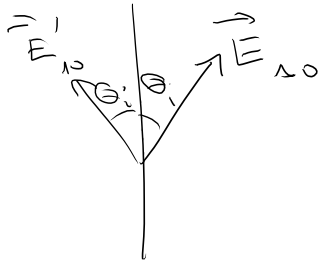


$$\vec{\nabla} \cdot \vec{D} = 0 \Rightarrow \vec{\nabla} \cdot (\epsilon \vec{E}) = 0 \Rightarrow (\epsilon \vec{E})_{\perp} \text{ is continuous.}$$

$$z < 0 \quad \vec{E}_i = E_{i0} e^{i(\vec{k}_i \cdot \vec{r} - \omega t)}$$

$$z > 0 \quad \vec{E}_r = E_{r0} e^{i(\vec{k}_r \cdot \vec{r} - \omega t)}$$



$$(\vec{E})_{\perp} = E_2 = E_{i0} \sin \theta_i - E_{r0} \sin \theta_r$$

$$z > 0 \quad \vec{E}_2 \quad (\vec{E})_{\perp} = E_{r0} \sin \theta_r$$

$$\epsilon_1 (E_{i0} - E_{r0}) \sin \theta_i = \epsilon_2 E_{r0} \sin \theta_r$$

$$\vec{\nabla} \cdot \vec{B} = 0 \Rightarrow (\vec{B})_{\perp} \text{ is continuous}$$

$$(\vec{B})_{\perp} = 0$$

$$\vec{\nabla} \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \Rightarrow E_{\parallel} \text{ is continuous}$$

$$E_{i0} \cos \theta_i + E_{r0} \cos \theta_r = E_{t0} \cos \theta_t$$

$$\vec{\nabla} \times \vec{H} = \frac{\partial \vec{D}}{\partial t} \quad \left(\frac{\vec{B}}{\mu} \right) \text{ is continuous}$$

$$\vec{H} = \frac{\vec{B}}{\mu} \quad B = \frac{E}{v} = \frac{E}{c} n$$

$$\left(E_{10} n_1 - E'_{10} n_1 \right) \frac{1}{\mu_1} = \frac{E_{20} n_2}{\mu_2}$$

$$\epsilon_1 (E_{10} - E'_{10}) \frac{n_1 \sin \theta_i}{n_1} = \epsilon_2 E_{20} \frac{\sin \theta_t}{n_2}$$

$$n_1 \sin \theta_i = n_2 \sin \theta_t$$

$$n = \sqrt{\frac{\epsilon \mu}{\epsilon_0 \mu_0}}$$

$$\frac{c}{v} = \sqrt{\frac{\epsilon \mu}{\epsilon_0 \mu_0}} \left(\frac{1}{\sqrt{\epsilon_0 \mu_0}} \right)$$

$$\frac{c}{v} = \sqrt{\frac{\epsilon \mu}{\epsilon_0 \mu_0}}$$

$$\frac{\epsilon_1}{n_1} (E_{10} - E'_{10}) = \frac{\epsilon_2 E_{20}}{n_2}$$

$$\frac{v}{c} = \frac{1}{n} \left(\frac{1}{\epsilon_0 \mu_0} \right)$$

$$\cancel{\frac{\epsilon_1}{\mu_1}} \frac{n_1}{\mu_1} (E_{10} - E'_{10}) = \cancel{\frac{\epsilon_2}{\mu_2}} \frac{n_2}{\mu_2} E_{20}$$

$$\frac{n_1}{\mu_1} (E_{10} - E'_{10}) = \frac{n_2}{\mu_2} E_{20}$$

$$(E'_{10} + E_{10}) \cos \theta_i = E_{20} \cos \theta_t$$

$$E_{10} - E'_{10} = \frac{\mu_1}{\mu_2} \frac{n_2}{n_1} E_{20}$$

$$E_{10} + E'_{10} = \frac{\cos \theta_t}{\cos \theta_i} E_{20}$$

$$2E_{10} = \left(\frac{\cos \theta_t}{\cos \theta_i} + \frac{\mu_1}{\mu_2} \frac{n_2}{n_1} \right) E_{20}$$

$$E_{20} = \frac{2}{\frac{\cos \theta_t}{\cos \theta_i} + \frac{\mu_2}{\mu_1} \frac{n_2}{n_1}} E_{10}$$

$$E_{10}' = \frac{\cos \theta_t}{\cos \theta_i} E_{20} - E_{10}$$

$$= \left[\frac{\cos \theta_t}{\cos \theta_i} \frac{2}{\frac{\cos \theta_t}{\cos \theta_i} + \frac{\mu_2}{\mu_1} \frac{n_2}{n_1}} - 1 \right] E_{10}$$

$$E_{10}' = \frac{\frac{\cos \theta_t}{\cos \theta_i} - \frac{\mu_2}{\mu_1} \frac{n_2}{n_1}}{\frac{\cos \theta_t}{\cos \theta_i} + \frac{\mu_2}{\mu_1} \frac{n_2}{n_1}} E_{10}$$

For what angle $E_{10}' = 0$?

$$\frac{\cos \theta_t}{\cos \theta_i} = \frac{\mu_2}{\mu_1} \frac{n_2}{n_1}$$

$$n_1 \sin \theta_i = n_2 \sin \theta_t$$

$$\sin \theta_t = \frac{n_1 \sin \theta_i}{n_2}$$

$$\frac{1 - \sin^2 \theta_t}{1 - \sin^2 \theta_i} = \left(\frac{\mu_2}{\mu_1} \frac{n_2}{n_1} \right)^2$$

$$\frac{1 - \frac{n_1^2}{n_2^2} \sin^2 \theta_i}{1 - \sin^2 \theta_i} = \left(\frac{\mu_2}{\mu_1} \frac{n_2}{n_1} \right)^2$$

$$1 - \frac{n_1^2}{n_2^2} \sin^2 \theta_i = \left(\frac{\mu_2}{\mu_1} \frac{n_2}{n_1} \right)^2 - \left(\frac{n_1^2}{n_2^2} \right)^2 \sin^2 \theta_i$$

$$1 - \frac{\mu_2}{\mu_1} \left(\frac{n_2}{n_1} \right)^2 = \left[\frac{n_1^2}{n_2^2} - \left(\frac{\mu_2}{\mu_1} \frac{n_2}{n_1} \right)^2 \right] \sin^2 \theta_i$$

Solution is called the Brewster angle.

