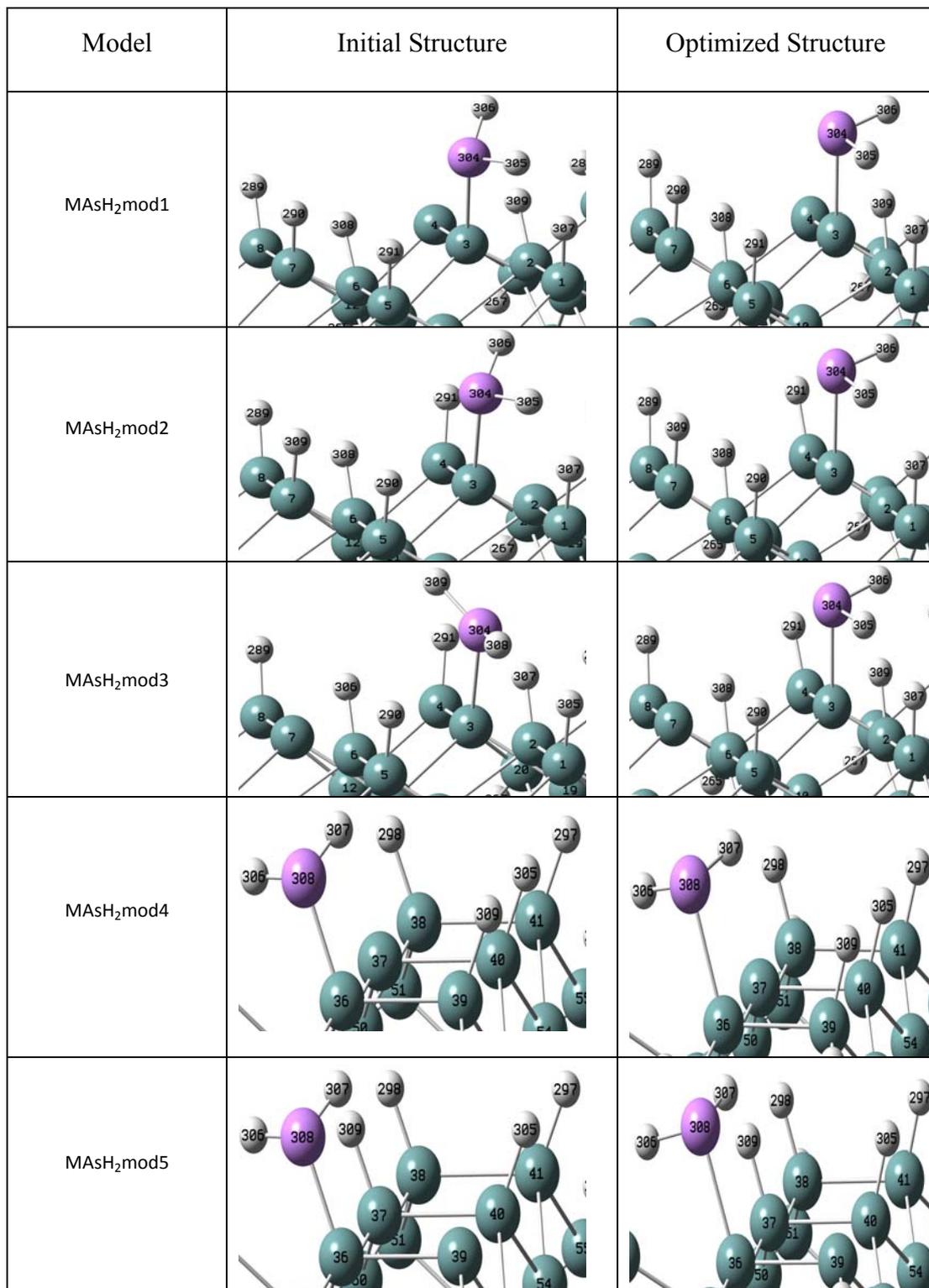
### 4.3 Adsorption of AsH<sub>2</sub> on Stepped Ge(100) surface

At this stage of the work, molecular adsorption of AsH<sub>2</sub> on stepped Ge surface has been confirmed by the optimization of unbridged and bridged adsorption models pictured in Fig. 4.3. The structural parameters and the total energies of the considered models are tabulated in Table 4.3. It is found that, AsH<sub>2</sub> prefers molecular adsorption actually in all considered adsorption models. In all optimized unbridged and bridged models AsH<sub>2</sub> is found to be bounded to one of the open surface bond with a bond length of 2.38 Å while the other bond is open. This outcome has excluded the spontaneous dissociative adsorption of AsH<sub>2</sub> on stepped Ge surface. Since the adsorption of AsH<sub>2</sub> is studied directly, the binding energy of AsH<sub>2</sub> (Table 4.3) in MAsH<sub>2</sub>mod1-MAsH<sub>2</sub>mod5 and BAsH<sub>2</sub>mod1-BAsH<sub>2</sub>mod5 is lower by ~2 eV than those (Table 4.2) in the dissociative adsorption models of AsH<sub>3</sub>. But, the most probable adsorption model of AsH<sub>2</sub> among the models in Table 4.3 (dissociative adsorption models of AsH<sub>3</sub>) and table 4.2 is found to be the same in which AsH<sub>2</sub> is bounded to the buckled down of the dimer.

### 4.4 Adsorption of AsH on Stepped Ge(100) surface

The adsorption of AsH<sub>2</sub> molecule on the surface has been expected to be followed by the adsorption of AsH molecule when one of the H atoms of AsH<sub>2</sub> has formed H<sub>2</sub> molecule with an adjacent H atom and desorbed from the surface. At this stage, the surface H atoms remained by the dissociation of AsH<sub>3</sub> (as AsH<sub>2</sub> and H) make the built up of H<sub>2</sub> molecules possible.

In the present work, the adsorption of AsH on stepped Ge(100) surface has been modeled again by unbridged (MAsHmod1-MAsHmod5) and bridged (BAsHmod1-BAsHmod5) models on the step-down and step-up terraces. The initial and optimized adsorption models of AsH are totally pictured in Fig. 4.4 by the labels of surface Ge atoms given in Fig. 3.4. In unbridged models, two open bonds are considered either on the same or adjacent dimer bonds. Therefore AsH molecule is adsorbed to one of the open bonds, when the other bond is open. In bridged models, AsH makes a



**FIG. 4.3.** The initial and optimized adsorption models of AsH<sub>2</sub> on stepped Ge(100) surface.

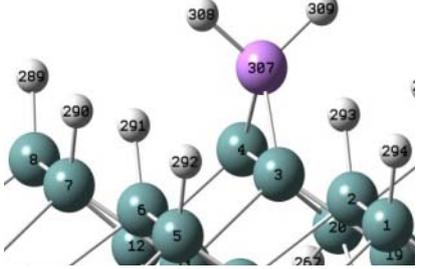
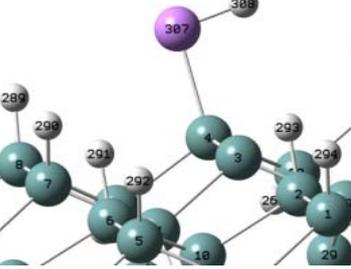
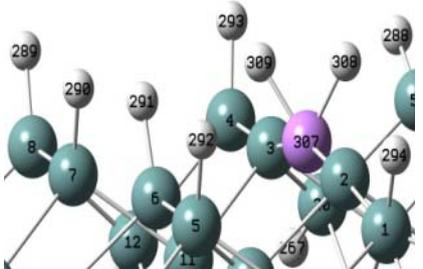
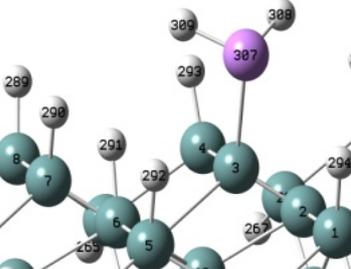
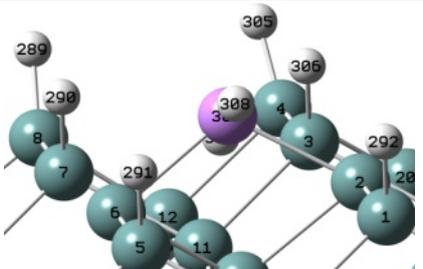
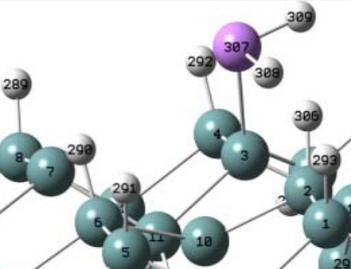
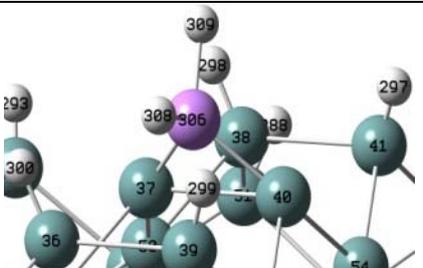
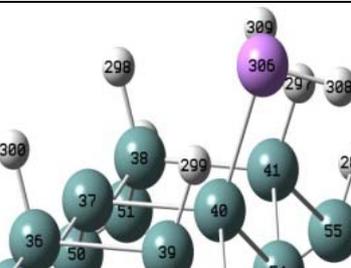
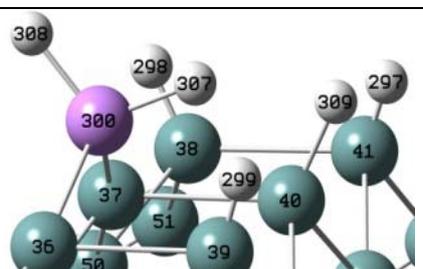
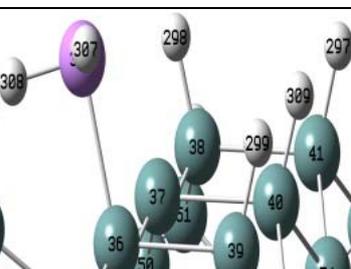
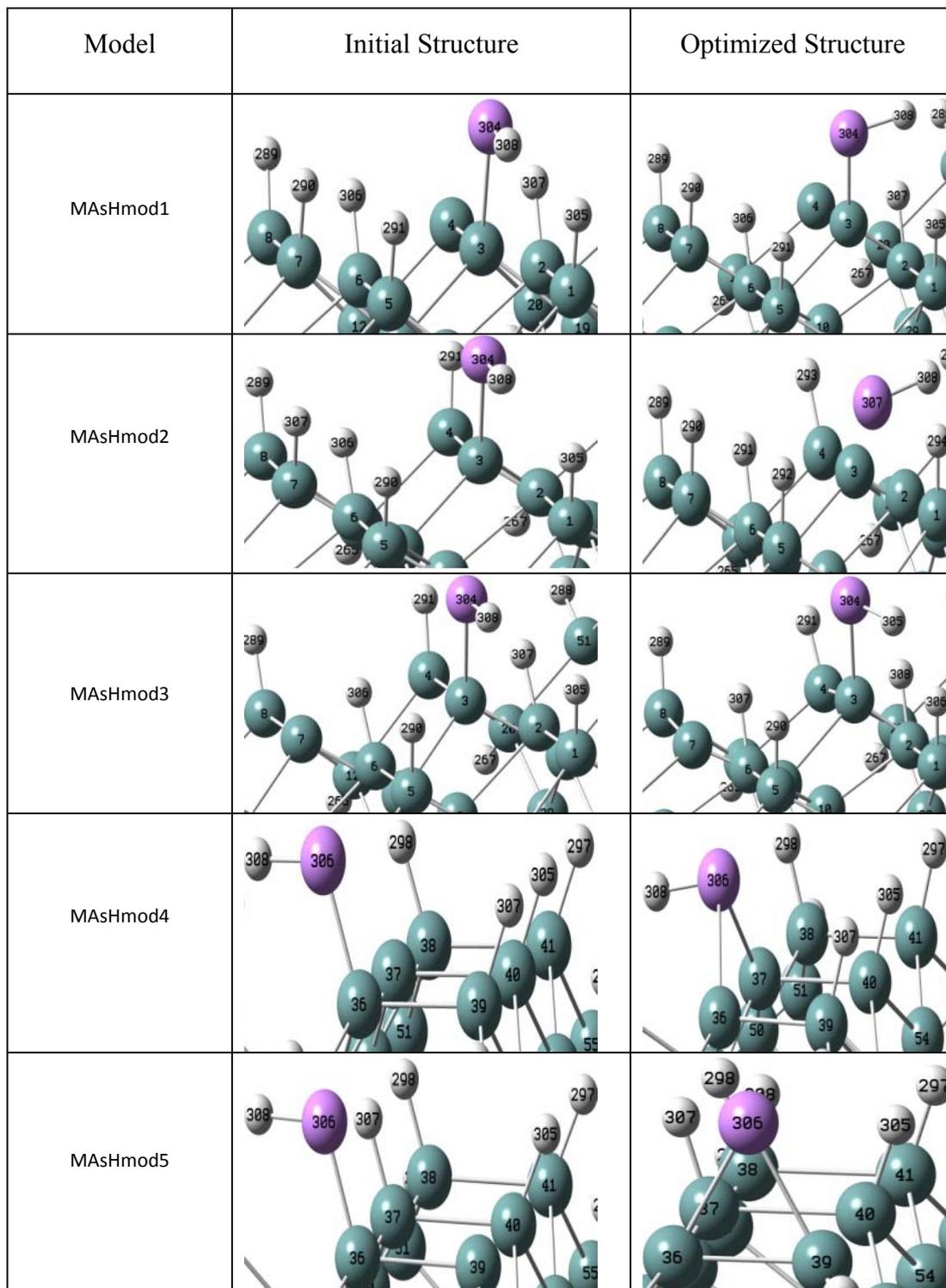
Model	Initial Structure	Optimized Structure
BAsH <sub>2</sub> mod1	 <p>Initial structure of BAsH<sub>2</sub>mod1 showing a central boron atom (307) and arsenic atoms (308) in a lattice environment. Atoms are numbered 1 through 12.</p>	 <p>Optimized structure of BAsH<sub>2</sub>mod1 showing the same lattice environment with the central boron atom (307) and arsenic atoms (308) in a different configuration. Atoms are numbered 1 through 12.</p>
BAsH <sub>2</sub> mod2	 <p>Initial structure of BAsH<sub>2</sub>mod2 showing a central boron atom (307) and arsenic atoms (308) in a lattice environment. Atoms are numbered 1 through 12.</p>	 <p>Optimized structure of BAsH<sub>2</sub>mod2 showing the same lattice environment with the central boron atom (307) and arsenic atoms (308) in a different configuration. Atoms are numbered 1 through 12.</p>
BAsH <sub>2</sub> mod3	 <p>Initial structure of BAsH<sub>2</sub>mod3 showing a central boron atom (308) and arsenic atoms (305, 306) in a lattice environment. Atoms are numbered 1 through 12.</p>	 <p>Optimized structure of BAsH<sub>2</sub>mod3 showing the same lattice environment with the central boron atom (307) and arsenic atoms (308) in a different configuration. Atoms are numbered 1 through 12.</p>
BAsH <sub>2</sub> mod4	 <p>Initial structure of BAsH<sub>2</sub>mod4 showing a central boron atom (305) and arsenic atoms (308) in a lattice environment. Atoms are numbered 1 through 54.</p>	 <p>Optimized structure of BAsH<sub>2</sub>mod4 showing the same lattice environment with the central boron atom (306) and arsenic atoms (309) in a different configuration. Atoms are numbered 1 through 54.</p>
BAsH <sub>2</sub> mod5	 <p>Initial structure of BAsH<sub>2</sub>mod5 showing a central boron atom (300) and arsenic atoms (307) in a lattice environment. Atoms are numbered 1 through 54.</p>	 <p>Optimized structure of BAsH<sub>2</sub>mod5 showing the same lattice environment with the central boron atom (307) and arsenic atoms (309) in a different configuration. Atoms are numbered 1 through 54.</p>

FIG. 4.3. (Cont.)

**TABLE 4.3.** The structural parameters, the total energy, and the binding energy of AsH<sub>2</sub>, for the optimized adsorption models of AsH<sub>2</sub> on stepped Ge(100) surface.

Model	Bond length(A°)			Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-As	As-H	Dimer Ge-Ge			
MAsH <sub>2</sub> mod1	2.38	1.45	2.46	3.7	-371612.7402	-7.902
MAsH <sub>2</sub> mod2	2.38	1.45	2.47	4.4	-371612.7413	-8.661
MAsH <sub>2</sub> mod3	2.38	1.45	2.47	4.4	-371612.7403	-8.628
MAsH <sub>2</sub> mod4	2.38	1.45	2.50	0.5	-371612.7408	-7.956
MAsH <sub>2</sub> mod5	2.38	1.45	2.49	0.2	-371612.7405	-8.032
BAsH <sub>2</sub> mod1	2.38	1.45	2.46	3.4	-371612.7453	-8.040
BAsH <sub>2</sub> mod2	2.38	1.45	2.47	4.4	-371612.7427	-8.653
BAsH <sub>2</sub> mod3	2.38	1.45	2.46	4	-371612.5798	-8.628
BAsH <sub>2</sub> mod4	2.38	1.45	2.48	1.5	-371612.7410	-8.046
BAsH <sub>2</sub> mod5	2.38	1.45	2.50	0.6	-371612.7417	-7.981

bridge between the open bonds either on the same as adjacent dimer bonds. The total energies of the models given in Table 4.4 have indicated that, AsH has preferred to make a bridge between the open bonds after optimization. The tendency of AsH to the bridged models has been also found in some optimized unbridged adsorption models (MAsHmod2, MAsHmod4, MAsHmod5). The most probable adsorption model of AsH corresponds to the minimum of the total energy is obtained when AsH makes a bridge between the open bonds on the same dimer bond of the step-down (BAsHmod1) and step-up (MAsHmod5) terraces. In optimized structures of these models, AsH is bonded to two surface Ge atoms with a bond length of 2.36A° and binding energy of ~ -10.7eV (Table 4.4). The optimized bridged models



**FIG. 4.4.** The initial and optimized adsorption models of AsH on stepped Ge(100) surface.

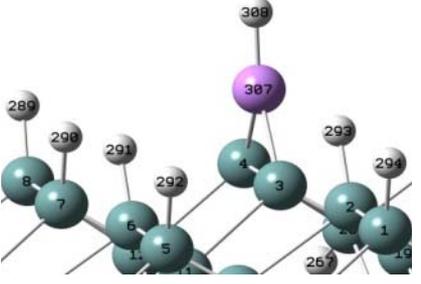
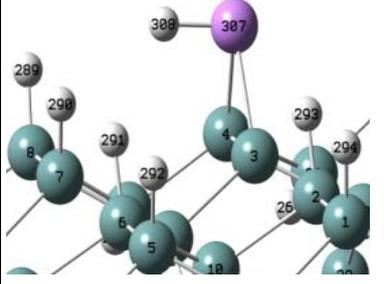
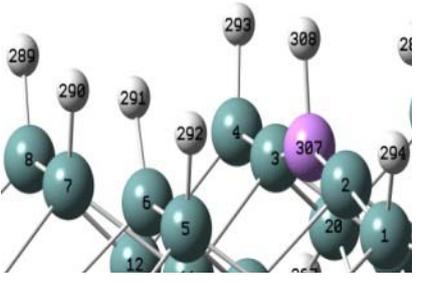
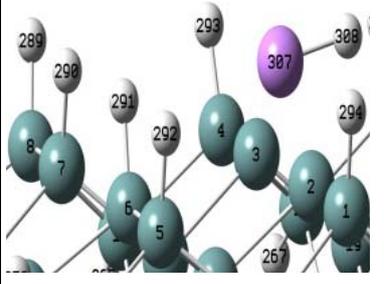
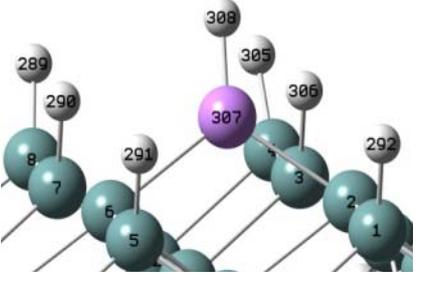
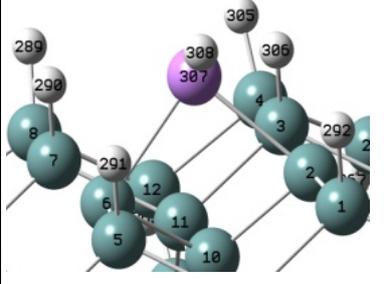
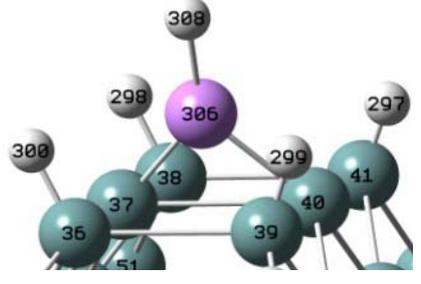
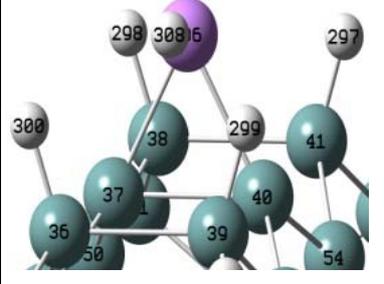
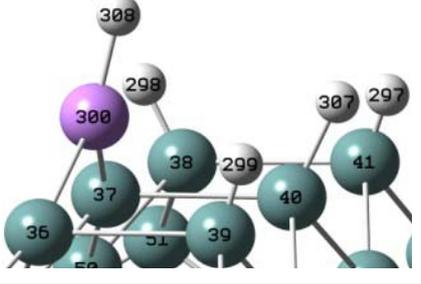
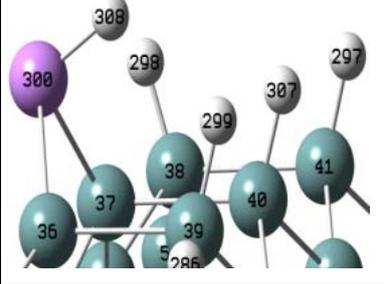
Model	Initial Structure	Optimized Structure
BAsHmod1		
BAsHmod2		
BAsHmod3		
BAsHmod4		
BAsHmod5		

FIG. 4.4. (Cont.)

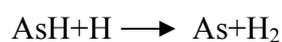
**TABLE 4.4.** The structural parameters, the total energy, and the binding energy of AsH for the optimized adsorption models of AsH on stepped Ge(100) surface.

Model	Bond length(A°)			Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-As	As-H	Dimer Ge-Ge			
MAsHmod1	2.16	1.45	2.87	19	-371612.0410	-7.105
MAsHmod2	2.65	1.45	2.71	18	-371612.0792	-8.874
MAsHmod3	2.25	1.45	2.47	4.5	-371612.0164	-7.160
MAsHmod4	2.53	1.45	2.50	9.1	-371612.1264	-9.467
MAsHmod5	2.36	1.45	2.36	0.9	-371612.1682	-10.688
BAsHmod1	2.36	1.45	2.34	4.8	-371612.1716	-10.658
BAsHmod2	2.66	1.45	2.76	16.4	-371612.0814	-8.933
BAsHmod3	2.55	1.45	2.51	5.6	-371612.1150	-9.842
BAsHmod4	2.36	1.45	2.35	0.6	-371612.1680	-10.683
BAsHmod5	2.51	1.45	2.49	8	-371612.1292	-9.543

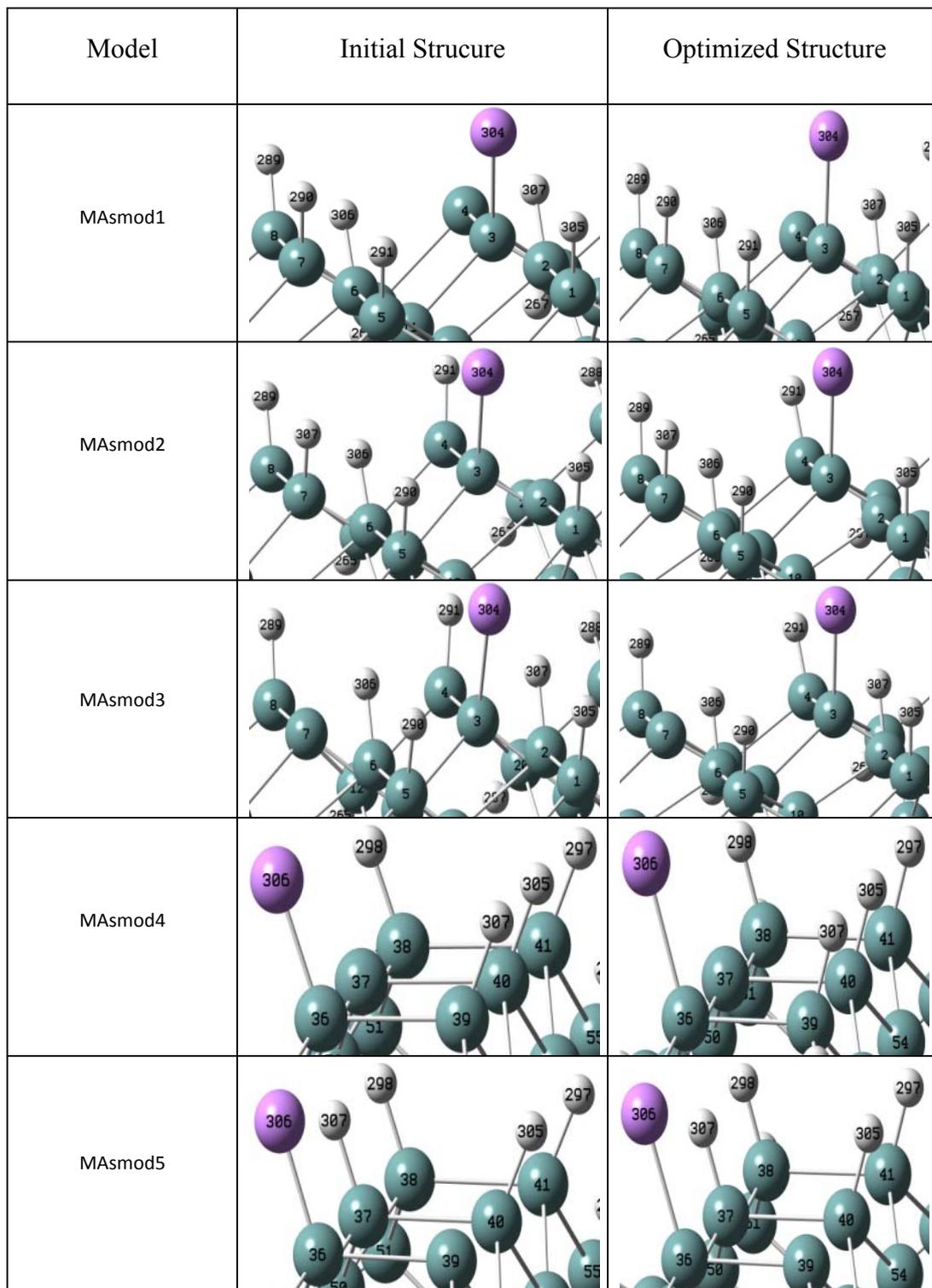
(BAsHmod2- BAsHmod4) have also indicated that AsH can make bridge between the adjacent dimers when one of the open bond on the same dimer is compensated by another fragment, H.

#### 4.5 Adsorption of As atom on Stepped Ge(100) surface

In this stage of the doping process of Ge sample, AsH<sub>3</sub> molecule of the arsine gas is expected to be reduced to As atom by



reaction. Here,  $H_2$  molecule, built up by H atom of AsH fragment and one of the adjacent surface H atom, has desorbed from the surface. The atomic adsorption of As has been examined by again unbridged (MAsmod1-MAsmod5) and bridged (BAsmod1-BAsmod5) models. It is examined whether the bridge model of AsH (Fig. 4.4) is broken or not during desorption of  $H_2$  from the surface. The initial and optimized adsorption structures of As on stepped Ge(100) surface are pictured in Fig. 4.5. The total energies of the models and the binding energy of As in these models are tabulated in Table 4.5. It is found that the adsorption of As on step-down and step-up terraces depend on the position of the open surface bonds. As atom has preferred to make the bridge structure between two Ge surface atoms when the open bonds are on the same dimer bond. Therefore the bridge structure of AsH on the same dimer (Fig. 4.4) has been saved on both step-down and step-up terraces by the adsorption of As. However, the bridge structures of AsH between the adjacent dimers (Fig. 4.4) have been found to be broken during the reduction of AsH to As. The bridge structure of As on the same dimer bond of the step-down terrace is characterized with the binding energy of -10.634eV and Ge-As bond length of  $2.36\text{\AA}$  in the optimized structure of BAsmod1. Similarly the bridge model of As atom (BAsmod4) on the same dimer bond of the step-up terrace becomes prominent by the binding energy of -10.661eV. On the other hand, the As atom has preferred the buckled down Ge atoms on both step-down and step-up terraces when the bridge structure of AsH between the adjacent dimers is broken during the desorption of  $H_2$  from the surface. In these most probable structures, MAsmod2 (or BAsmod2) and MAsmod5, the binding energy of As is calculated to be -10.936 and -10.237eV, respectively. The Ge-As bond length is found to be  $2.37\text{\AA}$  in the direct adsorption models.



**FIG. 4.5.** The initial and optimized adsorption models of As atom on stepped Ge(100) surface.

Model	Initial Structure	Optimized Structure
BAsmod1		
BAsmod2		
BAsmod3		
BAsmod4		
BAsmod5		

FIG. 4.5. (Cont.)

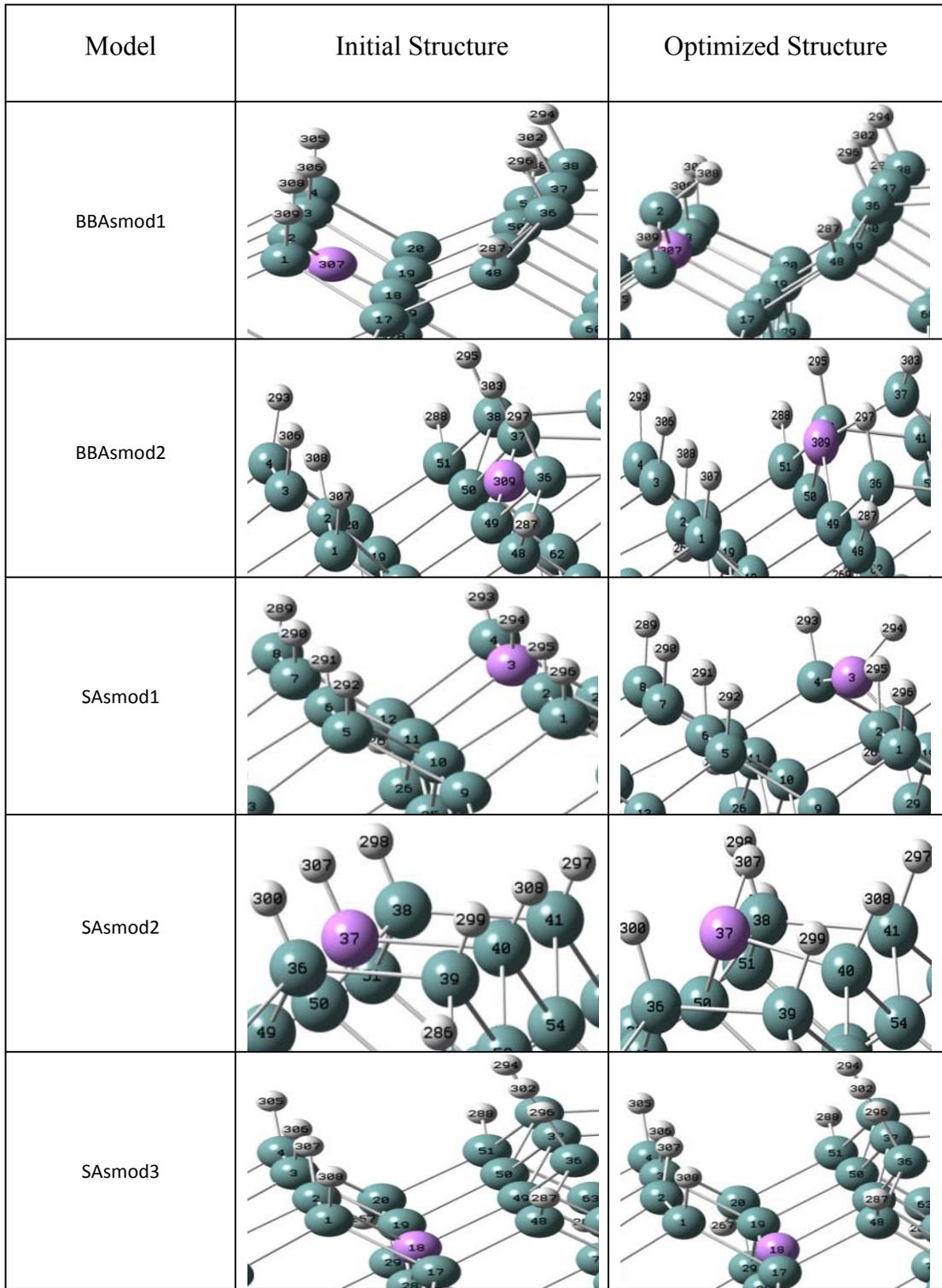
**TABLE 4.5.** The structural parameters, the total energy, and the binding energy of As, for the optimized adsorption models of As on stepped Ge(100) surface.

Model	Bondlength (Å <sup>o</sup> )		Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-As	Dimer Ge-Ge			
MAsmod1	2.37	2.46	5.6	-371611.5614	-10.163
MAsmod2	2.36	2.47	5.5	-371611.5630	-10.936
MAsmod3	2.36	2.47	5	-371611.5619	-10.9
MAsmod4	2.36	2.50	0	-371611.5627	-10.294
MAsmod5	2.37	2.50	0.4	-371611.5617	-10.237
BAsmo1	2.36	2.34	4.7	-371611.5787	-10.634
BAsmo2	2.37	2.47	5.3	-371611.5634	-10.947
BAsmo3	2.59	2.51	4.8	-371611.5217	-9.807
BAsmo4	2.36	2.35	0.5	-371611.5752	-10.661
BAsmo5	2.53	2.50	4.3	-371611.5343	-9.464

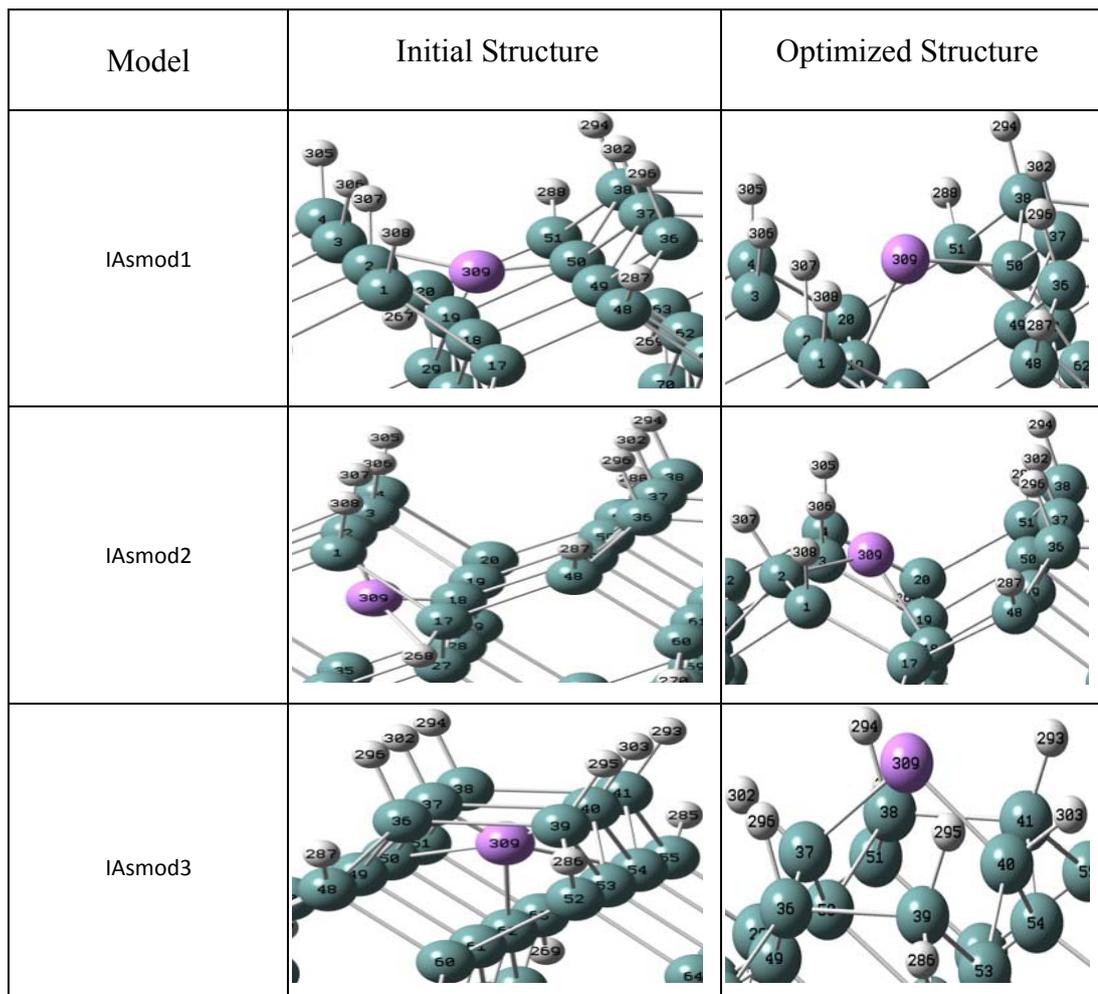
#### **4.6 Diffusion of As atom through the layers of Stepped Ge(100) surface**

In the last stage, the doping of stepped Ge(100) is simulated by the diffusion of the As atom towards the layers of the surface. During the diffusion, As atoms can have a sit between the surface Ge atoms breaking the Ge-Ge bonds or occupy substitutional

or interstitial places of the surface. The setting of As atoms between the surface Ge atoms on the step-down and step-up terraces is defined by BBAsmod1 and BBAsmod2 structures, respectively. The initial and optimized geometries, and the total energies of these models are given in Fig. 4.6 and Table 4.6, respectively. It is found that As atoms of these models push the adjacent Ge atoms out site the surface and occupy the empty places of Ge atoms after optimization. The binding energy of As in BBAsmod1 and BBAsmod2 structures is calculated (Eq. 1.1) to be -7.312 and -4.087eV, respectively. The other models SASmod1-SASmod3 and IASmod1-IASmod3 pictured in Fig. 4.6 have defined the substitutional and interstitial occupation sites of As atom on the stepped Ge(100) surface, respectively. In SASmod1-SASmod3 models, one site of Ge atom in the layers of the stepped Ge(100) surface is initially occupied by As atom. The main structures of these models are not changed after optimization (Fig. 4.6). The binding energy of As is calculated to be -3.843, -6.902, and -14.509eV for optimized SASmod1, SASmod2 and SASmod3 structures, respectively. It is found that the initial structures of IASmod1-IASmod3 models are changed mainly after optimization (Fig. 4.6). The IASmod1 model in which As atom is interstitial in the valley between the step-down and step-up terraces is converted to a bridge model between the layers of the terraces by optimization. Similarly the IASmod2 model in which As atom interstitially between the 1<sup>st</sup> and 2<sup>nd</sup> layers of the step-down terrace is changed to a bridge model between the adjacent Ge atoms on the 1<sup>st</sup> and 2<sup>nd</sup> layers of the step-down terrace. It is also found that, the interstitial site of As in IASmod3 has not been saved after optimization. In optimized IASmod3 structure, As atom has left its interstitial site and got out from the layers of the surface to make a bridge between the Ge atoms on the same dimer. The breakdown of the interstitial models (IASmod1-IASmod3) have indicated that As atoms do not prefer the interstitial sites during the doping process of the stepped Ge(100) surface. The binding energy of As is calculated to be -5.238, -9.080 and -8.022eV in optimized IASmod1, IASmod2 and IASmod3 structures, respectively. The binding energy of As in all BBAsmod1-BBAsmod2, SASmod1-SASmod2 and IASmod1- IASmod3 structures are found to be higher than that in the most probable adsorption models in which As atom is adsorbed to the step-down and step-up terraces with bridge (BASmod1, BASmod4) and unbridged (MASmod2, MASmod5) models. This outcome illustrates that, the substitutional



**FIG. 4.6.** The initial and optimized diffusion models of As atom on stepped Ge(100) surface.



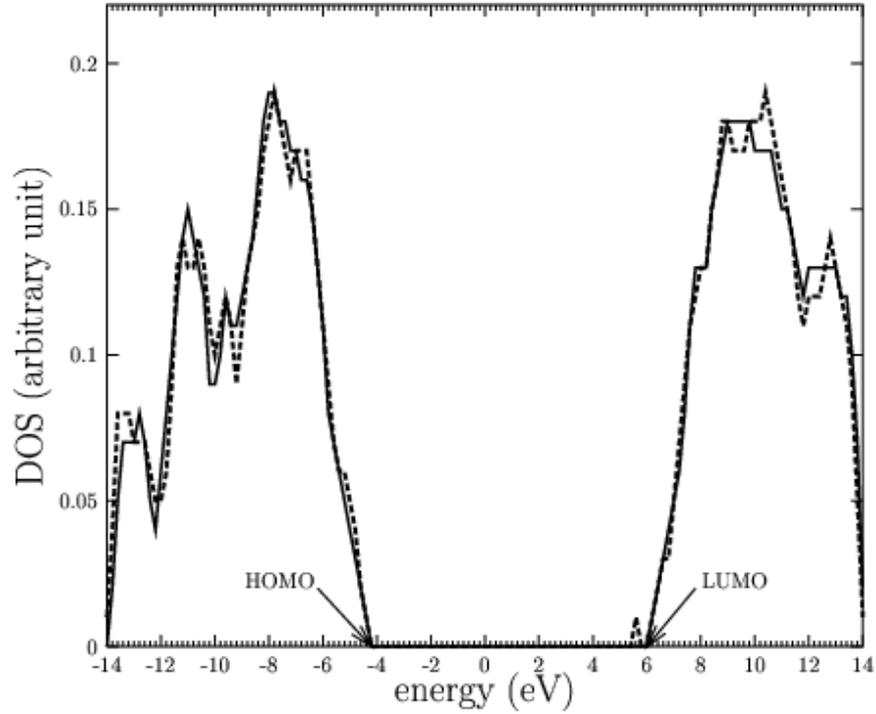
**FIG. 4.6.** (Cont.)

(SAsmod1-SAsmod2) and bridged models obtained by optimization of BBAsmod1-BBAsmod2 and IAsmod1-IAsmod3 structures can be obtained on the stepped Ge(100) surface by adjusting the laboratory conditions. On the other hand the binding energy of As in SAsmod3 is found to be highly lower than that of the most probable adsorption models on the step-down and step-up terraces. Therefore As atoms can diffuse through the layers in the laboratory conditions and occupy the empty sites of the stepped Ge(100) surface.

**TABLE 4.6.** The structural parameters, the total energy, and the binding energy of As, for the optimized diffusion models of As atom on stepped Ge(100) surface.

Model	Bond length (Å <sup>o</sup> )		Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	As-Ge	Dimer Ge-Ge			
BBAsmod1	2.34(up) 2.43(back)	---	---	-371612.8873	-7.311
BBAsmod2	2.34(up) 2.43(back)	---	---	-371612.7689	-4.087
SAsmod1	2.45 (dimer ) 2.45 (back)	---	0.9	-369560.8856	-3.843
SAsmod2	2.46(dimer) 2.45(back)	---	2	-369560.8951	-6.902
SAsmod3	2.48	---	---	-369560.6993	-14.509
IAsmod1	2.28	2.43	7.5	-371612.8111	-5.238
IAsmod2	2.33	2.39	14	-371612.9523	-9.080
IAsmod3	2.38	---	---	-371612.9135	-8.022

In the present work, the density of states (DOS) of optimized SAsmod3 is plotted in Fig. 4.7 for the states around the highest occupied molecular orbitals (HOMO) and the lowest unoccupied molecular orbitals (LUMO) of the stepped Ge(100) surface. The DOS of stepped Ge(100) surface based on single point total energy calculations is also included to Fig. 4.7 for comparison. Both profiles seeing in Fig. 4.7 are generated by Gaussian broadening technique with broadening of 0.2eV. This broadening level is found to be sufficient to observe the features around the HOMO and LUMO clearly. Since all the dangling bonds of the stepped Ge(100) surfaces with and without As atom are passivated by H atoms the energy separation between the LUMO and HOMO can be seen obviously. The energy separation between LUMO and HUMO corresponds to the optical gap between the conduction and valance band of bulk Ge. Since the stepped Ge(100) surfaces with and without As



**FIG. 4.7.** DOS of optimized stepped Ge(100) surface models with (dotted line) and without (solid line) As atom.

atom are modeled as clusters (not periodic structure) the energy difference between LUMO and HOMO ( $\sim 10\text{eV}$ ) is much greater than the actual energy gap of bulk Ge ( $0.67\text{eV}$ ) structure. As it is well known in the literature, the energy gap between LUMO and HOMO increases when the size of the cluster is decreased [66, 67]. Fig 4.7 illustrates the effect of As atom on DOS of stepped Ge(100) surface obviously. The DOS calculations of stepped Ge(100) surface have given an empty energy range between the HOMO and LUMO edges, but the same calculations on the stepped Ge(100) surface with a substitutional As atom (SAsmod3 model) have presented a feature at about  $5.5\text{eV}$ . Therefore the substitutional As atom initiates the doping process of stepped Ge(100) surface by giving a feature very close to the LUMO edge. The feature of As states in Fig. 4.7 defines the donor energy level of n-type stepped Ge(100) surface. Since the ratio between the number of As atom and Ge atoms in the SAsmod3 model is just  $1/180$ , the height of the As states is much lower than that of Ge states. The As donor energy level is presently calculated to be  $0.5\text{eV}$  (referenced to LUMO edge) with respect to the reported value of  $12.7\text{meV}$

(referenced to the conduction band edge of bulk Ge) [60]. Since the present calculations have been done with a cluster model instead of a bulk Ge, it is considered to be weak for the determination of the exact value of the donor energy level. But it is found to be able to present the existence of the donor energy level very close to the edge of the LUMO.

#### **4.7 Conclusion**

In the present work, the decomposition steps of arsine molecule on stepped Ge(100) surface have been investigated to determine the reaction paths in the doping process. It is shown that the dissociation of AsH<sub>3</sub> is provided by coming away of H atoms step by step; first AsH<sub>3</sub> molecule adsorbs to a dangling bond of the buckled down Ge atom close to the step edge, then the dissociation steps start and finally AsH<sub>3</sub> reduces to As atom on the stepped Ge(100) surface. It is also presently showed that AsH<sub>3</sub> dissociates into AsH<sub>2</sub>+H directly for certain adsorption models (MAsH<sub>3</sub>mod11, 12, 14 and BasH<sub>3</sub>mod2,3,5) just after the adsorption. Since the direct dissociation of AsH<sub>3</sub> was not identified on the flat Ge(100) surface [68], it is considered to be originated from much coordination of the stepped Ge(100) surface.

In the literature, the arsine-Ge surface systems were considered be important because of the faceting due to etching [26-28]. The steps like facets were determined to be controlled by the laboratory conditions; reducing the temperature, partial pressure and exposure time of AsH<sub>3</sub> the facets can be removed. This experimental outcome shows that faceting is directly related to the decomposition rate of AsH<sub>3</sub> and the desorption rate of Ge atoms from the surface. In Ref. [28] the etching of the Ge(100) surface by As atoms were controlled with 2 torr of Tertiarybutylarsine gas flow, 510°C of annealing temperature and 20min of exposure time to have arsenic terminated S<sub>A</sub> type stepped Ge(100) surface like the As adsorbed stepped Ge(100) surface of the present work. Therefore As doped S<sub>A</sub> type Ge(100) surface can be obtained in the laboratory with the step by step dissociation of AsH<sub>3</sub> as it is identified in our work. On the other hand, the substitutional occupation of the stepped Ge(100)

surface by As atom identified in this work for the last step of the dissociation is confirmed by the As concentration of  $1 \times 10^{19}/\text{cm}^3$  measured in As doped Ge(100) surface [26] at 500-700°C. Because this concentration is consistent to the vacancies (irregular vacancies or empty Ge sites) generated in the Ge surface for the temperature range of 500-700°C with the vacancy formation energy of 0.59eV [69]. The occupation of the empty Ge sites by As atoms obtained by the present total energy calculations is also confirmed by the Ge-As dimers observed on the STM images of the As activated  $S_A$  type stepped Ge(100) surface [28]. Therefore As atoms prefer to occupy empty Ge sites instead of interstitial sites of the surface.

## CHAPTER 5

### RESULTS: 2

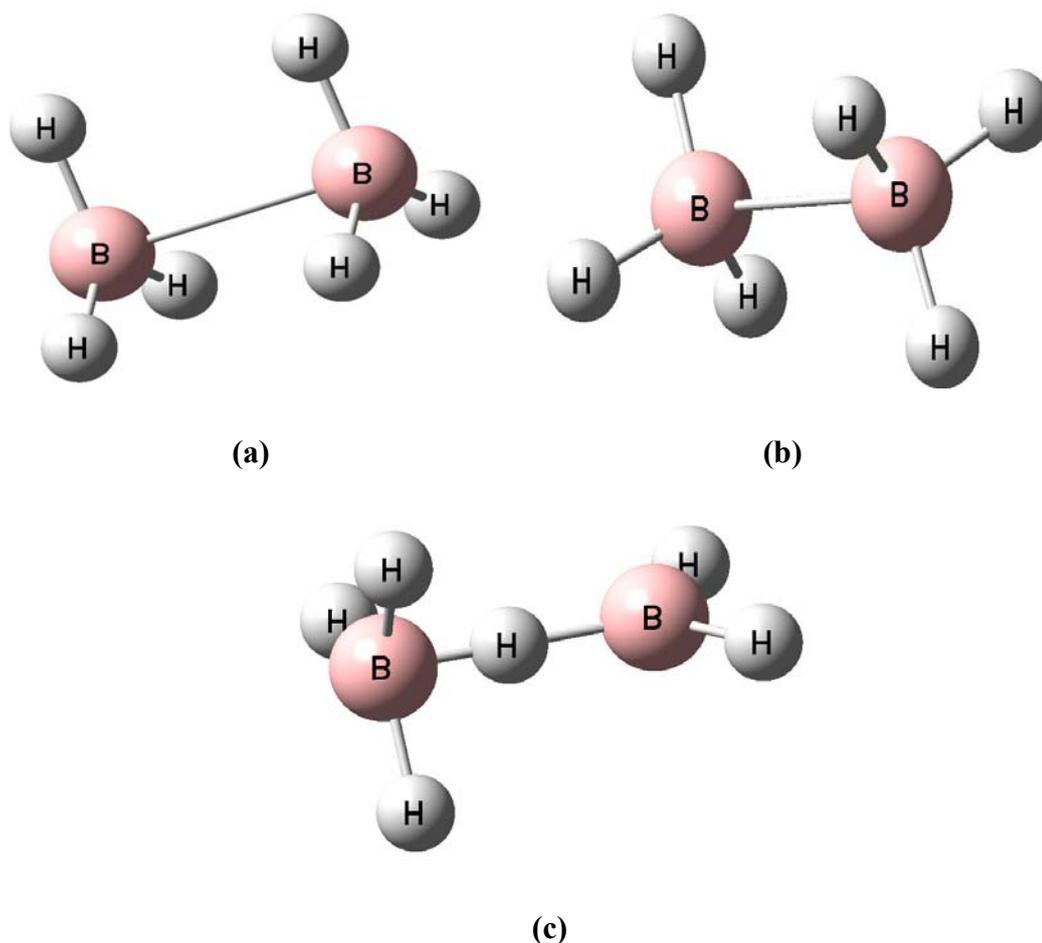
## STEPPED Ge(100) SURFACE EXPOSED TO DIBORANE GAS

### 5.1 Introduction

The diborane gas molecule consists of two  $\text{BH}_3$  molecules. In p-type doping process of stepped Ge(100) surface by diborane gas flow,  $\text{B}_2\text{H}_6$  gas molecules can dissociate into  $\text{BH}_3$ ,  $\text{BH}_2$ ,  $\text{BH}$ , and finally B fragments. In this part of the present work, first the most stable geometry and the decomposition stages of diborane molecule have been examined and then the adsorption of the fragments of  $\text{B}_2\text{H}_6$  on stepped Ge(100) surface have been studied by total energy calculations.

### 5.2 $\text{B}_2\text{H}_6$ molecular models

The two  $\text{BH}_3$  molecules in  $\text{B}_2\text{H}_6$  can bond to each other through either Boron or Hydrogen atoms. In the present work, three  $\text{B}_2\text{H}_6$  molecular models are considered. In one of the bonding model, two planar  $\text{BH}_3$  molecules with  $\text{D}_{3h}$  trigonal symmetry can bond to each other through the B-B bond. The two  $\text{BH}_3$  molecules of this model are coincided when  $\text{B}_2\text{H}_6$  is observed along B-B bond. In another bonding model, the  $\text{BH}_3$  molecules in  $\text{C}_{3v}$  symmetry are also connected to each other through the B-B bond. The dihedral angle ( $\text{HB}^{\wedge}\text{BH}$ ) between the B-H bonds of  $\text{BH}_3$  molecules is  $180^\circ$ . Therefore, the two  $\text{BH}_3$  molecules are not coincided along the B-B bond. In other possible bonding model, the first  $\text{BH}_3$  molecule is attached to the second one through one of the H atom of the second  $\text{BH}_3$  molecule. The planes of the  $\text{BH}_3$

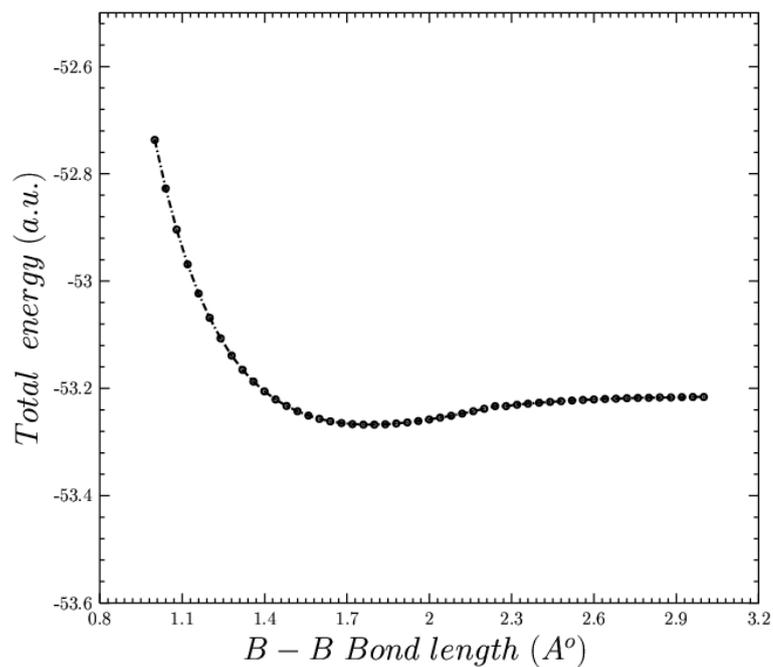


**FIG. 5.1.** The possible bonding models of  $BH_3$  in  $B_2H_6$  structure.

molecules both in  $D_{3h}$  symmetry are perpendicular to each other. The possible bonding models of  $BH_3$  in  $B_2H_6$  structure are pictured in Fig. 5.1. The length of B-B and B-H bonds in  $B_2H_6$  models are taken to be  $\sim 1$  and  $\sim 0.6 \text{ \AA}$ , respectively. The present three models are defined with the acronyms of  $M1B_2H_6$ ,  $M2B_2H_6$ , and  $M3B_2H_6$ .

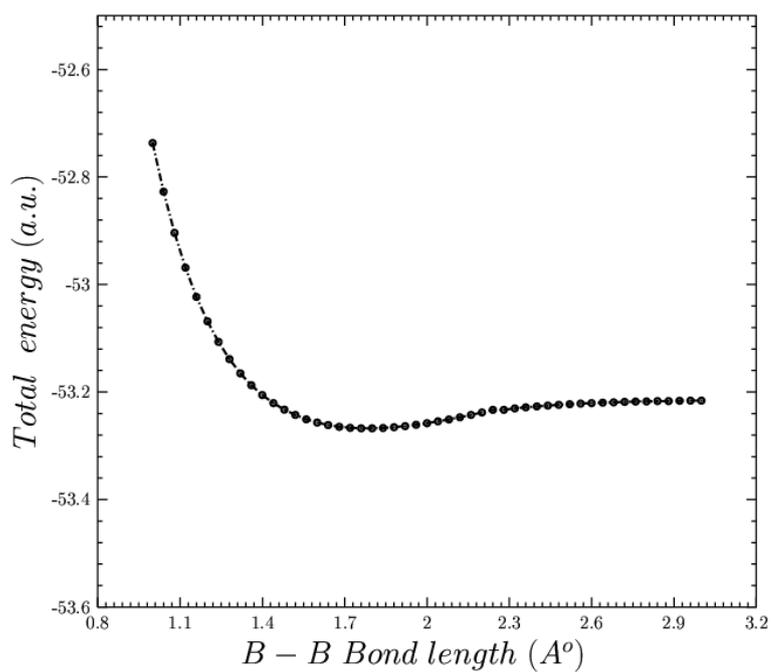
### 5.2.1 Dissociation of $B_2H_6$

In the present work, the initial geometries of  $M1B_2H_6$ ,  $M2B_2H_6$ , and  $M3B_2H_6$  are optimized by total energy calculations. Since the doping of any substrate by B atoms is initiated with the dissociation of diborane gas molecules, the optimization is

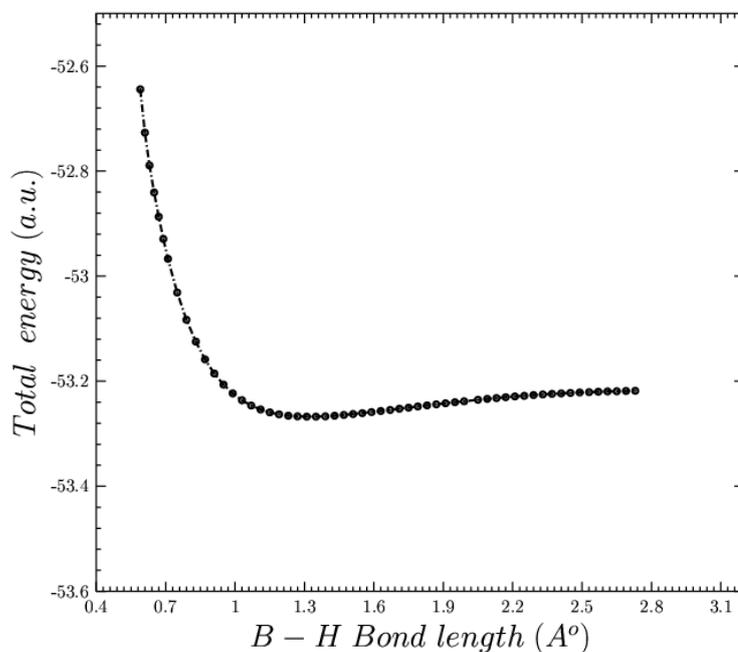


**FIG. 5.2.** The total energy versus B-B bond length for M1B<sub>2</sub>H<sub>6</sub> model.

performed by increasing the length of B-B and B-H bonds in M1B<sub>2</sub>H<sub>6</sub>, M2B<sub>2</sub>H<sub>6</sub>, and M3B<sub>2</sub>H<sub>6</sub> models, respectively. The total energy values are plotted as a function of

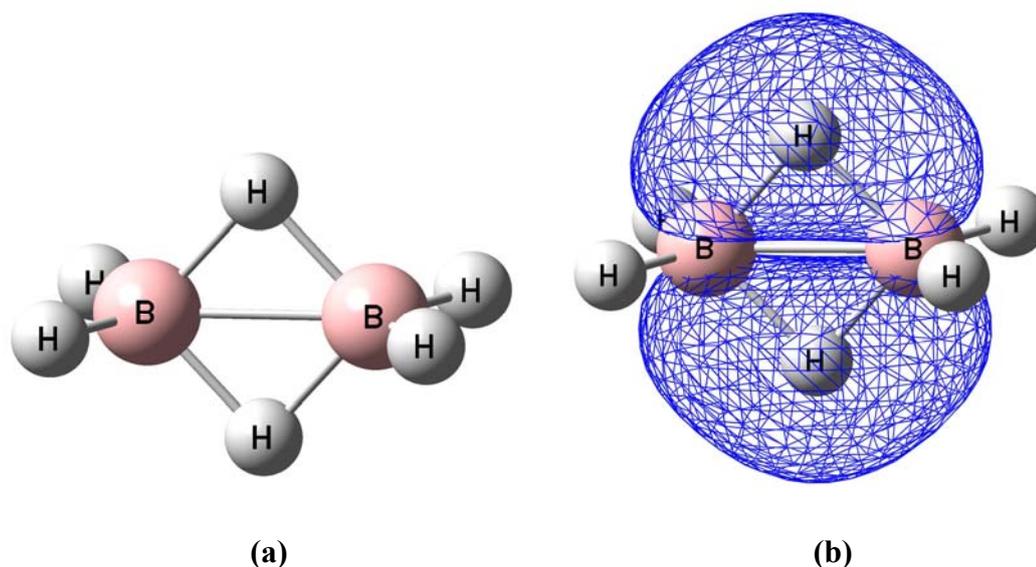


**FIG. 5.3.** The total energy versus B-B bond length for M2B<sub>2</sub>H<sub>6</sub> model.



**FIG. 5.4.** The total energy versus B-H bond length for M3B<sub>2</sub>H<sub>6</sub> model.

B-B and B-H bond lengths in Figs. 5.2, 5.3, and 5.4, for each optimization step of the models. It is found that, all three models have decomposed to two planar BH<sub>3</sub> molecules by elongating the corresponding bond between BH<sub>3</sub> molecules in B<sub>2</sub>H<sub>6</sub> structure. Furthermore the three models of B<sub>2</sub>H<sub>6</sub> molecules are found to be passed through the same optimum structure with the same lowest total energy before the dissociation. Therefore the ground state structure of B<sub>2</sub>H<sub>6</sub> molecule with minimum total energy of -53.30a.u is obtained during the dissociation process. The total energy of the optimized B<sub>2</sub>H<sub>6</sub> structure was reported to be -53.30a.u by Hartree-Fock calculations in Ref. [70]. In the literature, this structure of B<sub>2</sub>H<sub>6</sub> was identified with a pair of chemical bridge bond between B-H-B atoms having geometries look like a banana. The optimum structure of B<sub>2</sub>H<sub>6</sub> contains two types of H atoms; four H atoms of one type make four normal covalent bonds, but the other two H atoms form bridge bonds (banana bonds) between two B atoms. Figs. 5.5 (a) and (b) show the geometry and the pair of banana bonds for the optimized B<sub>2</sub>H<sub>6</sub> structure, respectively. The pair of banana bonds locates in the yz plane perpendicular to the plane of the other four H atoms. Since the banana bonds are formed by the bridge bond involve three atoms (B, H, B) and only two electrons, they are also defined to be three-center-two



**FIG. 5.5.** Geometry and the pair of banana bonds for the optimized  $B_2H_6$  structure.

electron-pair bond. The molecular orbital of  $B_2H_6$  due to the pair of banana bonds consists of  $2p_y$  atomic orbital of boron and  $1s$  atomic orbital of bridge hydrogen atoms. The length of B-H in the banana and normal covalent bond are found to be  $1.315$  and  $1.185\text{\AA}$ , respectively. These bonds were reported to be  $1.316$  and  $1.187\text{\AA}$  in Ref. [70]. Since the chosen basis vectors are different, the present total energy and bond lengths of the optimized  $B_2H_6$  structure are different a little bit with respect to the ones reported in Ref. [70]. In the present work, the necessary external energy ( $E_{\text{ext}}$ ) to dissociate the optimized structure of  $B_2H_6$  is calculated by

$$E_{\text{ext}} = E_{\text{final}} - E_{\text{initial}} \quad (5.1)$$

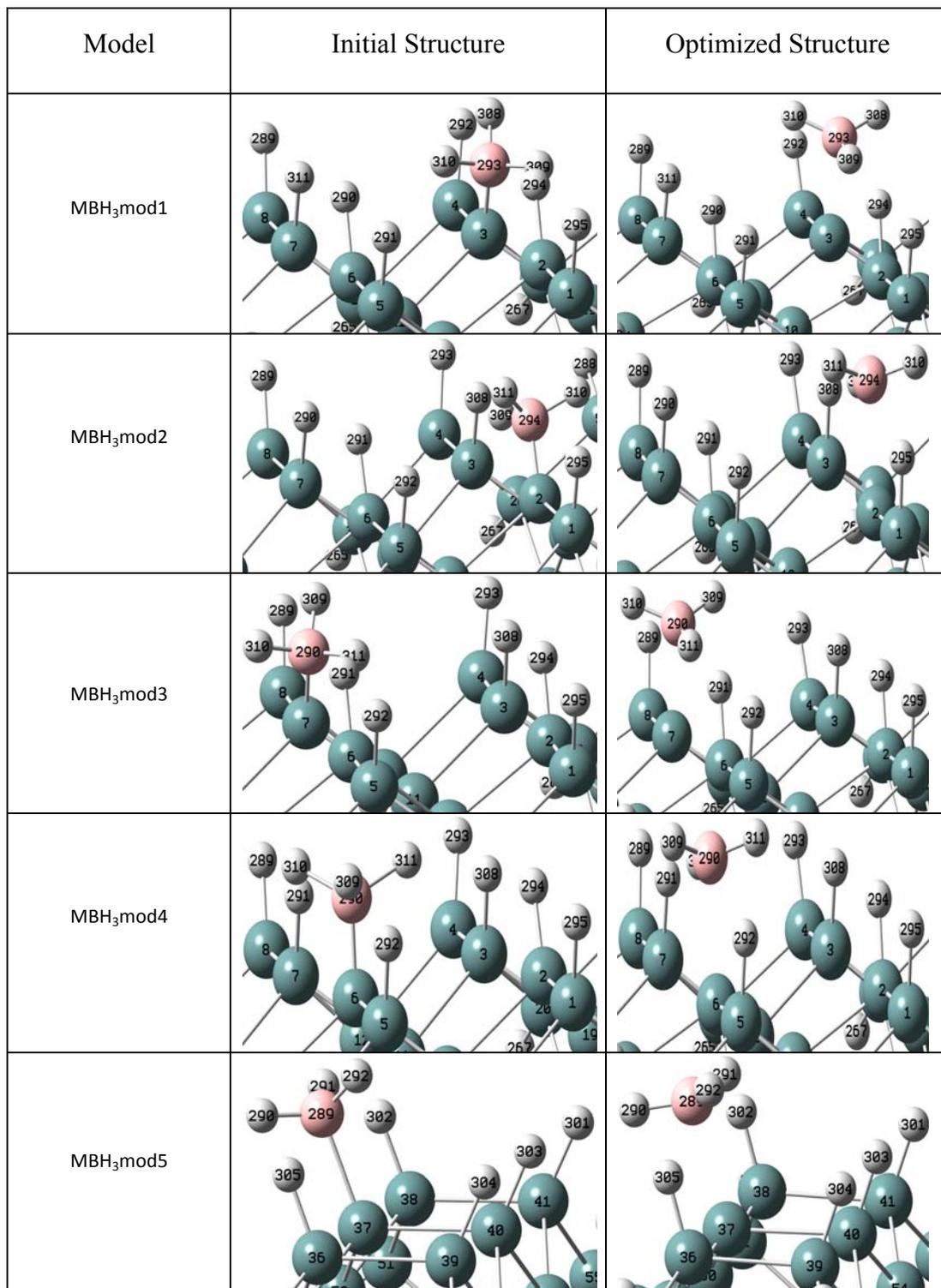
Here,  $E_{\text{final}}$  and  $E_{\text{initial}}$  represent the total energies of the dissociated and initial optimized structures of  $B_2H_6$ , respectively. In the present work, the necessary external energy for the dissociation of  $B_2H_6$  is calculated to be  $\sim 1.3\text{eV}$ . The calculated energy to decompose the  $B_2H_6$  molecule is in agreement with the experimental value of  $26\text{kcal/mol}$  ( $\sim 1.13\text{eV}$ ) [71]. The activation energy for the dissociation of  $B_2H_6$  was also calculated to be  $23\text{-}25\text{kcal/mol}$  ( $1\text{-}1.08\text{eV}$ ) in Ref. [72] by Hartree-Fock method with modified neglect of diatomic overlap (MNDO). In the same experimental work [71], the boron films were synthesized from  $B_2H_6 + \text{He}$  gas structure in CVD method by irradiating the surface with UV-laser light ( $\lambda = 193.6\text{nm}$ ). The present necessary external energy calculated for the dissociation of

$B_2H_6$  into two  $BH_3$  molecules is also found to be reasonable when it is compared with the UV-laser light energy  $\sim 6\text{eV}$  used for the total decomposition of  $B_2H_6$  in Ref. [71]. In the literature, there are certain works in which the external energy to decompose  $B_2H_6$  molecule into two  $BH_3$  molecules was tried to be decreased in the assistance of other media or hydrocarbon solvents [73, 74].

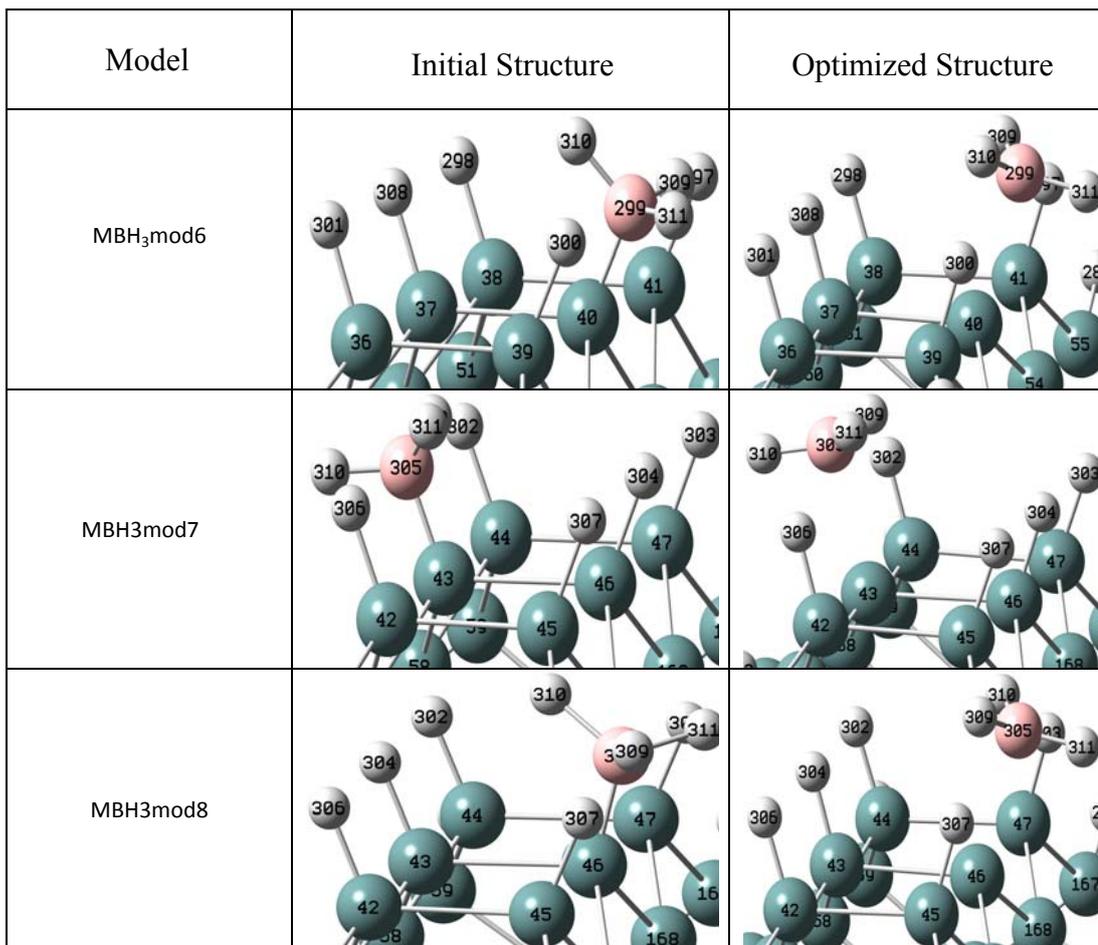
### **5.3 Adsorption of the fragments of $B_2H_6$ on Stepped Ge(100) surface**

#### **5.3.1 Adsorption of $BH_3$ on Stepped Ge(100) surface**

The adsorption of  $BH_3$  molecule on the stepped Ge(100) surface has been investigated by the same models defined in chapter 4. These models are designed again by considering the single and double open surface bonds on  $S_A$  type step-down and step-up terraces. In the first considered adsorption models (MBH<sub>3</sub>mod1-MBH<sub>3</sub>mod8),  $BH_3$  molecule is adsorbed to the step-down (MBH<sub>3</sub>mod1-MBH<sub>3</sub>mod4) and step-up (MBH<sub>3</sub>mod5-MBH<sub>3</sub>mod8) terraces with an open Ge bond taken at the step and close to the step regions. The adsorption of  $BH_3$  on stepped Ge(100) is studied for both buckled-up and buckled-down Ge atoms, separately. The other open bonds of the stepped Ge surface are saturated by H atoms. The adsorption models of  $BH_3$  on stepped Ge surface having single open bond are pictured in Fig. 5.6, by the labels of the surface Ge atoms given in Fig. 3.4. As an example, in MBH<sub>3</sub>mod2 structure,  $BH_3$  molecule is adsorbed to buckled-up side of the dimer bond via second Ge atom when the other surface atoms are totally compensated by H atoms. In the present work, the geometries of the adsorption models are optimized by minimizing their total energies. The optimized structures of MBH<sub>3</sub>mod1-MBH<sub>3</sub>mod8 models are also given in Fig. 5.6. The total energy of each optimized model is listed in Table 5.1. The binding energy of  $BH_3$  in each optimized adsorption model has been also calculated by Eq. (1.1) and tabulated in Table 5.1. The total energy calculations have shown that, the most probable model is MBH<sub>3</sub>mod2 in which  $BH_3$  is initially adsorbed to the buckled up Ge atom at the step region of the step-down terrace. Since the total energies of the naked stepped Ge surfaces (having single open bond at



**FIG. 5.6.** The initial and optimized adsorption models of BH<sub>3</sub> on stepped Ge(100) surface having single open bond.



**FIG. 5.6.** (Cont.)

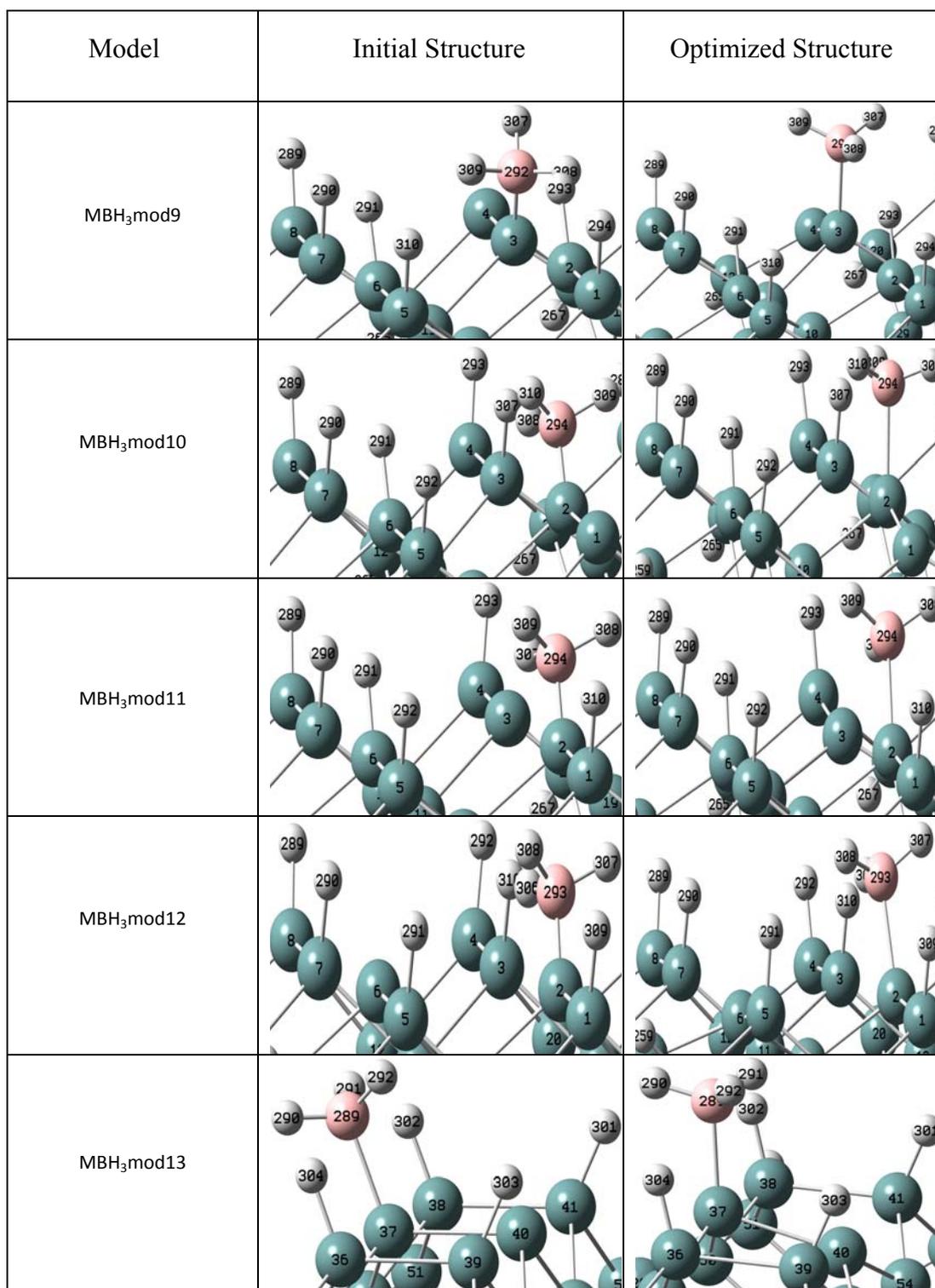
different sites) have found to be the same approximately (-369402.735a.u – (-369402.736a.u)), the most probable adsorption model (MBH<sub>3</sub>mod2) has been also confirmed by the binding energy of BH<sub>3</sub>. The minimum binding energy of BH<sub>3</sub> is calculated to be -3.690eV in MBH<sub>3</sub>mod2 structure. The total energies of the models (Table 5.1) are found to be very close to each other as it is reported before for the same adsorption models of AsH<sub>3</sub>. The maximum energy difference is only ~0.07eV between the step down models (MBH<sub>3</sub>mod1-MBH<sub>3</sub>mod4) in which BH<sub>3</sub> is initially adsorbed to the step or closed to the step regions. The energy difference is only ~0.02eV for the corresponding models (MBH<sub>3</sub>mod5-MBH<sub>3</sub>mod8) of the step-up terrace. On the other hand, the maximum total energy difference between the most probable adsorption model (MBH<sub>3</sub>mod2) and the step up model with highest total

**TABLE 5.1.** The structural parameters, the total energy, and the binding energy of  $\text{BH}_3$ , for the optimized adsorption models of  $\text{BH}_3$  on stepped Ge(100) surface having single open bond.

Model	Bond length ( $\text{\AA}$ )			Tilt angle (degree)	Total Energy (a.u)	Binding Energy (eV)
	Ge-B	B-H	Dimer Ge-Ge			
MBH <sub>3</sub> mod1	2.28	1.16	2.46	0.4	-369428.9406	-3.663
MBH <sub>3</sub> mod2	2.28	1.16	2.50	3.6	-369428.9416	-3.690
MBH <sub>3</sub> mod3	2.29	1.16	2.45	8.8	-369428.9391	-3.631
MBH <sub>3</sub> mod4	2.28	1.16	2.50	3.5	-369428.9407	-3.671
MBH <sub>3</sub> mod5	2.28	1.16	2.48	3.7	-369428.9413	-3.678
MBH <sub>3</sub> mod6	2.28	1.16	2.48	2.6	-369428.9413	-3.675
MBH <sub>3</sub> mod7	2.28	1.16	2.49	3.74	-369428.9414	-3.684
MBH <sub>3</sub> mod8	2.28	1.16	2.49	2.5	-369428.9407	-3.676

energy is found to be only  $\sim 0.02\text{eV}$ . In all adsorption models (MBH<sub>3</sub>mod1-MBH<sub>3</sub>mod8),  $\text{BH}_3$  molecule has been suspended on the open Ge bond after optimization. In most probable adsorption model (MBH<sub>3</sub>mod2),  $\text{BH}_3$  molecule has suspended on the open bond of the second Ge atom with a Ge-B distance of  $2.28\text{\AA}$ . The asymmetric dimer bond structure of the surface is not changed by optimization. The adsorption of  $\text{BH}_3$  on stepped Ge(100) surface with two open bonds has been defined by unbridged MBH<sub>3</sub>mod9-MBH<sub>3</sub>mod14 and bridged BBH<sub>3</sub>mod1-BBH<sub>3</sub>mod5 models. As it is considered in the previous chapter, the two open bonds are considered at the step region for both terraces, because of the total energies of the adsorption models at the step region are found to be lower than these of the others in the group of MBH<sub>3</sub>mod1-MBH<sub>3</sub>mod8 models. The two open surface bonds are either

on the same or adjacent dimer bonds. In MBH<sub>3</sub>mod9-MBH<sub>3</sub>mod14 models, BH<sub>3</sub> molecule is initially adsorbed to one of the open bond when the other bond is open. The two open bonds considered on the step-down and step-up terraces have also allowed the formation of bridged adsorption models (BBH<sub>3</sub>mod1-BBH<sub>3</sub>mod5). In Fig. 5.7, the initial and optimized models correspond to two open dangling bonds of the surface are pictured by the labels of Ge atoms given in Fig. 3.4. The total energies of the optimized bridged and unbridged adsorption models have been also listed in Table 5.2. The optimized unbridged adsorption models (MBH<sub>3</sub>mod9-MBH<sub>3</sub>mod14) have expressed only one kind of structure; when the model has two open bonds on the same or adjacent dimer bond, BH<sub>3</sub> remains on the initial adsorption bond leaving the other bond as open (MBH<sub>3</sub>mod9-MBH<sub>3</sub>mod14). Similarly, in the adsorption model of BBH<sub>3</sub>mod3, BH<sub>3</sub> is adsorbed on one of the open bond after optimization by removing the initial bridge between the adjacent dimers. But in the other bridge adsorption models (BBH<sub>3</sub>mod1, BBH<sub>3</sub>mod2, BBH<sub>3</sub>mod4, BBH<sub>3</sub>mod5), BH<sub>3</sub> breaks the bridge between the surface Ge atoms on the same (BBH<sub>3</sub>mod1, BBH<sub>3</sub>mod4) or adjacent (BBH<sub>3</sub>mod2, BBH<sub>3</sub>mod5) dimers and dissociates into BH<sub>2</sub>+H or BH+H<sub>2</sub>, after optimization. Therefore when BH<sub>3</sub> is adsorbed on stepped Ge (100) surface in the bridge model it will have high probability to be reduced to BH<sub>2</sub> or BH simultaneously. It is found that BH<sub>3</sub> is dissociated into BH directly in BBH<sub>3</sub>mod2 model and two H atoms broken from BH<sub>3</sub> molecule are desorbed from the surface in the form of H<sub>2</sub> molecule. Therefore when the stepped Ge terraces have been exposed to BH<sub>3</sub> gas, BH<sub>3</sub> molecules will be adsorbed to the surface either directly or dissociatively, due to the number and the position of the open bonds. Since the bond structures on the stepped Ge(100) surface are different for each adsorption model considered here, the most probable model is defined by the binding energies (Table 5.2) calculated for the fragments, BH<sub>3</sub>, BH<sub>2</sub>, and BH. The most probable direct adsorption (non dissociative) model of BH<sub>3</sub> (among MBH<sub>3</sub>mod9-MBH<sub>3</sub>mod14 and BBH<sub>3</sub>mod3 models) is obtained by the optimization of MBH<sub>3</sub>mod12 model on the step-down terrace. In optimized MBH<sub>3</sub>mod12 model, BH<sub>3</sub> molecule is bound to the surface with a bond length of 2.06Å and the binding energy of ~ -6eV (Table 5.2). The length and the tilt angle of the dimer bond having BH<sub>3</sub> molecule are found to be 2.52Å and 4.8°, respectively.



**FIG. 5.7.** The initial and optimized adsorption models of BH<sub>3</sub> on stepped Ge correspond to two dangling bonds of the surface.

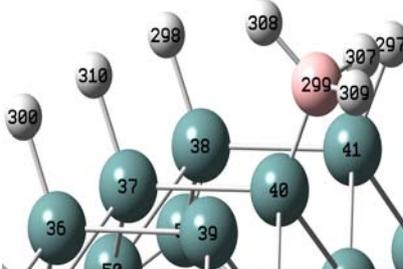
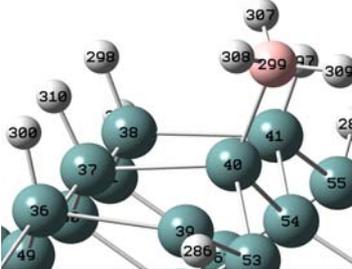
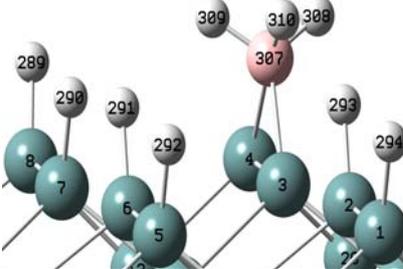
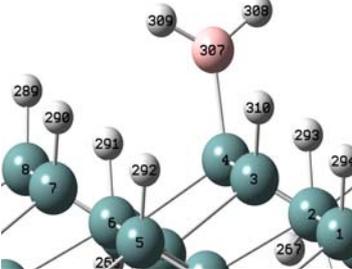
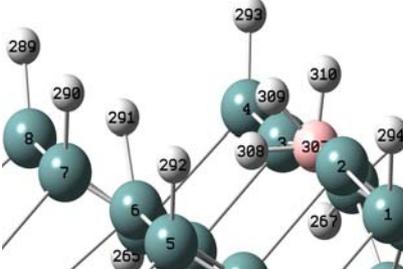
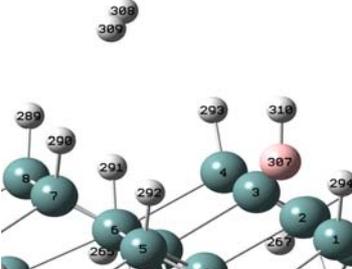
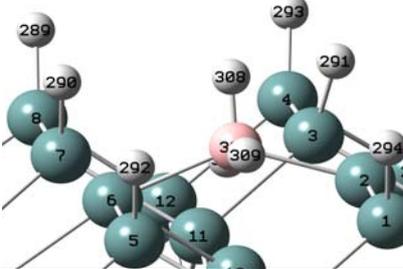
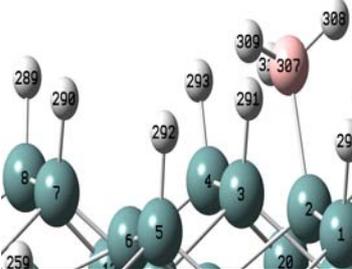
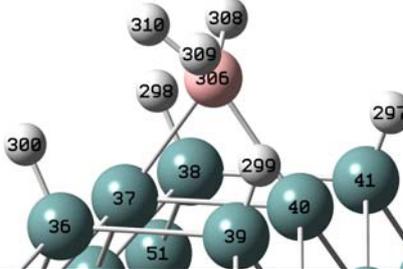
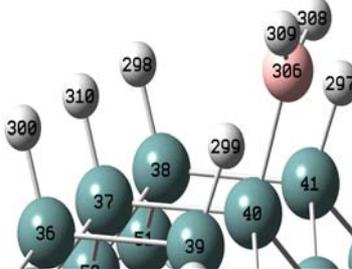
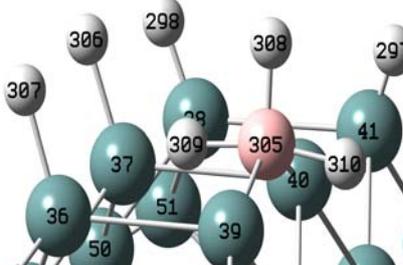
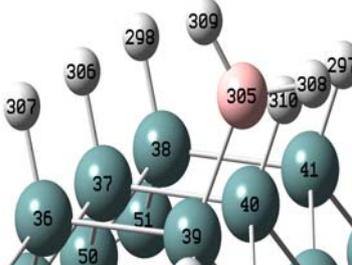
Model	Initial Structure	Optimized Structure
MBH <sub>3</sub> mod14	 <p>Initial structure of MBH<sub>3</sub>mod14 showing a central boron atom (red) coordinated to three methyl groups (teal spheres). The boron atom is labeled 299. Other atoms are labeled with IDs such as 300, 310, 298, 308, 297, 307, 309, 38, 41, 37, 36, 39, 40, 50, 51, 49, 286, 53, 54, 28.</p>	 <p>Optimized structure of MBH<sub>3</sub>mod14 showing the same central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 299. Other atoms are labeled with IDs such as 300, 310, 298, 308, 297, 307, 309, 38, 41, 37, 36, 39, 40, 50, 51, 49, 286, 53, 54, 28.</p>
BBH <sub>3</sub> mod1	 <p>Initial structure of BBH<sub>3</sub>mod1 showing a central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 307. Other atoms are labeled with IDs such as 309, 310, 308, 289, 290, 291, 292, 293, 294, 8, 7, 6, 5, 4, 3, 2, 1, 267, 268.</p>	 <p>Optimized structure of BBH<sub>3</sub>mod1 showing the same central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 307. Other atoms are labeled with IDs such as 309, 310, 308, 289, 290, 291, 292, 293, 294, 8, 7, 6, 5, 4, 3, 2, 1, 267, 268.</p>
BBH <sub>3</sub> mod2	 <p>Initial structure of BBH<sub>3</sub>mod2 showing a central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 307. Other atoms are labeled with IDs such as 293, 309, 310, 289, 290, 291, 292, 294, 8, 7, 6, 5, 4, 3, 2, 1, 267, 268, 308, 309.</p>	 <p>Optimized structure of BBH<sub>3</sub>mod2 showing the same central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 307. Other atoms are labeled with IDs such as 293, 309, 310, 289, 290, 291, 292, 294, 8, 7, 6, 5, 4, 3, 2, 1, 267, 268, 308, 309.</p>
BBH <sub>3</sub> mod3	 <p>Initial structure of BBH<sub>3</sub>mod3 showing a central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 307. Other atoms are labeled with IDs such as 293, 309, 310, 289, 290, 291, 292, 294, 8, 7, 6, 5, 4, 3, 2, 1, 267, 268, 308, 309, 12, 11, 20, 21.</p>	 <p>Optimized structure of BBH<sub>3</sub>mod3 showing the same central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 307. Other atoms are labeled with IDs such as 293, 309, 310, 289, 290, 291, 292, 294, 8, 7, 6, 5, 4, 3, 2, 1, 267, 268, 308, 309, 12, 11, 20, 21.</p>
BBH <sub>3</sub> mod4	 <p>Initial structure of BBH<sub>3</sub>mod4 showing a central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 306. Other atoms are labeled with IDs such as 310, 308, 298, 299, 297, 300, 38, 41, 37, 36, 39, 40, 51, 50, 51, 49, 286, 53, 54, 28.</p>	 <p>Optimized structure of BBH<sub>3</sub>mod4 showing the same central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 306. Other atoms are labeled with IDs such as 310, 308, 298, 299, 297, 300, 38, 41, 37, 36, 39, 40, 51, 50, 51, 49, 286, 53, 54, 28.</p>
BBH <sub>3</sub> mod5	 <p>Initial structure of BBH<sub>3</sub>mod5 showing a central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 305. Other atoms are labeled with IDs such as 298, 308, 297, 307, 309, 310, 38, 41, 37, 36, 39, 40, 51, 50, 51, 49, 286, 53, 54, 28.</p>	 <p>Optimized structure of BBH<sub>3</sub>mod5 showing the same central boron atom (red) coordinated to three methyl groups. The boron atom is labeled 305. Other atoms are labeled with IDs such as 298, 308, 297, 307, 309, 310, 38, 41, 37, 36, 39, 40, 51, 50, 51, 49, 286, 53, 54, 28.</p>

FIG. 5.7. (Cont.)

**TABLE 5.2.** The structural parameters, the total energy, and the binding energy of BH<sub>3</sub> (or BH<sub>2</sub> or BH), for the optimized adsorption models of BH<sub>3</sub> on stepped Ge(100) correspond to two dangling bonds of the surface.

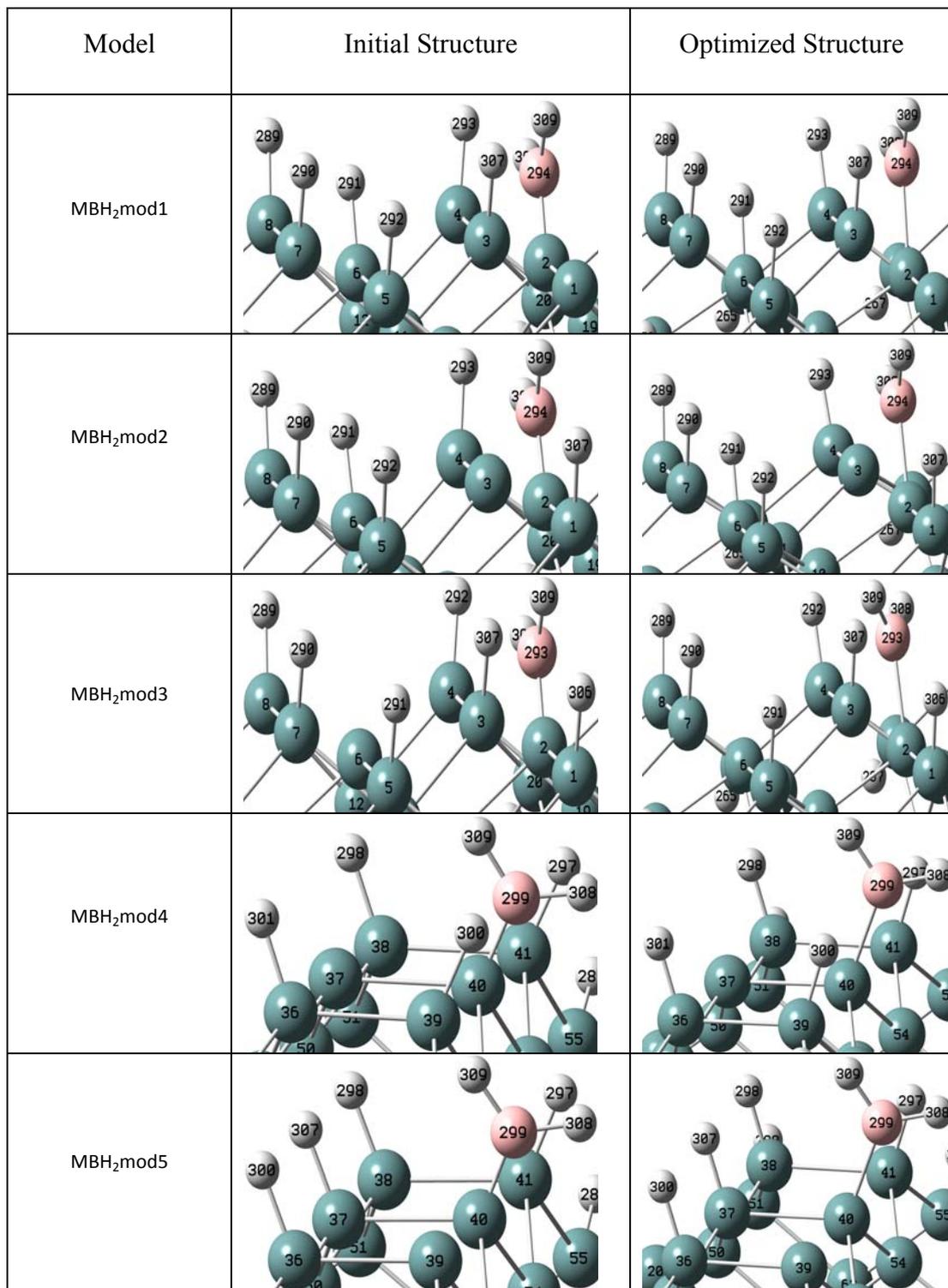
Model	Bond length (Å <sup>o</sup> )			Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-B	B-H	Dimer Ge-Ge			
MBH3mod9	2.07	1.16	2.46	25.0	-369428.3148	-5.635
MBH3mod10	2.06	1.16	2.50	18.0	-369428.3222	-5.839
MBH3mod11	2.06	1.16	2.55	6.7	-369428.2825	-5.488
MBH3mod12	2.06	1.16	2.52	4.8	-369428.2990	-5.935
MBH3mod13	2.06	1.16	2.49	17.5	-369428.3187	-5.785
MBH3mod14	2.06	1.16	2.49	18.7	-369428.3005	-5.462
BBH3mod1	1.97	1.16	2.47	3.4	-369428.4090	-7.170 for BH <sub>2</sub>
BBH3mod2	2.32	1.17	2.86	20.7	-369428.1551	-7.470 for BH
BBH3mod3	2.06	1.17	2.52	4.7	-369428.3032	-6.046
BBH3mod4	1.97	1.16	2.50	1.5	-369428.4044	-7.039 for BH <sub>2</sub>
BBH3mod5	1.97	1.16	2.50	1.9	-369428.4052	-7.060 for BH <sub>2</sub>

The total energies of the models in which BH<sub>3</sub> dissociates into BH<sub>2</sub> and H (BBH<sub>3</sub>mod1, BBH<sub>3</sub>mod4 and BBH<sub>3</sub>mod5) are very close to each other (Table 5.2). Since the structures of the substrates of these models are different, the binding energy of BH<sub>2</sub> in these models are calculated to be different. According to the binding energies given in Table 5.2, the optimized BBH<sub>3</sub>mod1 on the step down terrace is the most probable geometry explaining the BH<sub>2</sub>+H type dissociation. The binding energy of BH<sub>2</sub> in BBH<sub>3</sub>mod1 model is calculated to be -7.170eV (Table 5.2).

In optimized BBH<sub>3</sub>mod1 model, the length and the tilt angle of the dimer bond with BH<sub>2</sub> molecule are found to be 1.97Å<sup>o</sup> and 3.42<sup>o</sup>, respectively. In another dissociative model (BBH<sub>3</sub>mod2), two H atoms are desorbed from the surface and BH is suspended between two Ge atoms on adjacent dimers. In optimized BBH<sub>3</sub>mod2 model, the fragment of BH is suspended to Ge atoms with the binding energy of -7.470eV. Hence at this stage of BH<sub>3</sub> gas exposure, BH<sub>3</sub>, BH<sub>2</sub>, BH, and H will be appeared usually on the stepped Ge surface depending on the positions of the open bonds in front of BH<sub>3</sub> molecules. Besides, if BH<sub>3</sub> molecule decreases to BH directly as in BBH<sub>3</sub>mod2 model, the desorption of H atoms from the surface is provided by the formation of H<sub>2</sub> molecules.

### 5.3.2 Adsorption of BH<sub>2</sub> on Stepped Ge(100) surface

In the next stage, the molecular adsorption of BH<sub>2</sub> on the surface has been confirmed by the optimization of unbridged and bridged adsorption models pictured in Fig 5.8. The total energies of the optimized bridged and unbridged models are tabulated in Table 5.3. It is found that, when BH<sub>2</sub> molecule is adsorbed to one of the two open bonds of Ge(100) surface directly (MBH<sub>2</sub>mod1-MBH<sub>2</sub>mod5), it remains on the initial adsorption bond leaving the other bond as open, after optimization. Similarly, when BH<sub>2</sub> makes a bridge between the open bonds on the adjacent dimers, it breaks the bridge after optimization and bond to one of the open bond leaving the other bond as open (BBH<sub>2</sub>mod2, BBH<sub>2</sub>mod3, BBH<sub>2</sub>mod5). However in the other optimized bridged models (BBH<sub>2</sub>mod1, BBH<sub>2</sub>mod4), BH<sub>2</sub> saves its initial position, i.e, makes a bridge between two open Ge bonds on the same dimer. This outcomes of the optimized unbridged and bridged models have excluded the spontaneous dissociative adsorption of BH<sub>2</sub> on stepped Ge(100) surface. Since the molecular adsorption of BH<sub>2</sub> is studied directly, the binding energy of BH<sub>2</sub> (Table 5.3) in MBH<sub>2</sub>mod1-MBH<sub>2</sub>mod5 models is ~2-2.7eV lower than those (Table 5.2) in the dissociative adsorption models of BH<sub>3</sub>. The binding energy of BH<sub>2</sub> in MBH<sub>2</sub>mod1-MBH<sub>2</sub>mod5 models are also comparable with the ones calculated for the optimized BBH<sub>2</sub>mod2, BBH<sub>2</sub>mod3, and BBH<sub>2</sub>mod5 models. Since the open bond structures of the optimized unbridged (MBH<sub>2</sub>mod1-MBH<sub>2</sub>mod5) and bridged (BBH<sub>2</sub>mod1-BBH<sub>2</sub>mod5) models are completely different, the most probable geometry for the



**FIG. 5.8.** The initial and optimized adsorption models of BH<sub>2</sub> on stepped Ge(100) surface.

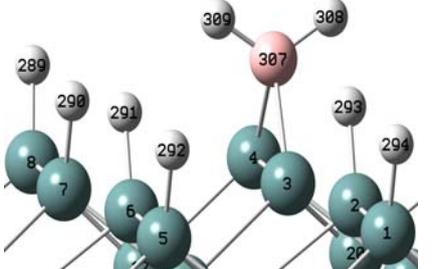
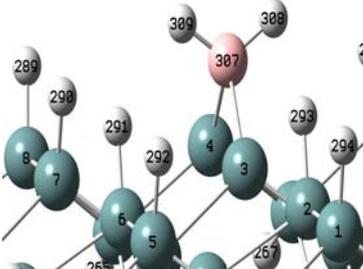
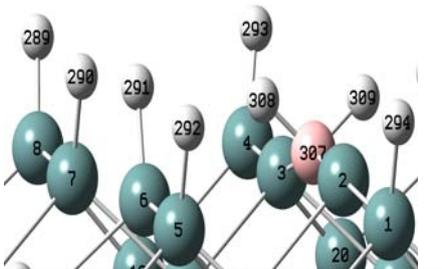
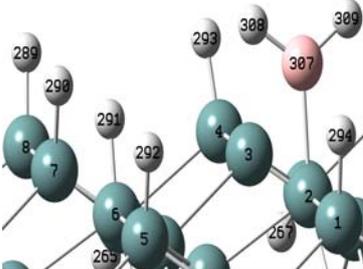
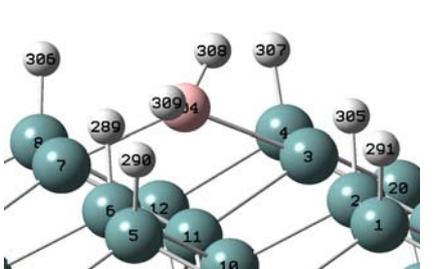
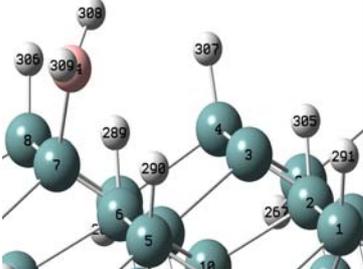
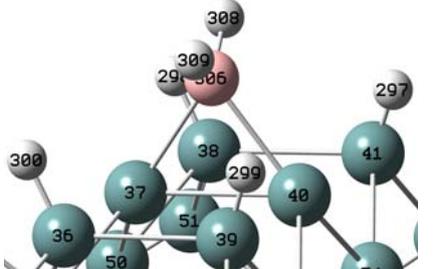
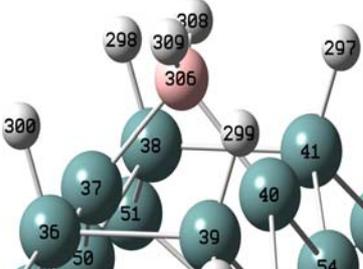
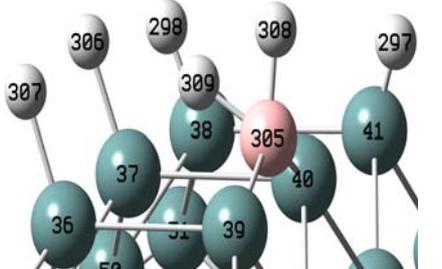
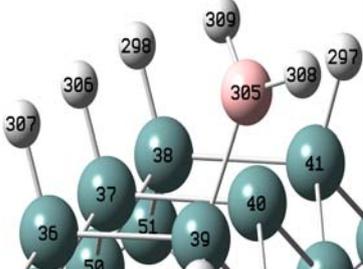
Model	Initial Structure	Optimized Structure
BBH <sub>2</sub> mod1	 <p>Initial structure of BBH<sub>2</sub>mod1 showing a central red atom (307) bonded to two grey atoms (308, 309) and a network of teal atoms (1-8, 20, 21, 22, 23, 24, 25, 26, 27).</p>	 <p>Optimized structure of BBH<sub>2</sub>mod1 showing the central red atom (307) and grey atoms (308, 309) in a different orientation relative to the teal network.</p>
BBH <sub>2</sub> mod2	 <p>Initial structure of BBH<sub>2</sub>mod2 showing a central red atom (307) bonded to two grey atoms (308, 309) and a network of teal atoms (1-8, 20, 21, 22, 23, 24, 25, 26, 27).</p>	 <p>Optimized structure of BBH<sub>2</sub>mod2 showing the central red atom (307) and grey atoms (308, 309) in a different orientation relative to the teal network.</p>
BBH <sub>2</sub> mod3	 <p>Initial structure of BBH<sub>2</sub>mod3 showing a central red atom (307) bonded to two grey atoms (308, 309) and a network of teal atoms (1-12, 20, 21, 22, 23, 24, 25, 26, 27).</p>	 <p>Optimized structure of BBH<sub>2</sub>mod3 showing the central red atom (307) and grey atoms (308, 309) in a different orientation relative to the teal network.</p>
BBH <sub>2</sub> mod4	 <p>Initial structure of BBH<sub>2</sub>mod4 showing a central red atom (306) bonded to two grey atoms (308, 309) and a network of teal atoms (36, 37, 38, 39, 40, 41, 49, 50, 51, 52, 53, 54).</p>	 <p>Optimized structure of BBH<sub>2</sub>mod4 showing the central red atom (306) and grey atoms (308, 309) in a different orientation relative to the teal network.</p>
BBH <sub>2</sub> mod5	 <p>Initial structure of BBH<sub>2</sub>mod5 showing a central red atom (305) bonded to two grey atoms (308, 309) and a network of teal atoms (36, 37, 38, 39, 40, 41, 49, 50, 51, 52, 53, 54).</p>	 <p>Optimized structure of BBH<sub>2</sub>mod5 showing the central red atom (305) and grey atoms (308, 309) in a different orientation relative to the teal network.</p>

FIG. 5.8. (Cont.)

**TABLE 5.3.** The structural parameters, the total energy, and the binding energy of BH<sub>2</sub>, for the optimized adsorption models of AsH<sub>2</sub> on stepped Ge(100) surface.

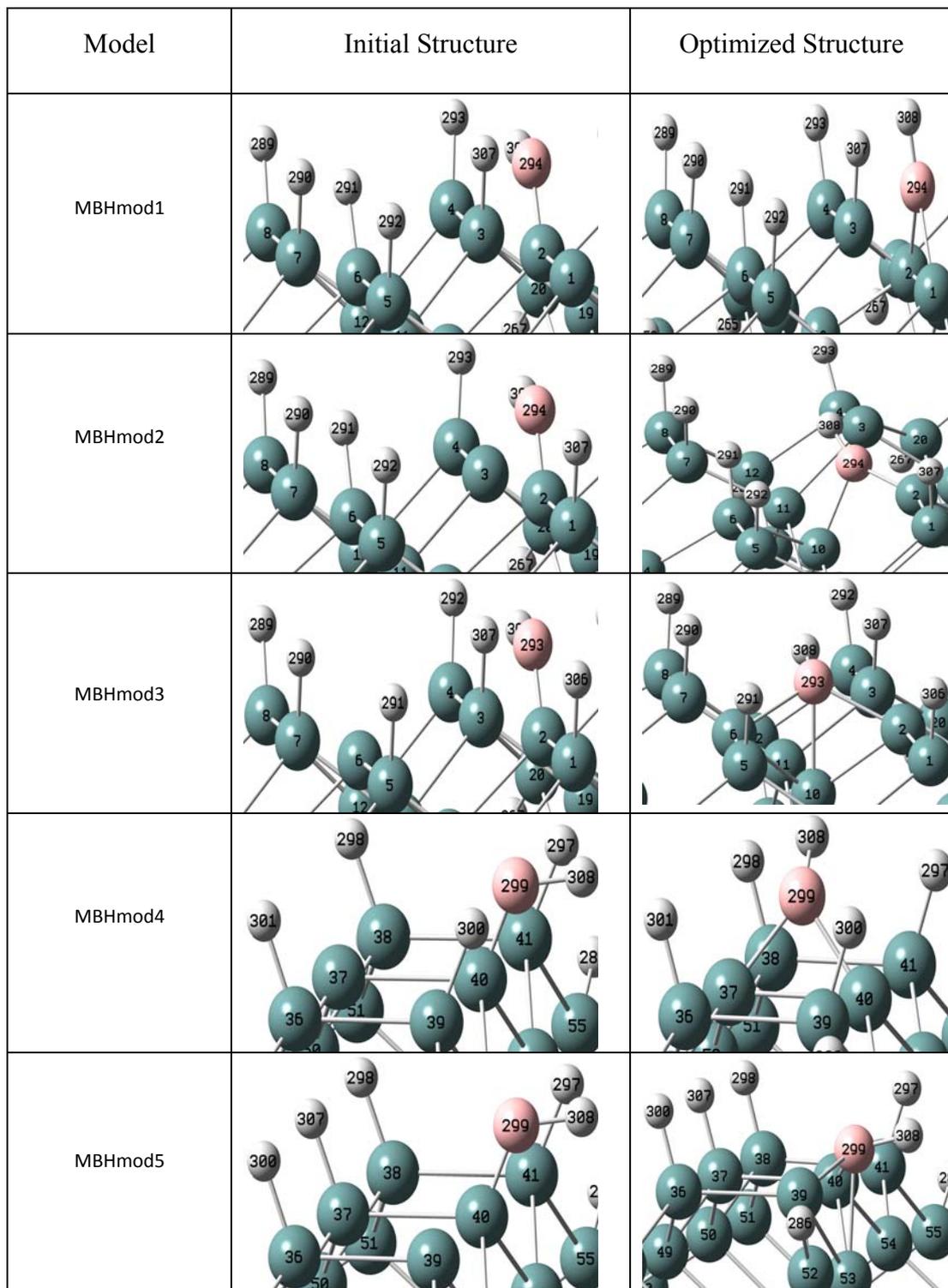
Model	Bond length (Å)			Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-B	B-H	Dimer Ge-Ge			
MBH2mod1	1.97	1.16	2.50	1.1	-369427.7777	-8.990
MBH2mod2	1.97	1.16	2.50	0.6	-369427.7780	-9.731
MBH2mod3	1.97	1.16	2.47	4.7	-369427.7781	-9.731
MBH2mod4	1.97	1.16	2.48	1.9	-369427.7782	-9.045
MBH2mod5	1.97	1.16	2.49	1.4	-369427.7778	-9.212
BBH2mod1	2.0	1.15	2.74	4.6	-369427.7781	-9.007
BBH2mod2	1.97	1.16	2.52	0.7	-369427.7778	-9.728
BBH2mod3	1.97	1.16	2.47	4.7	-369427.7828	-9.859
BBH2mod4	2.0	1.15	2.79	0.7	-369427.7756	-8.977
BBH2mod5	1.97	1.16	2.50	1.5	-369427.7786	-9.231

adsorption of BH<sub>2</sub> on stepped Ge(100) surface is determined by comparing the binding energy values given in Table 5.3. The most probable adsorption model is found to be BBH<sub>2</sub>mod3 in which BH<sub>2</sub> is adsorbed to the step down with the binding energy of -9.859eV. In optimized BBH<sub>2</sub>mod3 model, BH<sub>2</sub> is bounded to the surface with a bond length of 1.97Å. The length and tilt angle of the dimer bond having BH<sub>2</sub> molecule is 2.47Å and 4.7°, respectively.

### 5.3.3 Adsorption of BH on Stepped Ge(100) surface

In the laboratory conditions, the adsorption of  $\text{BH}_2$  molecule on stepped Ge(100) surface has been expected to be followed by the adsorption of BH molecule when one of the H atoms of  $\text{BH}_2$  has formed  $\text{H}_2$  molecule with an adjacent H atom and desorbed from the surface. At this stage, the surface H atoms remained by the dissociation of  $\text{BH}_3$  (as  $\text{BH}_2+\text{H}$  or  $\text{BH}+\text{H}+\text{H}$ ) make the built up of  $\text{H}_2$  molecules possible.

In the present work, the adsorption of BH on stepped Ge(100) surface has been modeled again by unbridged (MBHmod1-MBHmod5) and bridged (BBHmod1-BBHmod5) models on the step-down and step-up terraces. The initial and optimized adsorption models of BH are totally pictured in Fig. 5.9 by the labels of the surface Ge atoms. In unbridged models, two open bonds are considered either on the same or adjacent dimer bonds. As it is explained for AsH in the previous chapter, BH molecule adsorbed to one of the open bonds when the other bond is open. In bridged models, BH fragment makes a bridge between the surface Ge atoms either on the same or adjacent dimer bonds. It is found that BH in all optimized unbridged (MBHmod1-MBHmod5) and bridged (BBHmod1-BBHmod5) models has a tendency to make a bridge between two surface Ge. The tendency of BH to make a bridge between the surface Ge atoms is also noticed before in the spontaneous dissociation process of  $\text{BH}_3$  on the surface of BBH<sub>3</sub>mod2 (Fig. 5.7) model. According to the binding energies given in Table 5.4, the most probable adsorption models are obtained when BH makes a bridge between the surface Ge atoms on the same dimer bond of the step-down (BBHmod1) and step-up (BBHmod4) terraces. In optimized structures of these models, BH is bonded to two surface Ge atoms with a bond length of  $1.85\text{\AA}$  and the binding energy of  $\sim -10$  eV. The optimized bridged models, BBHmod2, BBHmod3, and BBHmod5, have also indicated that BH can make a bridge between the adjacent dimers on the same or different dimer rows.



**FIG. 5.9.** The initial and optimized adsorption models of BH on stepped Ge(100) surface.

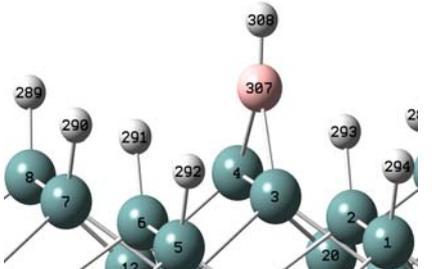
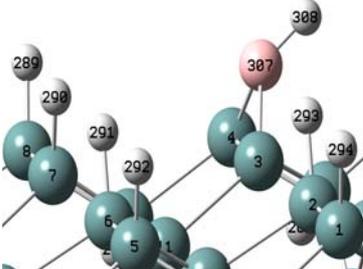
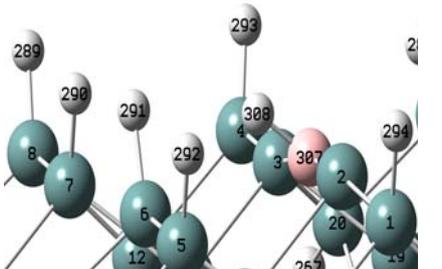
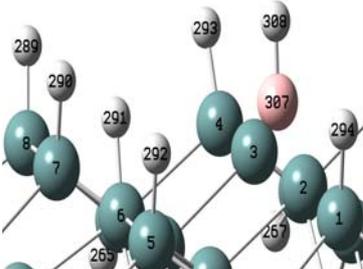
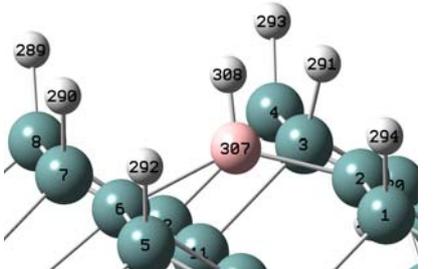
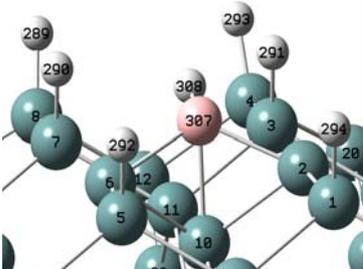
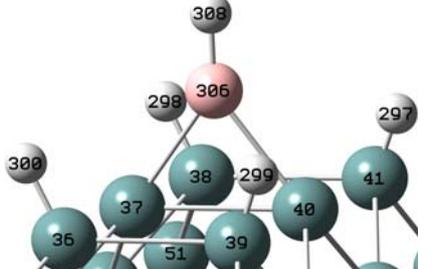
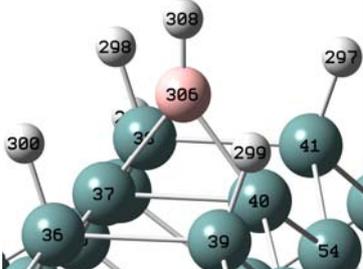
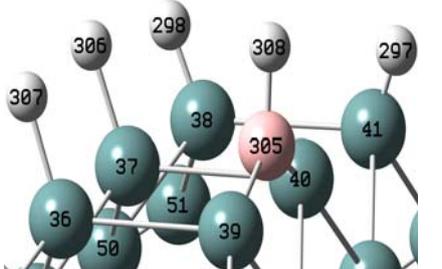
Model	Initial Structure	Optimized Structure
BBHmod1	 <p>Initial structure of BBHmod1 showing a central red atom (307) bonded to a grey atom (308) and several teal atoms (1-12). Other atoms are numbered 289, 290, 291, 292, 293, 294.</p>	 <p>Optimized structure of BBHmod1 showing the central red atom (307) and grey atom (308) in a different orientation relative to the teal atoms (1-12). Other atoms are numbered 289, 290, 291, 292, 293, 294.</p>
BBHmod2	 <p>Initial structure of BBHmod2 showing a central red atom (307) bonded to a grey atom (308) and several teal atoms (1-12). Other atoms are numbered 289, 290, 291, 292, 293, 294.</p>	 <p>Optimized structure of BBHmod2 showing the central red atom (307) and grey atom (308) in a different orientation relative to the teal atoms (1-12). Other atoms are numbered 289, 290, 291, 292, 293, 294.</p>
BBHmod3	 <p>Initial structure of BBHmod3 showing a central red atom (307) bonded to a grey atom (308) and several teal atoms (1-12). Other atoms are numbered 289, 290, 291, 292, 293, 294.</p>	 <p>Optimized structure of BBHmod3 showing the central red atom (307) and grey atom (308) in a different orientation relative to the teal atoms (1-12). Other atoms are numbered 289, 290, 291, 292, 293, 294.</p>
BBHmod4	 <p>Initial structure of BBHmod4 showing a central red atom (306) bonded to a grey atom (308) and several teal atoms (35-41). Other atoms are numbered 297, 298, 299, 300.</p>	 <p>Optimized structure of BBHmod4 showing the central red atom (306) and grey atom (308) in a different orientation relative to the teal atoms (35-41). Other atoms are numbered 297, 298, 299, 300.</p>
BBHmod5	 <p>Initial structure of BBHmod5 showing a central red atom (305) bonded to a grey atom (308) and several teal atoms (35-41). Other atoms are numbered 297, 298, 306, 307.</p>	 <p>Optimized structure of BBHmod5 showing the central red atom (305) and grey atom (308) in a different orientation relative to the teal atoms (35-41). Other atoms are numbered 297, 298, 306, 307.</p>

FIG. 5.9. (Cont.)

**TABLE 5.4.** The structural parameters, the total energy, and the binding energy of BH for the optimized adsorption models of BH on stepped Ge(100) surface.

Model	Bond length (Å)			Tilt angle (degree)	Total Energy (a.u.)	Binding Energy (eV)
	Ge-B	B-H	Dimer Ge-Ge			
MBHmod1	1.94	1.16	2.36	0.4	-369427.1546	-9.924
MBHmod2	1.88	1.16	2.46	14.3	-369427.0218	-7.042
MBHmod3	2.09	1.16	2.49	9.7	-369427.1150	-9.573
MBHmod4	1.87	1.16	2.46	0.7	-369427.1532	-9.924
MBHmod5	2.08	1.16	2.47	8.7	-369427.1418	-9.790
BBHmod1	1.85	1.16	2.48	4.2	-369427.1610	-10.098
BBHmod2	2.32	1.17	2.86	20.7	-369427.0376	-7.470
BBHmod3	2.08	1.16	2.48	9.48	-369427.1192	-9.684
BBHmod4	1.94	1.1	2.35	0.5	-369427.1531	-9.924
BBHmod5	2.15	1.17	2.51	10.1	-369427.1031	-8.739

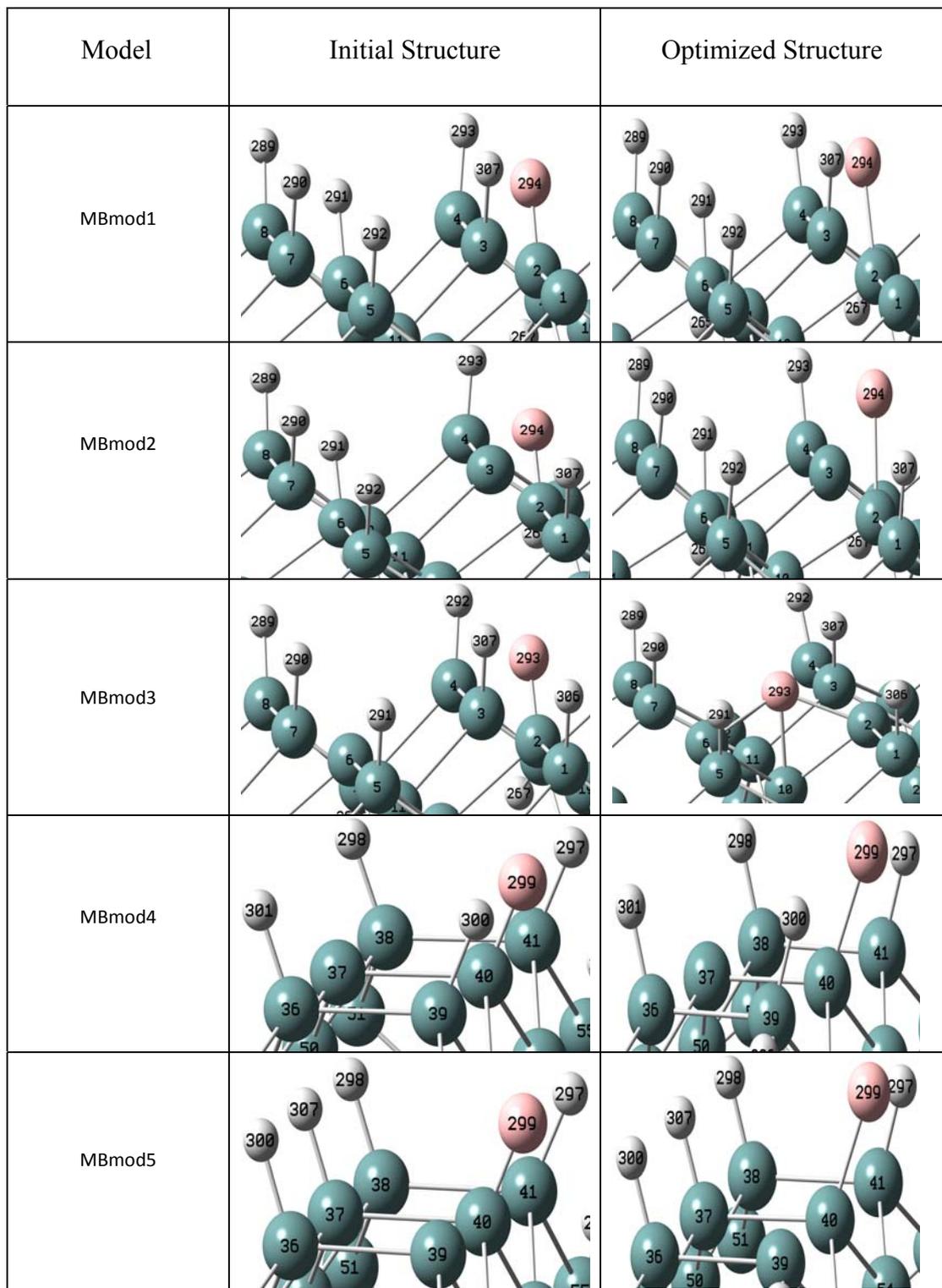
### 5.3.4 Adsorption of B atom on Stepped Ge(100) surface

In the next stage of the doping process of stepped Ge(100) sample, BH<sub>3</sub> molecule of the Borane gas is expected to be reduced to B atom by



reaction. As it is considered in the previous chapter, H<sub>2</sub> molecule built up by H atom of BH fragment and one of the adjacent surface H atom has been desorbed from the surface. The atomic adsorption of B has been examined by again unbridged

(MBmod1-MBmod5) and bridged (BBmod1-BBmod5) models. It is examined whether the bridge model of BH (Fig. 5.9) is broken or not during the desorption of H<sub>2</sub> from the surface. The initial and optimized adsorption models are pictured in Fig. 5.10, and their total energies are given in Table 5.5. It is found that the direct adsorption of B on step-down and step-up terraces is not changed after optimization for unbridged models (MBmod1-MBmod5). In all these models, Boron atom is remained on one of the open bond. It is also found that, the bridge structure in BBmod1-BBmod5 models are not changed after optimization. In optimized bridged models, B atom prefers to make a bridge between two Ge surface atoms either on the same or adjacent dimers. Since the bond structures of the substrates are different, the most probable model for the adsorption of B is determined by taking the binding energy of B in these models into account. It is found that the binding energy of B has the most negative value in BBmod1. In optimized BBmod1 model, Boron atom makes a bridge between two step down Ge atoms on the same dimer bond with the binding energy of -8.977eV. In another similar bridged model of the step up terrace (BBmod4), the binding energy of B is calculated to be -8.631eV. These two bridged models indicate that the bridge structure of BH (in the previous stage) on the same dimer (Fig. 5.9) has been saved on both step-down and step-up terraces during the reduction of BH to B. The bridged structure of B on the same dimer bond of the step-down and step up terraces is characterized with the Ge-B bond length of  $\sim 1.76\text{\AA}$  and  $1.94\text{\AA}$ , respectively. The length of the dimer bond in the most probable bridged models of B (BBmod1, BBmod4) is found to be  $2.62\text{\AA}$  and  $2.40\text{\AA}$  for the adsorption on step- down and step- up, respectively. For the same structures, BBmod1 and BBmod4, the tilt angle of the dimer bond having B atom bridge is calculated to be  $4.66^\circ$  and  $0.71^\circ$ , respectively.



**FIG. 5.10.** The initial and optimized adsorption models of B atom on stepped Ge(100) surface.

Model	Initial Structure	Optimized Structure
BBmod1		
BBmod2		
BBmod3		
BBmod4		
BBmod5		

FIG. 5.10. (Cont.)

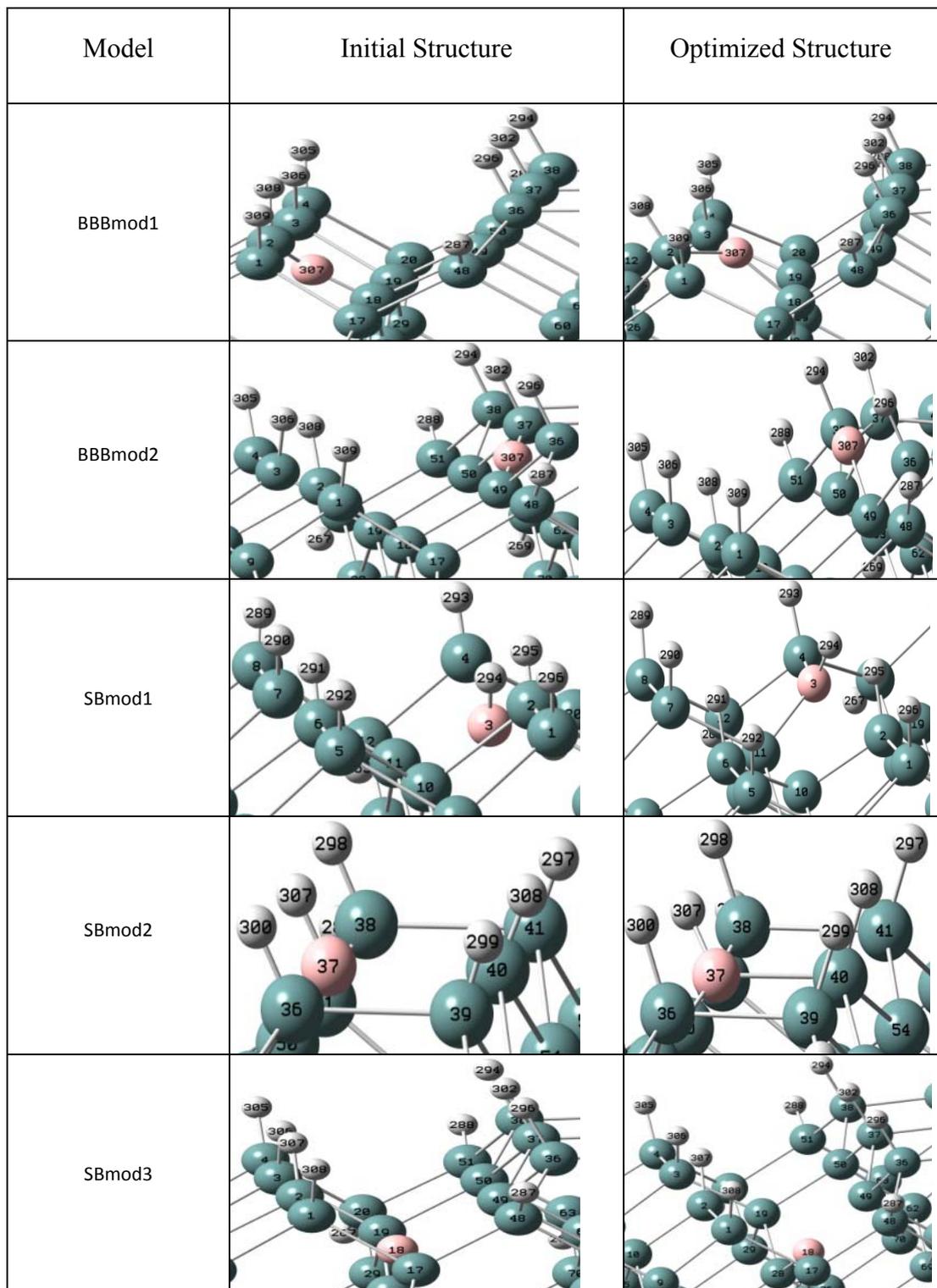
**TABLE 5.5.** The structural parameters, the total energy, and the binding energy of B, for the optimized adsorption models of B on stepped Ge(100) surface.

Model	Bond length (Å)		Tilt angle (degree)	Total Energy (a.u)	Binding Energy (eV)
	Ge-B	Dimer Ge-Ge			
MBmod1	1.93	2.51	1.8	-369426.4733	-7.820
MBmod2	2.09	2.51	0.8	-369426.4588	-8.158
MBmod3	2.06	2.50	9.4	-369426.4683	-8.408
MBmod4	1.92	2.49	2.5	-369426.4736	-7.867
MBmod5	1.92	2.50	2	-369426.4739	-8.053
BBmod1	1.76	2.62	4.7	-369426.5158	-8.977
BBmod2	1.84	3.64	16.6	-369426.4458	-7.801
BBmod3	2.06	2.49	9.2	-369426.4724	-8.522
BBmod4	1.94	2.40	0.7	-369426.5017	-8.631
BBmod5	2.04	2.49	8.2	-369426.4941	-8.602

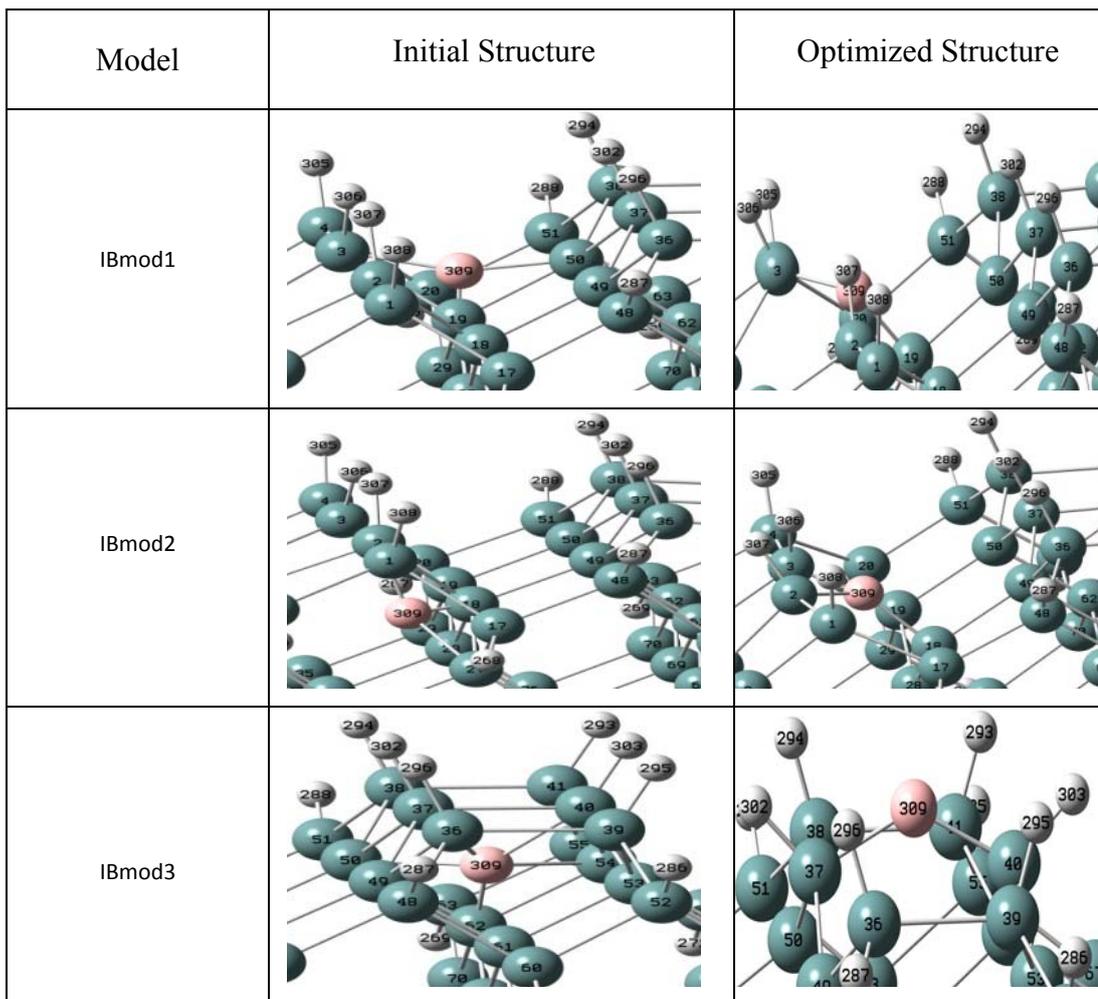
### 5.3.5 Diffusion of B atom through the layers of Stepped Ge(100) surface

At this stage of the present work, the p-type stepped Ge(100) is simulated by the diffusion of the B atoms towards the layers of the surface. As it is considered for the diffusion of As atoms in the previous chapter, during the diffusion, B atoms can have a sit between the surface Ge atoms breaking the Ge-Ge bonds or occupy substitutional or interstitial places of the stepped Ge(100) surface. The setting of B atoms between the surface Ge atoms on the step-down and step-up terraces is defined

by BBBmod1 and BBBmod2 structures, respectively. The initial and optimized geometries of these models are pictured in Fig 5.11. The total energies and the binding energies of the fragments for the optimized models obtained at this stage are given in Table 5.6. It is found that, the optimized BBBmod1 and BBBmod2 models show different structures than the optimized structures of BBAsmo1 and BBAsmo2; in BBBmod1 and BBBmod2 models, B atom makes a bridge between the layers of step-down and step-up terraces, respectively, breaking the Ge-Ge bond. The binding energy of B in BBBmod1 and BBBmod2 structures are calculated to be -6.367 and -6.245eV, respectively (Table 5.6). The other models, SBmod1-SBmod3 and IBmod1-IBmod3, given in Fig. 5.11 have defined the substitutional and interstitial occupation sites of B atoms on the stepped Ge(100) surface, respectively. In SBmod1-SBmod3 models, one site of Ge atom in the layers of the stepped Ge(100) surface is initially occupied by B atom. The main structures of these models are not changed after optimization. The binding energy of B is calculated to be -20.155, -23.116 and -13.080eV in optimized SBmod1-SBmod3 structures, respectively (Table 5.6). It is found that the initial structures of IBmod1-IBmod3 models are changed mainly after optimization. The IBmod1 model in which B atom is interstitially in the valley between the step-down and step-up terraces is converted to a bridge model between the layers of the terraces by optimization (Fig. 5.11). Similarly, the IBmod2 model in which B atom interstitially between the 1<sup>st</sup> and 2<sup>nd</sup> layers of the step-down terrace is changed to a bridge model between the adjacent Ge atoms on the 1<sup>st</sup> and 2<sup>nd</sup> layers of the step-down terrace (Fig. 5.11). It is also found that, the interstitial site of B in IBmod3 has not been saved after optimization. In Optimized IBmod3 structure, B atom has left its interstitial site and gone out from the layers of the surface to make a bridge between the surface Ge atoms on the same dimer. The breakdown of the interstitial models (IBmod1-IBmod3) have indicated that B atoms do not prefer the interstitial sites during the doping process of the stepped Ge(100) surface. The binding energy of B is calculated to be -6.142, -8.552 and -7.031eV (Table 5.6) in optimized IBmod1, IBmod2 and IBmod3 structures, respectively. According to the results given above, the binding energy of B in SBmod1-SBmod3 structures are all more negative with respect to that in all optimized bridged models (BBBmod1-BBBmod2, IBmod1-IBmod3). This outcome



**FIG. 5.11.** The initial and optimized diffusion models of B atom on stepped Ge(100) surface.



**FIG. 5.11.** (Cont.)

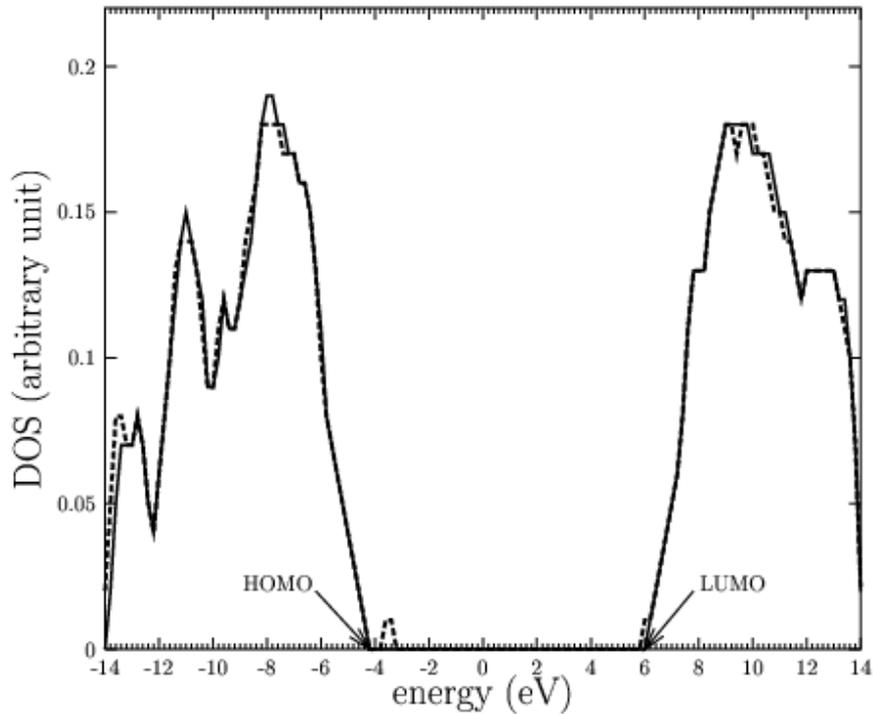
illustrates that, in the adjusted laboratory conditions, B atoms can temporarily make bridge models between the adjacent Ge atoms on the 1<sup>st</sup> and 2<sup>nd</sup> layers of the stepped down terrace, but they permanently prefer the substitutional sites with the most negative binding energies, during the diffusion.

In the present work, the density of states (DOS) of optimized SBmod2 is plotted in Fig. 5.12 for the states around the highest occupied molecular orbitals (HOMO) and lowest unoccupied molecular orbitals (LUMO) of the stepped Ge(100) surface. The DOS of stepped Ge(100) surface based on single point total energy calculations is also included to Fig. 5.12 for comparison. Both profiles seeing in Fig. 5.12 are generated by Gaussian broadening technique with broadening of 0.2eV. This

**TABLE 5.6.** The structural parameters, the total energy, and the binding energy of B, for the optimized diffusion models of B atom on stepped Ge(100) surface.

Model	Bond length (Å <sup>o</sup> )		Tilt angle (degree)	Total Energy (a.u)	Binding Energy (eV)
	Ge-B	Dimer Ge-Ge			
BBBmod1	1.91	2.45	11.2	-369427.8506	-6.367
BBBmod2	1.91	2.43	8.8	-369427.8461	-6.245
SBmod1	2.16(dimer) 2.15(back)	---	21.5	-367375.8912	-20.155
SBmod2	2.14(dimer) 2.13(back)	---	18.8	-367375.8970	-23.116
SBmod3	2.22	---	---	-367375.6449	-13.080
IBmod1	1.91	2.44	14.1	-369427.8423	-6.142
IBmod2	1.92	2.40	9.5	-369427.9309	-8.552
IBmod3	1.97	---	---	-369427.8749	-7.031

broadening level is found to be sufficient to observe the features around HOMO and LUMO clearly. As it is mentioned in chapter IV, the passivation of the all dangling bonds of the stepped Ge(100) surface models with and without B atom provide an obvious energy gap between LUMO and HOMO. This energy gap corresponds to the optical gap between the conduction and valance band of bulk Ge. Since the stepped Ge(100) surface is defined by limited number of Ge atoms in the considered cluster models, the energy difference between LUMO and HUMO (~10eV) is much greater than the actual energy gap of bulk Ge (0.67eV) structure.



**FIG. 5.12.** DOS of optimized stepped Ge(100) surface models with (dotted line) and without (solid line) B atom.

Fig. 5.12 is important to see the effect of B atom on DOS of stepped Ge(100) surface; while the energy range between LUMO and HOMO of stepped Ge(100) surface is empty, a feature located at about  $-3.7\text{eV}$  is obtained by the addition of B atom to the substitutional site of the stepped Ge(100) surface (SBmod2 model). Therefore the substitutional B atom initiates the doping process of stepped Ge(100) surface by giving a feature very close to the HOMO. This feature of B states in Fig. 5.12 defines the acceptor energy level of p-type stepped Ge(100) surface. As it is mentioned in the previous chapter, the small ratio between the number of B atom and Ge atoms in the SBmod2 model ( $1/180$ ) gives a very small B states height with respect to the height of the Ge states. The B acceptor energy level is presently calculated to be  $\sim 0.4\text{eV}$  (referenced to HOMO edge) with respect to the literature value of  $10.4\text{meV}$  (referenced to the valance band edge of bulk Ge) [60]. The present total energy calculations with limited number of cluster atoms point out the existence of B acceptor energy level, but it is found to be insufficient for the determination of the exact energy value of the acceptor level.

## 5.4 Conclusion

In the literature, although a considerable experimental efforts [2, 6, 20-22, 25] have been reported on the growth of p- type flat Ge(100) surface by B<sub>2</sub>H<sub>6</sub> gas flow, as far as the author knows, there isn't any theoretical or experimental work examining the doping of the vicinal (stepped) Ge(100) surface. Because of that, the adsorption and decomposition steps of BH<sub>3</sub> (fragment of B<sub>2</sub>H<sub>6</sub>) obtained in the present work are compared only with the corresponding steps of BH<sub>3</sub> defined experimentally on the growth of p-type flat Ge(100) surface. In these experimental works [2, 6, 20-22, 25], the decomposition steps of B<sub>2</sub>H<sub>6</sub> were not analyzed step by step, but especially in Ref. [21], the doping process was controlled by temperature – programmed desorption spectra (TPD) measurements for different B atom concentrations provided by different fluxes of B<sub>2</sub>H<sub>6</sub> gas source and substrate temperature. The  $\alpha$  peaks ( $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_1^*$ ,  $\alpha_2^*$ ) observed in TPD spectra of this work [21] in the range of (200-350°C) were associated with the desorption of H atoms from the Ge(100) surface. This outcome strongly indicates the dissociation of BH<sub>3</sub> molecules on Ge(100) surface occur by the heat treatment. Moreover, the H peaks of TPD spectra observed at different substrate temperatures illustrate the step by step dissociation as it is determined in the present work. The high probability obtained presently for the first step dissociation of BH<sub>3</sub> into both BH<sub>2</sub>+H and BH+H<sub>2</sub> can be explained by much coordination around the step edge of the stepped Ge(100) to initiate the dissociation. On the other hand, in a very recent work [20], B adsorption on Ge surface was demonstrated to be first increased with increasing B<sub>2</sub>H<sub>6</sub> exposure time at 100°C and finally saturated with concentration of  $6 \times 10^{14}/\text{cm}^2$ . Since the concentration of irregular vacancies (empty Ge sites) in Ge sample is limited, the saturation of B atoms concentration on Ge surface was explained as the adsorption of B atoms at Ge surface sites mainly. The saturation of B atoms concentration on Ge surface was also identified in another recent work [6] at 400°C for different flux of B<sub>2</sub>H<sub>6</sub> gas flow. These two experimental results [6, 20] have confirmed another result of the present work; B atoms prefer to occupy empty Ge sites instead of interstitial sites of the surface.

## CHAPTER 6

### CONCLUSION

In this project, a systematic theoretical study has been introduced on the dissociation paths of arsine ( $\text{AsH}_3$ ) and diborane ( $\text{B}_2\text{H}_6$ ) gas molecules on stepped Ge (100) surface. The arsine and diborane gas structures are widely used n- and p- type dopant sources for Ge, respectively. The determination of the dissociation paths of the dopant fragments might be an important preliminary step to control the doping processes of the substances. It may facilitate to fix the laboratory conditions, such as the flow rates and the pressures of the dopant sources, the temperature and the pressure of the substances.

The doping processes of the stepped Ge (100) surface by  $\text{AsH}_3$  and  $\text{B}_2\text{H}_6$  gas flow have been modeled by the possible adsorption and dissociation models. These models considered for the dissociation paths of the dopant fragments on stepped Ge (100) surface have been simulated by a substrate Ge cluster having (2x1) and (1x2) asymmetric dimerized domains separated by kink free  $S_A$  type step. The most probable adsorption and dissociation models of the  $\text{AsH}_3$  and  $\text{B}_2\text{H}_6$  molecules on stepped Ge (100) surface have been determined by the local minimum energy and /or binding energy calculations based on Hartree-Fock theory.

The total energy calculations have shown that, the step region (both up and down terraces) of the stepped Ge (100) surface has the most attractive sites for the initial stage of the adsorption for  $\text{AsH}_3$  molecules. The adsorption of  $\text{AsH}_3$  molecule on the sites of the up and down terraces of the step has been provided by the molecular

suspension when there is only one dangling bond on the surface. But, when there are at least two open bonds either on the same or different dimers adjacent to each other,  $\text{AsH}_3$  molecule makes an actual bond with the Ge surface; it is adsorbed directly ( $\text{AsH}_3$ ) or dissociatively ( $\text{AsH}_2+\text{H}$ ) to the surface having initially two dangling bonds on the same or adjacent dimers, respectively. This is the common result fixed by the binding energies of the considered models for both up and down terraces of the stepped Ge (100) surface. Since the doping processes have been initialized with the cleaved and cleaned substrate surfaces, all the surface bonds should be considered to be available for adsorption. Therefore both molecular and dissociative adsorptions of  $\text{AsH}_3$  molecule will be possible and the stepped Ge surface will have H atoms in addition to both  $\text{AsH}_3$  and  $\text{AsH}_2$  fragments at the initial stage of the doping process. The same result has been also obtained by the other adsorption models in which  $\text{AsH}_3$  makes a bridge between the dangling bonds;  $\text{AsH}_3$  is adsorbed molecularly and dissociatively on the same and adjacent dimers, respectively breaking the bridge bonds. This outcome has also indicated that  $\text{AsH}_3$  and  $\text{AsH}_2$  molecules do not prefer the bridge structure at the first stage of the adsorption. The H atoms left by the dissociation of  $\text{AsH}_3$  molecules can be either bounded to one of the open surface bonds or desorbed from the surface as  $\text{H}_2$  molecules if they are adjacent to other H atoms which are already on the surface by the previous dissociations.

In the next stage, it is found that the fragments of  $\text{AsH}_3$  molecules ( $\text{AsH}_2$  molecules) make a bridge between the available two dangling bonds on the same dimers by leaving one of the H atoms ( $\text{AsH}$ ). This result has been obtained for all optimized bridged and unbridged models considered on the up and down terraces of the step. The tendency of  $\text{AsH}$  to the bridged model was also identified for the bridges between the rows of dimers, but, the binding energy of  $\text{AsH}$  is determined to be less negative in these models. This result has indicated that  $\text{AsH}$  can prefer the bridged structures on the adjacent dimers if only the other dangling bond of its dimer is not available. Therefore depending on the available open bonds of the Ge surface,  $\text{AsH}_3$ ,  $\text{AsH}_2$ , and  $\text{AsH}$  molecules in the unbridged and bridged structures, respectively will be appeared on the surface. As it is considered above, the H atoms left by  $\text{AsH}_3$  and  $\text{AsH}_2$  molecules can be bonded to the open bonds or desorbed from the surface as  $\text{H}_2$ .

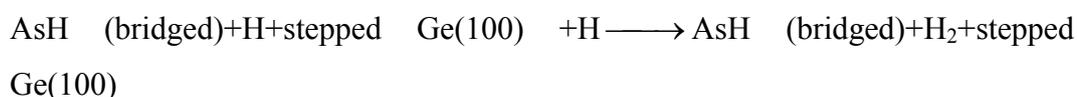
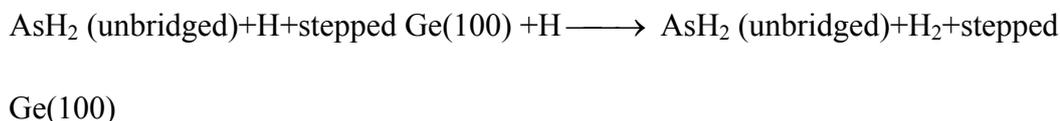
The present total energy calculations have revealed that the AsH fragment has saved its bridge structure on the dimers of both step-down and step-up terraces when it has lost its H. However, the bridge structures of AsH between the adjacent dimers have been found to be broken during the reduction of AsH to As. Therefore at the end of the dissociation steps As atom in the bridge and unbridged structures will be appeared on the stepped Ge (100) surface. Since AsH<sub>3</sub> molecules have been continuously provided in the doping process by arsine gas flow AsH<sub>3</sub>, AsH<sub>2</sub>, AsH fragments and H atoms can be totally on the surface in addition to As atoms.

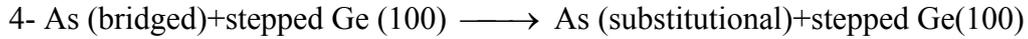
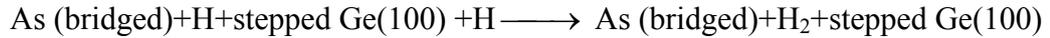
In the last stage of the doping process, As atoms diffuse towards the layers of the stepped Ge (100) surface. According to the optimized models As atoms can make bridges between the Ge atoms on adjacent layers of the substrate when they are diffusing. The total energy calculations have displayed that the As atoms have the most negative binding energy when they occupy the empty sites (irregular vacancies) of the layers of the stepped Ge(100).

The dissociation path of the AsH<sub>3</sub> molecule on stepped Ge(100) surface can be outlined by the following steps:

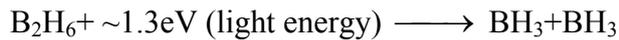


or





The doping process of the stepped Ge(100) surface by p -type dopants have been simulated by the dissociation steps of the B<sub>2</sub>H<sub>6</sub> gas molecule. In the present work, first the dissociation of B<sub>2</sub>H<sub>6</sub> has been investigated independent of the substrate. It is found that diborane gas molecule dissociates into two BH<sub>3</sub> molecules by external energy of ~1.3eV. In the literature, this first dissociation step was provided by light energy:



The total energy calculations have shown that, BH<sub>3</sub> fragments departed from B<sub>2</sub>H<sub>6</sub> molecule have suspended on the step down terrace of the Ge(100) surface when there is only one dangling bond on the surface. It is found that the actual adsorption of BH<sub>3</sub> on the surface has been provided when at least two surface bonds either on the same or adjacent dimers are open. At the first stage of the adsorption, BH<sub>3</sub> molecules have been adsorbed to the surface either directly or dissociatively, due to the number of initial adsorption bonds. When the adsorption has been satisfied by a single adsorption bond, BH<sub>3</sub> doesn't change its structure (direct adsorption). But, when BH<sub>3</sub> molecule adsorbs to the surface via double bonds (on the same or adjacent dimers) like in the initial bridge models, BH<sub>3</sub> molecule dissociates into BH<sub>2</sub>+H or BH+H<sub>2</sub>. Therefore at the first step of the adsorption of BH<sub>3</sub>, the BH fragment will be appeared on the stepped Ge(100) surface in addition to BH<sub>3</sub>, BH<sub>2</sub> molecules and H atoms. This remarkable result has showed that dissociation of BH<sub>3</sub> on Ge(100) surface can be easier than AsH<sub>3</sub>'s. The fragments, BH<sub>3</sub>, BH<sub>2</sub> and BH are found to be bounded to the surface by a single and double adsorption bonds (bridged model), respectively in the optimized models. This outcome has been confirmed with the

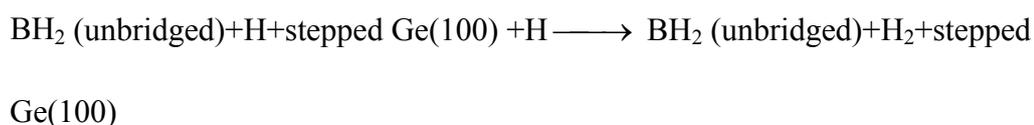
optimization of the direct adsorption models of BH<sub>2</sub> and BH. At this step of BH<sub>3</sub> adsorption, desorption of H atoms (in H<sub>2</sub> structure) from the surface has been obviously determined during the reduction of BH<sub>3</sub> to BH.

The most probable adsorption model of BH in bridged structure has been determined to be not changed when H atom is left; the surface B atoms have always preferred to make a bridge between two step down or two step up Ge atoms on the same dimers. The tendency of B atoms to make bridge structures between the Ge atoms of the adjacent layers has been also determined for the diffusion steps. But for the diffusion steps, the most negative binding energy of B atom has been calculated when B atoms have occupied the Ge sites in the layers of the substrate substitutionally.

The dissociation path of the BH<sub>3</sub> molecule on stepped Ge(100) surface can be outlined by the following steps:

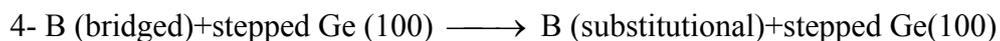
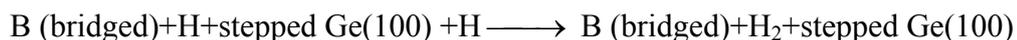


or



or





The total most probable unbridged adsorption models presented in this work are all obtained by the adsorption of AsH<sub>3</sub> and AsH<sub>2</sub> (or BH<sub>3</sub> and BH<sub>2</sub>) on buckled down side of the Ge dimer bonds. The small tilt angle initially defined for the asymmetric dimer bonds of the stepped Ge(100) surface is found to be increased in all optimized adsorption models in which one of the dangling bond of the corresponding dimer is open. Besides, the length of the dimer bond directly related to the adsorption is decreased when the adsorption is strong.

In the present work, The DOS have been also calculated for the stepped Ge(100) surface which is substitutionally occupied by As (or B) atom. The feature of As (or B) states obtained very close to the LUMO (or HOMO) in DOS spectrum has showed the beginning of the n – (or p-) type doping of the stepped Ge(100) surface.

In this project, a prototype study has been introduced for the adsorption and dissociation steps of the AsH<sub>3</sub> and B<sub>2</sub>H<sub>6</sub> on the stepped Ge(100) surface and the diffusion of As and B atoms in the layers of the stepped Ge(100) surface. Since the periodic boundary conditions are not taken into account the numerical outcomes are not compared directly with the corresponding experimental results. But the adsorption, dissociation and diffusion structures obtained in this work were confirmed either by experimental images or quantities given in the literature. The present work can be evaluated as a preliminary work for the first principles calculations and the experimental works dealing with the kinematics of the AsH<sub>3</sub> and BH<sub>3</sub> dopant molecules on the stepped Ge(100) surface.

## REFERENCES

- [1] H. Shang, H. Okorn-Schmidt, K. K. Chan, M. Copel, J. A. Ott, P. M. Kozlowski, S. E. Steen, S. A. Cordes, H. S. P. Wong, E. C. Jones, and W. E. Haensch, *Tech. Dig. Int. Electron Devices Meet.* 441 (2002).
- [2] A. B. Greytak, L. J. Lauhon, M. S. Gudiksen, and C. M. Lieber, *Appl. Phys. Lett.* 84, 4176 (2004).
- [3] C.O. Chui, and K. C. Saraswat, "Germanium Nanodevices and Technology" in *Advanced Gate Stacks for high mobility semiconductors*, vol. 27, chp. 13, p 293, edited by A. Dimoulas, E. Gusev, P. C. Mc Intyre, and M. Heyns, Springer deries in advanced microelectronics, Springer Berlin Heidelberg, (2007).
- [4] R. E. Jones, S. G. Thomas, S. Bharatan, R. Thoma, C. Jasper, T. Zirkle, N. V. Edwards, R. Liu, X. D. Wang, Q. Xie, C. Rosenblad, J. Ramm, G. Isella, H. von Känel, J. Oh, and J. C. Campbell, *Tech. Dig. Int. Electron Devices Meet.* 793 (2002).
- [5] P. R. Bandaru, S. Sahni, E. Yablonovitch, J. Liu, H. Jun Kim, and Y. H. Xie, *Mater Sci Eng. B* 113, 79 (2004).
- [6] J. M. Hartmann, J. F. Damlencourt, Y. Bogumilowicz, P. Holliger, G. Rolland, and T. Billon, *J. Cryst. Growth* 274, 90 (2005).
- [7] W. C. Dunlap Jr., *Phys. Rev.* 94, 1531 (1954).
- [8] J. S. Saby, and W. C. Dunlap Jr., *Phys. Rev.* 90, 630 (1953).
- [9] F. A. Trumbore, *Bell Syst. Tech. J.* 39, 169 (1960).
- [10] P. V. Pavlow, and V. A. Uskov, *Soviet Phys. Solid State* 8, 2377 (1967).
- [11] T. Canneaux, D. Mathiot, J. P. Ponpon, S. Roques, S. Schmitta, and C. Dubois, *Mater Sci Eng. B* 154–155, 68 (2008).

- [12] A. Satta, E. Simoen, T. Clarysse, T. Janssens, A. Benedetti, B. De Jaeger, M. Meuris, and W. Vandervorst, *Appl Phys Lett.* 87, 172109 (2005).
- [13] S. K. Mandal, S. Das, and C. K. Maiti, *Mat Sci Semicon Proc.* 8, 353 (2005).
- [14] R. J. Zambrano, F. A. Rubinelli, W. M. Arnoldbik, J. K. Rath, and R. E. I. Schropp, *Sol. Energ Mat. C* 81, 73 (2004).
- [15] L. Radic, A. F. Saavedra, K. S. Jones, and M. E. Law, *J. Vac. Sci. Technol. B* 24, 478 (2006).
- [16] M.S. Carroll, and R. Koudelka, *Semicond Sci Tech.* 22, S164 (2007).
- [17] S. Brotzmann, and H. Bracht, *J Appl Phys.* 103, 033508 (2008).
- [18] P. Tsouroutas, D. Tsoukalas, I. Zergioti, N. Cherkashin, and A. Claverie, Diffusion and activation of phosphorus in germanium. *Mat Sci Semicond Proc.*, (2008). doi:10.1016/j.mssp.2008.09.005.
- [19] Y. Kawamura, Y. Shimizu, H. Oshikawa, M. Uematsu, E. E.Haller, and K. M. Itoh, *Physica B* 404, 4546 (2009).
- [20] Y. Yamamoto, K. Köpke, R. Kurps, J. Murota, and B. Tillack, *Thin Solid Films*, 518, S44 (2010).
- [21] H. Kim and J. E. Greene, *J. Vac. Sci. Tech. A* 17, 354 (1999).
- [22] Q. Lu, T. R. Bramblett, M. A. Hasan, N.-E. Lee, and J. E. Greene, *J. Appl. Phys.* 78, 6027 (1995).
- [23] F. Gao, D. D. Huang, J. P. Li, M.Y. Kong, D. Z. Sun, J. M. Li, Y. P. Zeng, and L.Y. Lin, *J. Crys. Growth* 223, 489 (2001).
- [24] S. Kamatsu, M. Kasamatsu, K. Yamada, and Y. Moriyoshi, *J. App. Phys.* 71, 5654 (1992).
- [25] E. Tutuc, S. Guha, and J. O. Chu, *Appl. Phys. Lett.* 88, 043113 (2006).
- [26] M. Takenaka, K. Morii, M. Sugiyama, Y. Nakano, and S. Takagi, *Jpn J. of Appl. Phys.* 50, 010105 (2011).
- [27] W.E. McMahon and J.M. Olson, *J. Crystal Growth* 225, 410 (2001).
- [28] S. Gan, L. Li, M. J. Begarney, D. Law, B.-K. Han, and R. F. Hicks, *J. Appl. Phys.* 85, 2004 (1999).
- [29] E. Suvar, J. Christensen, A. Kuznetsov, and H.H. Radamson, *Mat. Sci.*

- and Eng. B 102, 53 (2003).
- [30] Chi On Chui, K. Gopalakrishnan, P. B. Griffin, J. D. Plummer, and Krishna C. Saraswat, Appl. Phys. Lett. 83, 3275 (2003).
- [31] B. A. G. Kersten, H. J. W. Zandvliet, D. H. A. Blank, and A. van Silfhout, Surf. Sci. 322, 1 (1995).
- [32] T. Sato, T. Sueyoshi, T. Amakusa, M. Iwatsuki, and H. Tochiwara, Surf. Sci. 340, 328 (1995).
- [33] H. Shigekawa, K. Hata, K. Miyake, M. Ishida, and S. Ozawa, Phys. Rev. B 55, 15448 (1997).
- [34] T. Sato, T. Iwatsuki, and H. Tachihara, J. Electron Microsc. 48, 1 (1999).
- [35] C. Tegenkamp, J. Wollschläger, H. Pfnür, F. J. Meyer zu Heringdorf, and M. Horn-von Hoegen, Phys Rev. B 65, 235316 (2002).
- [36] H. J. W. Zandvliet, Phys. Rep. 388, 1 (2003).
- [37] C. Tegenkamp, and H. Pfnür, Surf. Sci. 574, 205 (2005).
- [38] J. Wollschläger, and C. Tegenkamp, Phys. Rev. B 75, 245439 (2007).
- [39] R. M. Tromp, R.J. Hamers, and J.E. Demuth, Phys. Rev. Lett. 55, 1303 (1985).
- [40] R. J. Hamers, R.M. Tromp, and J.E. Demuth, Phys. Rev. B 34, 5343 (1986).
- [41] S. D. Kevan, Phys. Rev. B 32, 2344 (1985).
- [42] C. Collazo-Davila, D. Grozea, E. Landree, and L.D. Marks, Surf. Sci. 375, 293 (1997).
- [43] X. R. Qin, and M. G. Lagally, Phys. Rev. B 59, 7293 (1999).
- [44] K. Hata, S. Yasusda, and H. Shigekawa, Phys. Rev. B 60, 8164 (1999).
- [45] T. Shirasawa, and S. Mizumo, and H. Tochiwara, Surf. Sci. 600, 815 (2006).
- [46] B. Stankiewicz, L. Jurczyszyn, Surf. Sci. 601, 1981 (2007).
- [47] R. E. Schlier, and H. E. Farnsworth, J. Chem. Phys. 30, 917 (1959).
- [48] D. J. Chadi, Phys. Rev. Lett. 43, 43 (1979).

- [49] P. E. Wierenga, J. A. Kubby, and J. E. Griffith, *Phys. Rev. Lett.* 59 2169 (1987).
- [50] N. C. Bartelt, T. L. Einstein, and C. Rottman, *Phys. Rev. Lett.* 66, 961 (1991).
- [51] D. J. Chadi, *Phys. Rev. Lett.* 59, 1691 (1987).
- [52] H. J. W. Zandvliet, *Phys. Rev. B* 61, 9972 (2000).
- [53] J. B. Foresman and AEleen Frisch, "Exploring Chemistry with Electronic Structure Methods", Gaussian, Inc. Pittsburgh, 1995.
- [54] Chemistry 6440/7440, <http://www.slideworld.com/slideshows.aspx/Chemistry-6440--7440-ppt-519616>, last visited date 26.07.2011.
- [55] Hartree- Fock Method, [http://en.wikipedia.org/wiki/Hartre-Fock\\_method](http://en.wikipedia.org/wiki/Hartre-Fock_method), , last visited date 26.07.2011.
- [56] A. Szabo and N. S. Oslund, " Modern Quantum Chemistry: Introduction to Advanced Electronic Structure Theory", New York, McGraw-Hill 1989.
- [57] M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, V. G. Zakrzewski, J. A. Montgomery, R. E. Stratmann, J. C. Burant, S. Dapprich, J. M. Millam, A. D. Daniels, K. N. Kudin, M. C. Strain, O. Farkas, J. Tomasi, V. Barone, M. Cossi, R. Cammi, B. Mennucci, C. Pomelli, C. Adamo, S. Clifford, J. Ochterski, G. A. Petersson, P. Y. Ayala, Q. Cui, K. Morokuma, D. K. Malick, A. D. Rabuck, K. Raghavachari, J. B. Foresman, J. Cioslowski, J. V. Ortiz, B. B. Stefanov, G.Liu, A.Liashenko, P. Piskorz, I. Komaromi, R. Gomperts, R. L. Martin, D. J. Fox, T. Keith, M. A. Al- Laham,C.Y.Peng, A. Nanayakkara, C. Gonzalez, M. Challacombe, P. M. W. Gill, B. G. Johnson, W. Chen, M. W. Wong, J. L. Andres, M. Head-Gordon, E. S. Replogle and J. A. Pople, Gaussian2003 Rev. D.01(Gaussian, Inc. Wallingford CT, 2004).
- [58] C. C. J. Roothaan, *Rev. Mod. Phys.* 23, 69 (1951).
- [59] G. G. Hall, "The Molecular Orbital Theory of Chemical Valency. VIII. A Method of Calculating Ionization Potentials". *Proceedings of the Royal Society London A* 205, 541 (1951).

- [60] C. Kittel, "Introduction to Solid State Phys.," 8<sup>th</sup> Ed., USA, 2005.
- [61] Y. Yoshimoto, Y. Nakamura, H. Kawai, M. Tsukado, and M. Nakayama, Phys. Rev. B 61, 1965 (2000).
- [62] M. Needels, M.C. Payne, and J.D. Joannopoulos, Phys. Rev. B 38, 5543 (1988).
- [63] T. Shirasawa, S. Mizuno, and H. Tochiara, Surf. Sci. 600, 815 (2006).
- [64] Y. Takagi, Y. Yoshimoto, K. Nakatsuji, and F. Komori, J. Phys. Soc. Jpn. 72, 2425 (2003).
- [65] H. Ueba, Surf. Sci. 603, 831 (2009).
- [66] Y. Negishi, H. Kawamata, F. Hayakawa, A. Nakajima, and K. Kaya, Chem. Phys. Lett. 294, 370 (1998).
- [67] J. Wang, M. Yang, G. Wang, and J. Zhao, Chem. Phys. Lett. 367, 448 (2003).
- [68] Ş. Katırcıoğlu, Surf. Rev. Lett. 14, 507 (2007) .
- [69] A. Chroneos, R. W. Grimes and C. Tsamis, J. Mater. Sci:Mater Electron 18, 763 (2007).
- [70] F. Wang, W. Pang, and M. Huang, J. Electron Spectrosc. 151, 215 (2006).
- [71] T. P. Fehlner and S.A. Fridmann, Inorg. Chem. 9, 2288 (1970).
- [72] S. Komatsu, M. Kasamatsu, K. Yamada, and Y. Mariyoshi, J. Appl. Phys. 71, 5654 (1992).
- [73] B. M. Mikhailov, and Y. N. Bubnov, Organaboron Compounds in Organic Synthesis, Harwood Academic Publishers, Amsterdam, 1984.
- [74] Yu-Bo Fan, Zong-Biao Ding, Quan-Rui Wang, and Feng-Gang Tao, Chem. Phys. Let. 328, 39 (2000).